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First-Principle Investigations of Carrier Multiplication in Si Nanocrystals: a Short Review

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Abstract. Carrier Multiplication (CM) is a Coulomb-driven non-radiative recombination mechanism which leads to the generation of multiple electron-hole pairs after absorption of a single high-energy photon. Recently a new CM process, termed space separated quantum cutting, was introduced to explain a set of new experiments conducted in dense arrays of silicon nanocrystals. The occurrence of this effect was hypothesized to generate the formation of Auger unaffected multiexciton configurations constituted by single electron-hole pairs distributed on different interacting nanocrystals. In this work we discuss ab-initio results obtained by our group in the study of CM effects in systems of strongly interacting silicon nanocrystals. By solving a set of rate equations, we simulate the time evolution of the number of electron-hole pairs generated in dense arrays of silicon nanocrystals after absorption of high energy photons, by describing the circumstances under which CM dynamics can lead to the generation of Auger unaffected multiexciton configurations.

INTRODUCTION

Nano-structured third generation solar cell devices are promising systems to increase the percentage of electrical energy generated by photovoltaic (PV) modules. In order to increase photocurrent production and conversion efficiency we have to maximize the absorption of the incident solar energy and to minimize the relevance of dissipative mechanisms. In single junction solar cells, the maximum theoretical thermodynamic conversion efficiency is defined by the Shockley-Queisser limit [1], that is about the 30%. This limit moves to about 66% when multijunction solar cells are considered. The occurrence of non-dissipative recombination mechanisms like the Carrier Multiplication (CM) can reduce the impact of loss thermalization mechanisms on the solar cell performances. CM is a relaxation mechanism induced by the Coulomb interaction between carriers that leads to the generation of multiple electron-hole (e-h) pairs after absorption of a single high-energy photon (with an energy at least twice the energy gap of the system). CM has been observed in a large number of nanostructured systems, such as PbSe and PbS [2–7] CdSe and CdTe [4, 8, 9], PbTe [10], InAs [11], Si and Ge [12, 13] nanocrystals (NCs). Recently experimental evidences of new CM dynamics were observed in Photoluminescence (PL) [14–16] and in Induced Absorption (IA) experiments [17] conducted in low pulse conditions. In the first case, similarities between PL signals recorded in Er³⁺ doped Si-NCs and in Si-NCs organized in dense arrays were interpreted by hypothesizing the occurrence of a new quantum-cutting CM effect, termed space separated quantum cutting (SSQC). When this effect occurs, a high energy excited carrier decays toward the band edge (conduction band (CB) edge for electrons, valence band (VB) edge for holes) by transferring its excess energy to a nearby NC where an extra e-h pair is generated. In the second case SSQC was used to interpret IA dynamics recorded in low pulse conditions for excitations above and below the CM energy threshold; in this case the intensity recorded for the high excitation photon energy was about two times higher than the one obtained for the lower excitation photon energy, indicating an approximate doubling of the number of generated excitons. Moreover the missing of a fast decay component in the signal recorded for the high energy excitation leads to exclude the formation of Auger affected multiexciton configurations localized on the same NC [17]. In this work we review results obtained in ab-initio calculations of CM dynamics in systems of isolated and interacting H-terminated Si-NCs. Ab-initio techniques based on the Density Functional Theory (DFT) have been already applied by our group to calculate

structural, electronic, optical and transport properties of semiconductors of different dimensionality [18–30]. Here we extend the application of these theoretical tools to calculate CM lifetimes in systems of isolated and interacting Si-NCs. The calculated CM lifetimes are then introduced as parameters in a set of specific rate equations that are solved to investigate the dynamics of high energy excited states in systems of strongly interacting Si-NCs. Our outcomes are then used to discuss results of Refs. 14–16 and of Ref. 17.

METHOD

In our approach CM rates are calculated within the DFT by applying first order perturbation theory (Fermi's Golden rule) to Kohn-Sham (KS) states [31–34]. CM is therefore described as an impact ionization (II) mechanism (the inverse of the Auger recombination (AR) process) that follows the primary photoexcitation event. This scheme permits to correctly estimate CM processes for bulk systems and nanostructures [35–38]. We model the decay of an exciton into a biexciton as the sum of two processes [32, 34], one ignited by electron relaxation (decay of an electron in a negative trion, hole is a spectator) and one ignited by hole relaxation (decay of a hole in a positive trion, electron is a spectator). The simultaneous involvement of both particles (the electron and the hole) in the process is neglected in the present treatment. Finally, CM lifetimes are calculated as reciprocal of rates [39]. The CM rate $R_{n_a, \mathbf{k}_a}^e(E_i)$ for mechanisms ignited by the relaxation of an electron with energy E_i , is given by:

$$R_{n_a, \mathbf{k}_a}^e(E_i) = \sum_{n_c, n_d}^{cond.} \sum_{n_b}^{val.} \sum_{\mathbf{k}_b, \mathbf{k}_c, \mathbf{k}_d}^{1BZ} 4\pi \left[|M_D|^2 + |M_E|^2 + |M_D - M_E|^2 \right] \delta(E_a + E_b - E_c - E_d). \quad (1)$$

Similarly, for mechanisms induced by relaxation of a hole with energy E_i , we have:

$$R_{n_a, \mathbf{k}_a}^h(E_i) = \sum_{n_c, n_d}^{val.} \sum_{n_b}^{cond.} \sum_{\mathbf{k}_b, \mathbf{k}_c, \mathbf{k}_d}^{1BZ} 4\pi \left[|M_D|^2 + |M_E|^2 + |M_D - M_E|^2 \right] \delta(E_a + E_b - E_c - E_d). \quad (2)$$

The indexes n and \mathbf{k} identify KS states, 1BZ is the first Brillouin zone and $|M_D|$ and $|M_E|$ are the direct and exchange screened Coulomb matrix elements, respectively. In reciprocal space, $|M_D|$ and $|M_E|$ assume the form:

$$M_D = \frac{1}{V} \sum_{\mathbf{G}, \mathbf{G}'} \rho_{n_d, n_b}(\mathbf{k}_d, \mathbf{q}, \mathbf{G}) W_{\mathbf{G}\mathbf{G}'} \rho_{n_a, n_c}^*(\mathbf{k}_a, \mathbf{q}, \mathbf{G}')$$

$$M_E = \frac{1}{V} \sum_{\mathbf{G}, \mathbf{G}'} \rho_{n_c, n_b}(\mathbf{k}_c, \mathbf{q}, \mathbf{G}) W_{\mathbf{G}\mathbf{G}'} \rho_{n_a, n_d}^*(\mathbf{k}_a, \mathbf{q}, \mathbf{G}')$$

where both $\mathbf{k}_c + \mathbf{k}_d - \mathbf{k}_a - \mathbf{k}_b$ and \mathbf{G}, \mathbf{G}' are vectors of the reciprocal lattice, $\mathbf{q} = (\mathbf{k}_c - \mathbf{k}_a)_{1BZ}$ and $\rho_{n,m}(\mathbf{k}, \mathbf{q}, \mathbf{G}) = \langle \mathbf{n}, \mathbf{k} | e^{i(\mathbf{q} + \mathbf{G}) \cdot \mathbf{r}} | \mathbf{m}, \mathbf{k} - \mathbf{q} \rangle$ is the oscillator strength. The Fourier transform of the zero-frequency screened interaction $W_{\mathbf{G}, \mathbf{G}'}(\mathbf{q}, \omega = 0)$ is given by:

$$W_{\mathbf{G}, \mathbf{G}'}(\mathbf{q}, \omega = 0) = v_{\mathbf{G}, \mathbf{G}'}^{bare}(\mathbf{q}) + W_{\mathbf{G}, \mathbf{G}'}^p(\mathbf{q}, \omega = 0) =$$

$$\frac{4\pi \cdot \delta_{\mathbf{G}, \mathbf{G}'}}{|\mathbf{q} + \mathbf{G}|^2} + \frac{\sqrt{4\pi e^2}}{|\mathbf{q} + \mathbf{G}|} \bar{\chi}_{\mathbf{G}, \mathbf{G}'}(\mathbf{q}, \omega = 0) \frac{\sqrt{4\pi e^2}}{|\mathbf{q} + \mathbf{G}'|}. \quad (3)$$

In Eq. 3, the first term ($v_{\mathbf{G}, \mathbf{G}'}^{bare}(\mathbf{q})$) denotes the bare interaction while the second one ($W_{\mathbf{G}, \mathbf{G}'}^p(\mathbf{q}, \omega = 0)$) includes the screening caused by the medium. These terms are calculated using the many body code Yambo [40]. $\bar{\chi}_{\mathbf{G}, \mathbf{G}'}(\mathbf{q}, \omega)$ is the symmetrized reducible polarizability. Noticeably, $W_{\mathbf{G}, \mathbf{G}'}^p(\mathbf{q}, \omega)$ is often given as a function of the reducible polarization $\chi_{\mathbf{G}, \mathbf{G}'}(\mathbf{q}, \omega)$, where:

$$\bar{\chi}_{\mathbf{G}, \mathbf{G}'}(\mathbf{q}, \omega = 0) = \frac{\sqrt{4\pi e^2}}{|\mathbf{q} + \mathbf{G}|} \chi_{\mathbf{G}, \mathbf{G}'}(\mathbf{q}, \omega = 0) \frac{\sqrt{4\pi e^2}}{|\mathbf{q} + \mathbf{G}'|}.$$

The reducible polarizability is connected to the irreducible polarizability $\chi_{\mathbf{G},\mathbf{G}'}^0$ by the Dyson equation that, in the Random Phase Approximation (RPA), assumes the form:

$$\chi_{\mathbf{G},\mathbf{G}'} = \chi_{\mathbf{G},\mathbf{G}'}^0 + \sum_{\mathbf{G}_1,\mathbf{G}_2} \chi_{\mathbf{G},\mathbf{G}_1}^0 v_{\mathbf{G}_1,\mathbf{G}_2} \chi_{\mathbf{G}_2,\mathbf{G}'}.$$

The presence of off-diagonal elements in the solution of the Dyson equation is related to the inclusion of the local fields that stem from the breakdown of the translational invariance imposed by the lattice. In our approach the noninteracting response function $\chi_{\mathbf{G},\mathbf{G}'}^0$ is developed in terms of the bare Green's function, that is:

$$\chi_{\mathbf{G},\mathbf{G}'}^0(\mathbf{q}, \omega) = 2 \sum_{n,n'} \int_{\text{BZ}} \rho_{n',n}^*(\mathbf{k}, \mathbf{q}, \mathbf{G}) \rho_{n',n}(\mathbf{k}, \mathbf{q}, \mathbf{G}') \times \left[\frac{f_{n\mathbf{k}-\mathbf{q}}(1 - f_{n'\mathbf{k}})}{\omega + \epsilon_{n,\mathbf{k}-\mathbf{q}} - \epsilon_{n',\mathbf{k}} + i0^+} - \frac{f_{n\mathbf{k}-\mathbf{q}}(1 - f_{n'\mathbf{k}})}{\omega + \epsilon_{n',\mathbf{k}} - \epsilon_{n,\mathbf{k}-\mathbf{q}} - i0^+} \right] \quad (4)$$

where $f_{n\mathbf{k}}$ is the occupation factor of the $|n\mathbf{k}\rangle$ state (zero or one in our case). An exact box-shaped Coulomb cut-off technique is used in order to remove the spurious Coulomb interaction among replicas (see Ref. 41).

Systems of non-interacting NCs are simulated by placing a single freestanding NC in an cubic box. In this context H-terminated Si-NCs with diameters ranging from about 1.3 to 2.4 nm have been considered. Systems of interacting NCs are instead constructed by placing two NCs in the same simulation box at a tunable separation. In this case CM dynamics are divided in three contributions that are depicted in Fig. 1. The first one is termed one-site CM and takes into account processes that involve states localized on the same NC (blue panels of Fig. 1). The second one is the SSQC (yellow panels of Fig. 1) that leads to the generation of e-h pairs distributed on different NCs. The third one is the Coulomb Driven Charge Transfer (CDCT, orange panels of Fig. 1) that leads to the generation of positive or negative trions. SSQC and CDCT define the so called two-site CM processes. A detailed quantification of one-site CM, SSQC and CDCT processes is fundamental to interpret the experimental results of Refs. 14 and 17.

RESULTS

In this section we summarize results obtained by our group in the study of CM processes in Si-NCs. In our works [39, 42–45] we have considered four different isolated Si-NCs (the $\text{Si}_{35}\text{H}_{36}$, $\text{Si}_{87}\text{H}_{76}$, $\text{Si}_{147}\text{H}_{100}$ and the $\text{Si}_{293}\text{H}_{172}$ NCs, with diameters ranging from 1.3 nm to 2.4 nm) and two systems of interacting Si-NCs obtained by placing two different NCs in the same simulation box at a tunable separation, from 1.0 to 0.4 nm (the $\text{Si}_{147}\text{H}_{100} \times \text{Si}_{293}\text{H}_{172}$ and the $\text{Si}_{35}\text{H}_{36} \times \text{Si}_{293}\text{H}_{172}$). When first order perturbation theory is adopted to study CM effects in NCs, CM rates and CM lifetimes are given as a function of E_i .

Detailed DFT calculations of CM lifetimes in isolated Si-NCs led to conclude that (for more details see Refs. 39 and 42):

- CM is active when the initial carrier excess energy, i.e. the energy of the initial carrier E_i calculated with respect to the band edge (the CB edge for electrons, the VB edge for holes), exceed the energy gap E_g . CM lifetimes monotonically decrease with E_i from tens of nanoseconds (near the CM energy threshold) to fractions of femtoseconds (at high energies, that is far from the CM activation threshold).
- Near the CM energy threshold, CM lifetimes scatter among three orders of magnitude due to the quantum confinement effect.
- Far from the activation threshold, CM is proven to be more efficient in Si-NCs than in Si bulk.
- When an absolute energy scale is adopted, that is when CM is represented as a function of E_i , CM lifetimes seem to be independent upon NC size at high energies. We have a sort of exact compensation between the effective Coulomb matrix elements, that increase when NC's size decrease, and the density of final states that increase when NC's size increase.
- When a relative energy scale is adopted, that is when the CM is reported as a function of the ratio between the initial carrier excess energy (energy of the initial carrier calculated with respect the band edge) and E_g , CM is proven to be more efficient in small NCs.

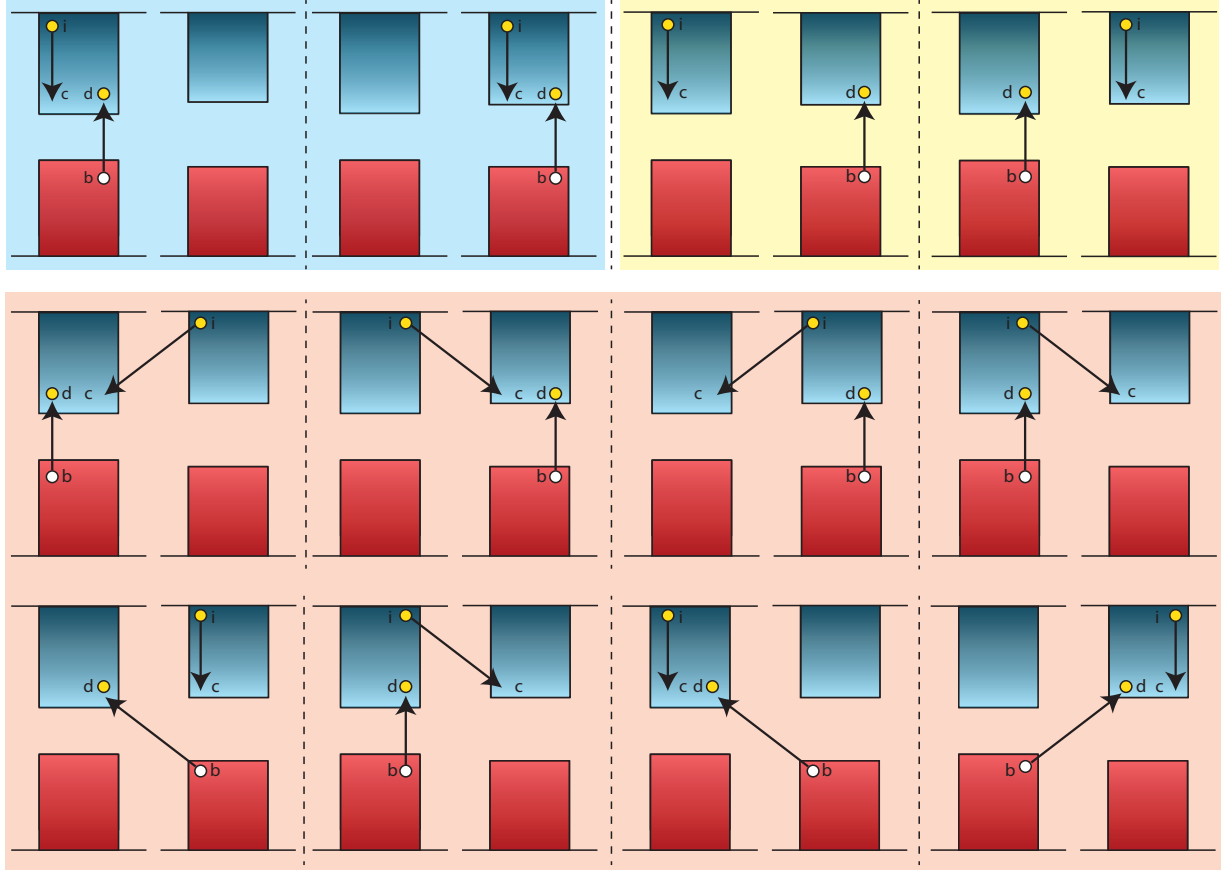


FIGURE 1. A schematic representation of one-site CM (blue panels), SSQC (yellow panels) and CDCT (orange panels) processes is reported in the figure. Reprinted with permission from Ref. 42.

By extending our analysis to the study of systems of interacting Si-NCs, that is the $\text{Si}_{147}\text{H}_{100} \times \text{Si}_{293}\text{H}_{172}$ and the $\text{Si}_{35}\text{H}_{36} \times \text{Si}_{293}\text{H}_{172}$, we observed that:

- when NC-NC separation move from 1.0 nm to 0.4 nm, NCs interplay increase and new CM decay channels are activated. The delocalization of wavefunctions over both NCs amplify the importance of two-site CM mechanisms; the relevance of both SSQC and CDCT processes increase when NC-NC separation decrease.
- Both SSQC and CDCT lifetimes decrease when E_i increase.
- When NCs are placed in close proximity, at high values of E_i , for the largest and more realistic system (the $\text{Si}_{147}\text{H}_{100} \times \text{Si}_{293}\text{H}_{172}$), SSQC lifetimes settle to few ps and CDCT lifetimes settle to fraction of ps.
- SSQC rate increases when NCs size increase. A similar behavior is not observed neither for one-site CM nor for CDCT.

Despite both SSQC and CDCT can benefit of the experimental conditions where the presence of an embedding matrix (formation of minibands) or the presence of several interacting NCs (typical condition of three-dimensional realistic systems) are expected to amplify the relevance of two-site CM processes, our results point out that one-site CM mechanisms are always faster than two-site CM processes. In particular a clear hierarchy of the CM lifetimes τ emerges from our calculations, that is:

$$\tau_{\text{one-site}} < \tau_{\text{CDCT}} < \tau_{\text{SSQC}}.$$

As a consequence, after absorption of a single high energy photon, a direct generation of single excitons distributed on different interacting NCs is not compatible with our results. Soon after the primary photoexcitation event, that is

the absorption of a high energy photon, we always have the formation of multiexcitons localized in the same NC. The interpretation of results obtained in Refs. 14–17 require therefore a more complicated scheme and cannot be ascribed only to the occurrence of SSQC processes.

In order to calculate the time evolution of the number of e-h pairs generated in a sample of strongly interacting Si-NCs after absorption of high energy photons in low pulse conditions, we solve a set of rate equations where parameters are extracted from our ab-initio simulations. The rate equations, represented by the system of Eqs. 5, describe the dynamics of Fig. 2. In this scheme we suppose that AR can be also an active and not only a destructive mechanism. The final states generated by CM (biexcitons for our NCs) are subject to AR. If AR occurs before the biexciton thermalization it can be responsible for repopulating high energy levels that lie above the CM energy threshold. The high energy e-h pair generated by AR can therefore, again, decay by CM. This new feature of the AR is defined Auger exciton recycling. Noticeably a similar idea, where AR is considered an active and not only a detrimental effect, was proposed to interpret energy transfer mechanisms in Er^{3+} doped Si-NCs [46, 47].

$$\begin{aligned} \frac{d}{dt}n_{X^*} &= -\left(\frac{1}{\tau_{\text{one-site}}} + \frac{1}{\tau_{\text{SSQC}}} + \frac{1}{\tau_{\text{relax}}}\right)n_{X^*} + \frac{f}{\tau_{\text{Auger}}}n_{XX} \\ \frac{d}{dt}n_{XX} &= -\frac{1}{\tau_{\text{Auger}}}n_{XX} + \frac{1}{\tau_{\text{one-site}}}n_{X^*} \\ \frac{d}{dt}n_X &= \left(\frac{2}{\tau_{\text{SSQC}}} + \frac{1}{\tau_{\text{relax}}}\right)n_{X^*} - \frac{1}{\tau_{\text{radiative}}}n_X + \frac{1-f}{\tau_{\text{Auger}}}n_{XX} \end{aligned} \quad (5)$$

We solve the system of Eqs. 5 by assuming an initial configuration that is represented by a high energy e-h pair X^* localized on a Si-NC (see Fig. 2). In Eqs. 5, n_{X^*} is the fraction of above CM threshold excitons X^* , n_X is the fraction of below CM threshold excitons X and n_{XX} is the fraction of biexcitons. The e-h pair X^* , generated after absorption of a high energy photon, can thermalize to the conduction and valence band edges ($X^* \rightarrow X$), can decay by CM leading to the formation of a biexciton XX ($X^* \rightarrow XX$) or can decay by SSQC leading to the formation of two e-h pairs distributed on two different NCs ($X^* \rightarrow X+X$). While SSQC leads to the formation of space separated e-h pairs ($X+X$) that can thermalize and recombine radiatively, the biexciton generated by CM can relax to the band edges or can restore a new configuration that can again decay by CM through an Auger exciton recycling procedure. The procedure above described, represented in Fig. 2, stops when thermalization mechanisms make impossible to generate active configurations that can, again, decay by CM. The scheme of Fig. 2, as implemented in Eqs. 5, permits to monitor the time evolution of the number of e-h pairs generated in the sample after absorption of high energy photons (to make the structure of such equations easier, we do not include CDCT mechanisms). Moreover, we can understand how SSQC, AR and relaxation mechanisms influence such dynamics and we can try to interpret the results obtained in pump and probe experiments conducted on Si-NCs organized in a dense arrays.

In Eqs. 5 the order of magnitude of CM one-site, SSQC and Auger exciton recycling lifetimes ($\tau_{\text{one-site}}$, τ_{SSQC} and τ_{Auger} , respectively) have been estimated by first principles calculations. Regarding τ_{Auger} , by using the same Coulomb matrix elements calculated to estimate CM lifetimes, we have proven that, for NCs of about 2 nm of diameter, τ_{Auger} settles to about 1 ps. It is important to note that this value is fully compatible with results obtained in experiments conducted on colloidal Si-NCs [12]. By assuming that biexciton lifetimes τ_{biexc} scale linearly with NC volume, we can extrapolate from the data reported in Ref. 12 the biexciton lifetime for Si-NCs of 2.4 nm of diameter by obtaining $\tau_{\text{biexc}} \approx 6$ ps. The biexciton lifetime represents however an upper limit for the Auger recycling [48], as a consequence the result $\tau_{\text{Auger}} \approx 1$ ps is totally reasonable (we note that a biexciton time of 6 ps was also obtained by Klimov et al. [49] in CdSe colloidal NCs of about 2.4 nm of diameter). Obviously the present of surface-related states can inhibit AR processes as pointed out by A. Othonos et al. [50].

The radiative recombination time $\tau_{\text{radiative}}$ is assumed to be 1 ns. The parameter f defines the fraction of X^* that are recycled from XX ; in a realistic system this fraction depends on the competition between biexciton relaxation and Auger recycling rates. Remarkably, due to the complexity of the considered systems, thermalization rates have not been calculated by first principles. Starting from results of Ref. 51, however, cooling time of the order of 1-10 ps are expected for Si-NCs with a diameter of about 2.5 nm. In our approach we will simulate dynamics of excited carriers by considering both relaxation times of few ps and relaxation time in the sub-ps region.

The results of Eqs. 5 are reported in Fig. 3 assuming $f = 1$ and an initial population equal to the 5% of X^* . In the figure the purple line denotes the total fraction of e-h pairs generated in the sample after photons absorption. Red and

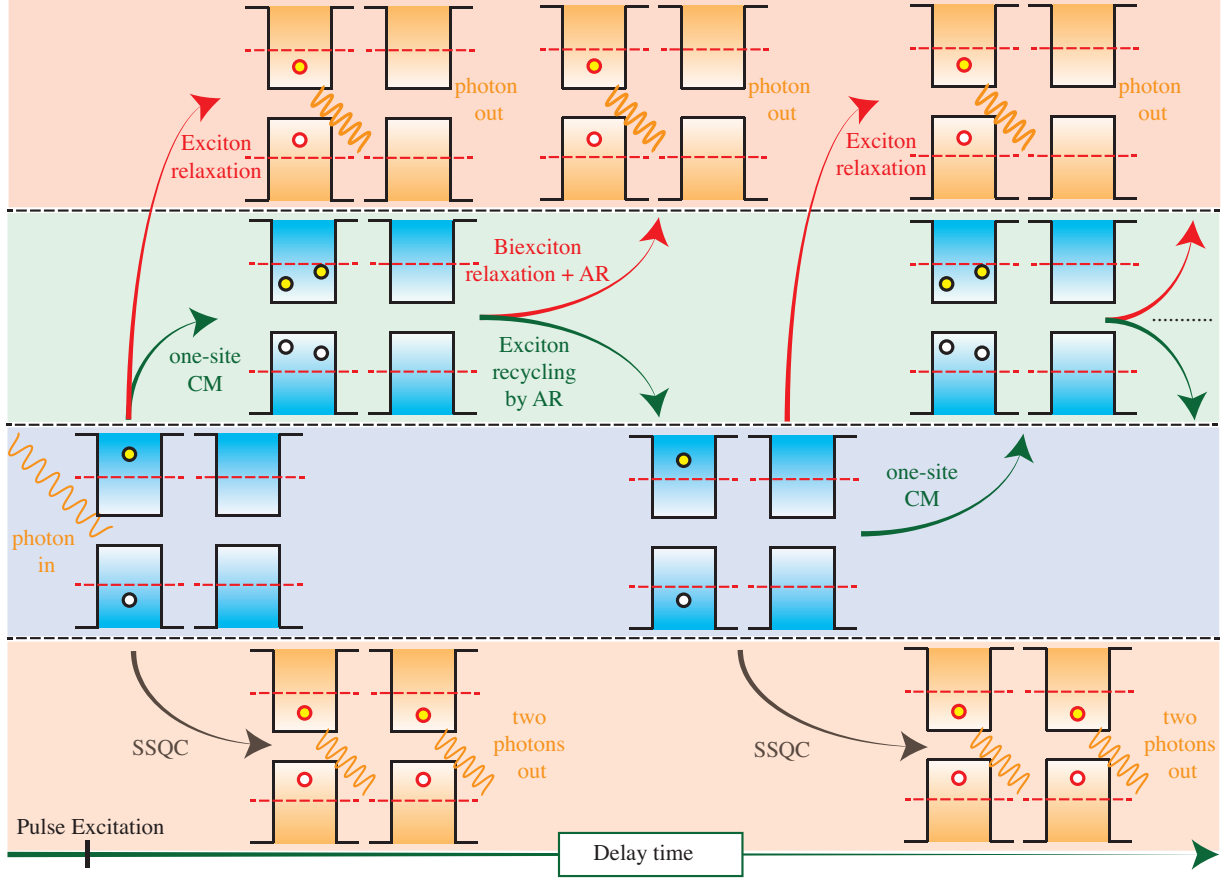


FIGURE 2. A schematic representation of dynamics represented in Eqs. 5 is depicted in the figure. An high-energy exciton X^* generated after pulse excitation can decay by CM into a biexciton XX, by SSQC into two single excitons $X+X$ or can thermalize to X. The biexciton can restore an active configuration X^* , that is an e-h pair that can again decay by CM, through an exciton recycling procedure or can relax and decay to X. X^* can decay by CM, by SSQC or can relax. The cyclic procedure stops when thermalization mechanisms make impossible to restore an active configuration X^* . Reprinted with permission from Ref. 42.

green lines represent the fraction of biexciton (XX) and single excitons ($X+X^*$) generated in the sample and reported as a function of the delay time. The parameters used for the simulations of panels (a)-(d) are reported in the caption of Fig. 3. From Fig. 3 we observe that one-site CM is responsible for probing a double number of excitons with respect to the number of absorbed photons immediately after the pulse excitation. The time evolution of the number of e-h pairs is then determined by the combination of one-site CM, SSQC, exciton recycling and thermalization mechanisms. Initially the population is dominated by biexcitons localized in single NCs (red line). Then single excitons localized on different interacting NCs emerge (green line). After the crossing of red and green lines, it is more likely the formation of two excitons in space separated NCs instead of biexcitons localized on single NCs. Time evolution of the total fraction of e-h pairs generated after photon absorption depends on both SSQC and relaxation lifetimes. Anyway the purple lines never show a fast decay component, in agreement with results of Ref. 17.

The situation change when only a fraction of biexcitons XX can recycle an active configuration X^* , that is when $f < 1$. We have considered two different situations, that is $f = 0.85$ and $f = 0.60$. Results obtained are reported in Fig. 4. It is evident that when thermalization mechanisms reduce biexcitons energies so that only a fraction of them can restore an active configuration by AR exciton recycling, a fast decay component appears in the purple line. In our model therefore dynamics of excited states are strongly connected with the competition between biexciton relaxation and exciton recycling mechanisms. When the biexciton thermalization rates are higher than exciton recycling rates the presence of an Auger fast decay component characterize the time evolution of the number of e-h pairs generated after absorption of high energy photons also in cases where low pulse conditions are verified. Here more complicated

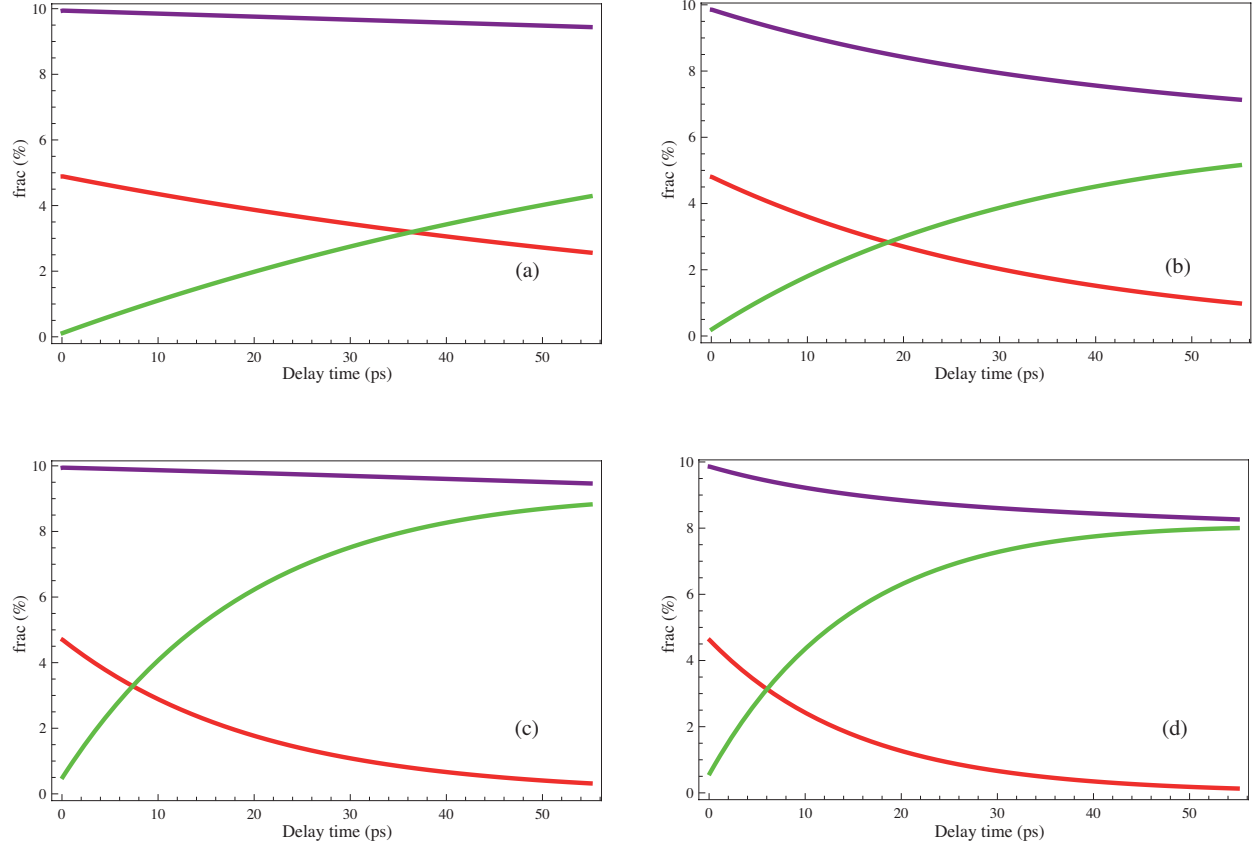


FIGURE 3. The solution of Eqs. 5 are reported in the figure. We assume that only the 5% of NCs are excited by high energy photons (low pulse conditions). The purple line indicates the total fraction of e-h pairs generated in the sample. Green and red lines represent the fraction of biexcitons and single excitons. Calculations have been performed assuming $\tau_{\text{one-site}} = 0.01$ ps, $\tau_{\text{Auger}} = 1$ ps, and $\tau_{\text{radiative}} = 1000$ ps. From panel (a) to panel (d) we have $\tau_{\text{SSQC}} = 1$ ps and $\tau_{\text{relax}} = 5$ ps, $\tau_{\text{SSQC}} = 1$ ps and $\tau_{\text{relax}} = 0.5$ ps, $\tau_{\text{SSQC}} = 0.2$ ps and $\tau_{\text{relax}} = 5$ ps, $\tau_{\text{SSQC}} = 0.2$ ps and $\tau_{\text{relax}} = 0.5$ ps. We assume here that the biexciton is always recycled ($f = 1$). Reprinted with permission from Ref. 42.

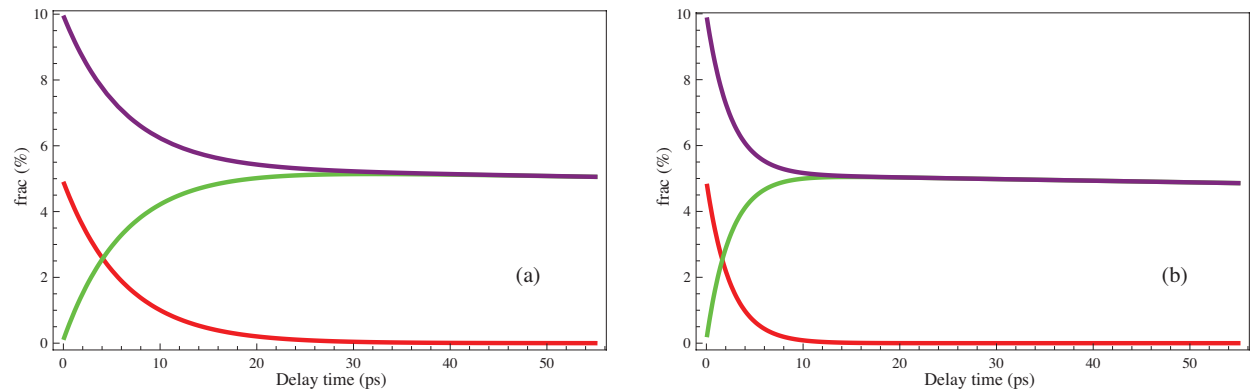


FIGURE 4. Solutions of Eqs 5 are reported in the figure for $f = 0.85$ (panel a) and $f = 0.60$ (panel b). We assume $\tau_{\text{SSQC}} = 1$ ps and $\tau_{\text{relax}} = 5$ ps. Reprinted with permission from Ref. 42.

models have to be proposed in order to explain results of Ref. 17.

CONCLUSIONS

In this work we have reviewed some of the results obtained by our group in the study of the CM processes in systems of isolated and interacting Si-NCs. In particular we have shed light on the dependence of the CM dynamics on NCs size and we have summarize the effects induced by NCs interplay on CM dynamics. In order to interpret a set of pump and probe experiments conducted on Si-NCs organized in a dense array we have solved a set of rate equations where the parameters have been determined by first principle calculations. In the implementation of such equations we have re-interpreted the idea of Auger recombination that is now considered also an active and not only a destructive process. This new feature of the Auger has been defined Auger exciton recycling. We have proven that when Auger exciton recycling mechanisms are faster than biexciton relaxation processes our results can explain experimental evidences.

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