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1 2 2	A COMBINED NUMERICAL APPROACH FOR THE THERMAL ANALYSIS OF A PISTON WATER PUMP
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7	ABSTRACT
8 9 10 11	The paper proposes a numerical model for the investigation of a piston water pump under different operating conditions. In particular, the lubricating system is analysed and modelled. The study accounts for the lubrication and friction phenomena, heat transfer, multiphase fluid approach and motion simulation.
12 13 14 15 16 17 18 19 20	A computational thermo fluid dynamics approach has been adopted to develop a numerical tool able to simulate the behaviour of the oil during the machine working phases. The CFD approach simulates the moving metal components by means of moving meshes techniques; the friction phenomenon is estimated on the basis of formulations available in literature. The numerical model evaluates the heat transfer between moving metal parts and oil during the operating phases of the system. Furthermore, the heat transfer between oil and environment is calculated, accounting for conduction through the metal crankcase walls. A multiphase fluid approach is used for the simulation of the oil and air mixing during the crank rotation.
21 22 23 24 25 26	The heat transfer coefficient predicted by the CFD approach are employed in a lumped and distributed numerical model; the reliability and accuracy of the proposed numerical approach is addressed and validated against experimental results. Experimental data have been collected by means of a thermographic camera and thermocouples. Finally, the tool's predictive capabilities are addressed by simulating different working conditions.
27 28	KEYWORDS: heat transfer, friction, piston water pump, CFD, lumped parameter, moving mesh.
29	1. INTRODUCTION
30	Water piston pumps are largely employed in many industrial applications, but they are

31 mainly used in the urban sector, fitted on drain cleaning trucks, waste bin washers and 32 road sweepers. Bigger size pumps are used for ship keels cleaning. Due to the machine versatility, the pump can operate continuously or not; in addition, it can be used in cold 33 country as well as in hot places. Thus, it is fundamental to project the machine in order 34 to ensure the necessary heat transfer from the internal moving parts to the external 35 environment. Therefore, overheating must be avoided to guarantee the performance and 36 37 the lifetime of the pump itself for each working condition. A key role is played by 38 lubricant oil which is the transfer fluid that transmit the heat from cranks, rods, pistons 39 and crankshaft to the crankcase walls.

A great support can be offered to engineers by numerical simulations, in order to predict
heat transfer for different working conditions of many systems and components. In
particular, computational fluid dynamics models are largely employed to describe the

thermo fluid dynamics behaviour of various machines. Bhutta et al. [1] presented a

44 complete review of CFD analysis of heat exchangers. Different turbulence models and

45 velocity-pressure coupling schemes have been compared, for a wide variety of heat

46 exchanger architectures. In this regard, H. Mroue et al. [2] investigated the performance

of a heat exchanger equipped with six thermosyphons by means of a CFD approach

- 48 without simulating the two-phase change that occurs inside the thermosyphons; an
- 49 overview of numerical models used to investigate the condensation, evaporation and
- 50 boiling in these systems can be found in [3].

51 Within the context of centrifugal pumps, a critical review of different CFD models has

52 been presented by Shah et al. [4] in order to outline the most interesting areas of

research to improve the pump performance: cavitation analysis, diffuser pump analysis,

volute flow study and impeller-volute interaction.

55 In order to simulate the thermo fluid dynamics behaviour of the oil inside the crankcase,

56 different phenomena must be accounted for. Firstly, attention should be devoted to the

57 movement description of cranks, rods, pistons, and crankshaft that caused the oil-air

- 58 mixing (splash lubrication). Moving meshes give the possibility to the user to include
- moving parts, based on equations well known in literature [5, 6]. This numerical
 technique is expensive in terms of computational resources, but it ensures good
- accuracy in modelling moving parts and solid fluid moving interfaces. Menéndez
- 62 Blanco and Fernández Oro [7], for instance, used this numerical approach to construct a
- model of an air-operated piston pump for lubricating greases. Subsequently, it is
- 64 necessary to calculate the thermal energy introduced into the system by friction.

Different approaches can be found in literature [5, 6, 8, 9, 10, 11], referred to analysis of

- 66 engine pistons. Indeed, piston water pumps and engines present similar architectures of
- pistons, crank mechanisms, rings. In particular, detailed descriptions of the friction
 between the piston rings and the cylinder wall have been outlined by Cho and Moon [6]
- and by Livanos and Kyrtatos [8], while Tateishi [9] proposed an empirical
- approximation. One of the most applied equation in numerical modelling is the Chen
- and Flynn correlation [10], used also by Hooper et al. [11] to successfully simulate a
- stepped piston engine using one dimensional CFD approach. Once calculated the heat
- released by friction, fluid properties and heat transfer models must be defined. The fluid
- is described as a two phases mixture of air and oil; thus, the volume of fluid (VOF)
 approach is used. Several examples of VOF simulations are available in literature

76 applied to different contexts. Jouhara et al. [12] simulated flow and heat transfer in a

thermosyphon: by means of VOF technique, evaporation and condensation wereaccounted for as well as the interaction between gas and liquid. Lückmann et al. [13]

78 accounted for as well as the interaction between gas and inquid. Luckmann et al. [1 79 applied the numerical method to resolve the free-surface oil flow in a lubricant oil

80 pumping system of a reciprocating compressor.

In [14] a numerical approach has been used to predict the transient behaviour of a

82 lubrication in a wet clutch of a hydromechanical variable transmission; the volume of

fluid approach has been employed in the numerical model in order to determine the oil
distribution in the clutch region under different rotating velocities. A similar study was

conducted by Terzi et al [15] where a VOF approach has been used to determine the

86 lubrification flow within a multi-plate wet clutch.

Air and oil physical properties need to be updated on the basis of the temperature field: while air property correlations are included in the library of the software, oil ones have

to be provided. Habchi et al. [16] developed and validated models of pressure and

90 temperature dependencies of standard oil properties. Heat transfer problems have been

- 91 widely simulated by means of numerical models, especially for heat exchangers [1].
- Also heat transfer in cylinder walls has been largely studied: Rakopoulos et al. [17]

- 93 compared different heat transfer formulations. In this paper, dimensionless numbers [18,
- 19] are involved in correlations [20, 21] able to described the heat transfer coefficient in
- a very simple way. Brucker and Majdalani [20] presented a comprehensive table of
- 96 Nusselt number expressions for different geometries, flow conditions and ranges of
- validity. In particular, the equation proposed by Churchill and Chu [21] is used to
- calculate the Nusselt number that characterized the heat transfer between the crankcase
- walls and the environment. A similar approach has been successfully used by Bottazziet al. [22] to construct and to develop a numerical model able to simulate the thermo-
- dynamics behaviour of a coffee roasting machine and, in particular, the heat transfer
- from a hot air flow to coffee beans during toasting phases.
- The aim of this study is the development of a numerical tool that can be used for the
 investigation of lubricating system for piston water pump in order to design new
 crankcase and to improve existing components.
- Thus, the model is intended to predict the influence of the various parameters that characterize the heat transfer between oil and metal parts, such as surface geometry, temperature and oil mixing. The main goal of the numerical tool is to predict the evolution of the temperature map in order to define the steady value for different working conditions.
- 111 Finally, the accuracy of the numerical results of the proposed model are validated
- against experimental data. The experimental measurements+ are collected by means of
- thermocouples and a thermographic camera applied to a standard pump tested for
- 114 different working conditions.

115 2. CFD MODEL

Piston water pump are generally composed of three alternative pistons, with 120° of 116 angular displacement between each one. A complete numerical model of the pump can 117 be obtained joining three single models representing one piston. Thus, initially, a single 118 model regarding a crank, a rod and a piston is developed. Once prepared the geometry, 119 120 the mesh is constructed. As previously said, moving mesh technique is applied in order to simulate the splash lubrication effects. Motion of each moving part need to be 121 modelled. Thus, energy dissipated due to the friction is estimated and introduced into 122 the system. For fluid modelling, a "Volume of Fluid" approach is used, in order to 123 describe the two phases mixture of oil and air. Oil properties are expressed as a function 124 of the temperature. Finally, heat transfer from metal moving part to the environment is 125 defined by means of dimensionless formulations. The implementation of all these 126 features is necessary in order to ensure a good accuracy of the model, but it determines 127 a high computational effort. In addition, the heat transfer phenomenon is a slow 128 mechanism that requires a long computational time. Thus, a 2D model is used in order 129 to obtain a model that can be usefully adopted by pump designers: indeed, the model 130 accuracy is important as well as the possibility to obtain the results in a reasonable time. 131 Once all the features are properly configured in the 3D single piston model, it is 132 possible to automatically scale from the 3D to a 2D model using a section plane that 133 includes the axis of the central piston and that is perpendicular to the pump base. 134

135

136 2.1 Motion model

137 The single piston model accounts for two moving parts: the rod and the piston. Both the 138 motions of the rod and the piston are simulated by means of moving mesh technique. In the first case, two blocks are constructed: a fixed one, that is the void of the crankcase,
and a moving one that accounts for the rod. Indeed, this last one is a box that includes
the rod and that moves inside the fixed block. This movement is the rod motion and it is
possible to define it with a geometrical analysis [5]. Referring to the layout of Fig. 1,
rod position on a plane *XY* is described by Eq. 1 and Eq. 2:

144
$$x_B = r_c \cdot \cos(\omega \cdot t - \pi)$$
(1)

145
$$y_B = r_c \cdot \sin(\omega \cdot t - \pi)$$

146 (2)

where x and y are the position coordinates of the point B referred to the fixed system 147 148 shown in Fig. 1; r_c is the eccentricity, i.e. the crank length, ω is the rotational velocity, t is the time, $-\pi$ is summed because the simulation starts when the piston is at the bottom 149 dead centre (BDC). A roto-translation of rigid body is defined when the motion of a 150 generic point J (Eq. 3) is known. Considering the generic point J, its movement respect 151 the fixed coordinate system can be described as the vectoral sum of the translation 152 velocity of a moving system and the rotational velocity referred to that system. The 153 moving coordinate system is constructed with axes parallel to the ones of the fixed 154 system and origin in B. The rotational axis coincides to the Y axis of the moving system. 155

156
$$\vec{v}_{totJ} = \vec{v}_{transB} + \dot{\beta}_B \times \overline{BJ}$$
 (3)

157 The components of the translational velocity of the moving system are expressed by Eq.158 4 and Eq. 5, while the angular velocity is calculated with Eq. 6.

159
$$\dot{x}_B = -\omega \cdot r_c \cdot \sin(\omega \cdot t - \pi)$$
 (4)

160
$$\dot{y}_B = \omega \cdot r_c \cdot \cos(\omega \cdot t - \pi)$$
 (5)

161
$$\dot{\beta}_{B} = \lambda \cdot \omega \cdot \left(\frac{\cos(\omega \cdot t)}{\sqrt{1 - \lambda^{2} \cdot \sin^{2}(\omega \cdot t)}} \right)$$
 (6)

162 Deriving Eq. 1 and Eq. 2 respect time, it is possible obtain Eq. 3 and Eq. 4. With simple 163 mathematical steps (see Appendix A) it is possible to determine Eq. 6, where λ is the ratio 164 between crank and rod length. The software automatically applies Eq. 3 to all the cells of 165 the moving mesh, once introduced Eq. 4 and Eq. 5 and Eq. 6.

Once the rod movement is detailed, piston motion is simulated. To do that, a second
overset mesh is configured. As done for the rod, the void of the crankcase is used as
fixed block, while a moving block accounts for the piston. The motion is a translation of
a rigid body and it can be described on the basis of the motion equation of the small end
connecting rod (point A in Fig. 1) obtained from the analysis of a generic crank-rod
mechanism (see Appendix A).

172
$$\dot{x}_{A} = r_{c} \cdot \omega \cdot \left[\sin \alpha + \frac{\lambda \cdot \sin 2\alpha}{2 \cdot \sqrt{1 - \lambda^{2} \cdot \sin^{2} \alpha}} \right]$$
 (7)

The two moving blocks of the overset mesh zones are overlapping each other; thus, a third overset interface has to be configured in order to assign the correct behaviour to each cell that are positioned in the overlapping region between rod and piston blocks.





Fig. 1. Crank-rod mechanism, reference system.2.2 Friction model

Friction analysis has a key role to assess the dissipated energy. It is very useful to assess 180 181 at each contact surface the amount of energy that is released as heat. Unfortunately, no studies are available in literature that investigate friction evaluation on a piston water 182 pump. On the contrary, there are some interesting works accounting for friction on an 183 internal combustion engine [5, 6, 8, 9, 10, 11]. Water piston pumps and engines 184 presented a quite similar architecture, in terms of crank-connecting rod mechanism, 185 186 piston and rings. Dissipated energy due to friction in an engine, is frequently calculated 187 as a whole, on the basis of energy balance, but in a few cases it is possible to found approximated correlation regarding the various contact surfaces. 188

189 According to Heywood [5], Eq. 8 can be used to calculate the friction force F_{f_rbe} 190 referred to the contact between the connecting rod big end and the crankshaft, under the 191 hypothesis of continuous oil film between the surfaces:

192
$$F_{f_{rbe}} \approx \left(\pi \cdot d_{rbe} \cdot l_{rbe}\right) \cdot \mu_{oil} \cdot \left(\frac{\pi \cdot d_{rbe} \cdot \omega}{\overline{c}_{rbe}}\right) = \frac{\mu_{oil} \cdot \pi^2 \cdot d_{rbe}^{-2} \cdot l_{rbe} \cdot \omega}{\overline{c}_{rbe}}$$
(8)

193 Where d_{rbe} is the internal diameter of the connecting rod big end, l_{rbe} is the contact 194 length (thickness of connecting rod big end), μ_{oil} is the oil dynamics viscosity, \overline{C}_{rbe} is 195 the mean radial clearance. Once obtained the friction force by means of this 196 approximated approach, it is possible to determine the related friction torque M_{f_rbe} (Eq. 197 9) and the dissipated power P_{f_rbe} (Eq. 10):

198
$$M_{f_{-}rbe} = F_{f_{-}rbe} \cdot d_{rbe} / 2$$
 (9)

$$199 \qquad P_{f_rbe} = M_{f_rbe} \cdot \omega \tag{10}$$

The same approach can be applied to assess the dissipated power P_{f_rse} referred to the contact surface between the connecting rod small end and the pin. This contact, in fact, presents a similar geometry configuration (cylinder vs. cylinder contact surface) and an analogous lubrication condition. Another important contribution to the energy dissipation is the friction between the crankshaft and the two needle bearings. An approximated method to choose size the component is provided by producers. Each needle bearing supports a force F_{f_rnb} :

207
$$F_{f_nb} = p_{\text{max}} \cdot (\pi \cdot d_p^2 / 4) \cdot n_p / 2$$
 (11)

where p_{max} is the water maximum pressure, d_p the piston diameter, n_p the number of pistons. Obviously, the force is divided by two because there are two needle bearings. The related friction torque M_{f_nb} can be calculated by means of Eq.12:

211
$$M_{f_nb} = 0.5 \cdot C_f \cdot d_{nb} \cdot F_{f_nb}$$
(12)

where C_f is the constant friction coefficient, value characteristic of the bearing

architecture and tabulated by the producers, d_{bn} is the internal diameter of the

- component (where the crankshaft is connected). Thus, the related dissipated power canbe assessed by Eq. 10.
- In order to complete the friction evaluation, two additional dissipated power terms have 216 217 to be accounted for: the first one is due to the contact surface between the seal placed in 218 the cylinder wall and the ceramic piston part (P_{f_ring}) and the second one is referred to the friction between the journal box and the piston $(P_{f_{-ib}})$. To calculate these two terms, 219 several approaches referred to engine pistons are available in literature [8, 9] but in this 220 221 case to consider the piston water pump as an engine is a poor approximation, due to the different ring kind and number for each piston and due to the different pressure curve 222 during the cycle. A different approach can be based on efficiency analysis. The ratio 223 224 between hydraulic (P_{hyd}) and mechanical (P_{mech}) power is the total efficiency of the 225 pump η_{tot} :

226
$$\eta_{tot} = \frac{P_{hyd}}{P_{mech}} = \frac{Q \cdot (p_{max} - p_{suc})}{\omega \cdot M_{max}} = \eta_{vol} \cdot \eta_{hm}$$
(13)

where *Q* is the flow rate, p_{suc} the pressure at the pump suction and M_{max} the maximum torque, referred to the maximum pressure p_{max} . The total efficiency η_{tot} is equal to the product of volumetric efficiency η_{vol} and hydromechanical efficiency η_{hm} :

230
$$\eta_{vol} = Q / \left[3 \cdot \omega \cdot \left(2 \cdot r_c \right) \cdot \left(\pi \cdot d_p^{-2} / 4 \right) \right]$$
(14)

- while η_{vol} is defined as the ratio between the flow rate and the ideal geometrical flow rate, η_{hm} can be obtained on the basis of experimental data combining Eq. 14 with Eq.
- 13. The total dissipated power $P_{f_{tot}}$ can be calculated as:

234
$$P_{f_{tot}} = P_{hyd} \cdot (1 - \eta_{hm}) = 2 \cdot P_{f_{nb}} + 3 \cdot (P_{f_{rbe}} + P_{f_{rbe}} + P_{f_{rbe}} + P_{f_{rbe}} + P_{f_{rbe}})$$
(15)

afterwards, subtracting the previously calculated terms of dissipated power, it is

- possible to estimate the sum of the two investigated terms. Based on producer's know-
- how, the ratio between the terms is fixed: thus, P_{f_ring} and P_{f_jb} can be separately assessed.
- The total friction losses on the piston is calculated by both the proposed approach and the Chen and Flynn correlation [10] and the results are compared as a check. This empirical correlation is one of most used technique to estimate the total dissipated power due to the friction in combustion chamber simulation. Both the approaches provide results of the same order.
- In the constructed model, the dissipated power terms are included as thermal flux from
- the contact surface to the fluid. The rod is made of aluminium, that is a good conductor; thus, the hypothesis of uniform energy distribution can be assumed and both P_{f_rbe} and
- 247 $P_{f_{-rse}}$ are addressed to the external rod surface. A uniform energy distribution is also

supposed assigning P_{f_jb} to the part of the cylinder internal wall that is immersed in oil. P_{f_ring} is referred to the cylinder and the piston parts those work in contact with water and do not influence the oil behaviour: thus, P_{f_ring} is not included in the numerical model. $P_{f_nb_i}$ instead, must be accounted for in the overall numerical model of the pump but not in the single piston model.

253

254 2.3 Fluid model

The fluid inside the crankcase is modelled as a multiphase non reacting mixture by means of the Volume of Fluid approach. The spatial distribution of each phase at a given time is defined in terms of volume fraction. The Segregated Flow model is used to solve the conservation equations separated for each phase, except for the pressure field which is common. In this study, also the temperature field has to be accounted for; the model used is the Segregated Multi-Phase Temperature.

261 The two phases considered are air and lubricant oil. While the air physical properties are included in the software data base as temperature and pressure dependant, the oil ones 262 must be provided by the user. The temperature influence on density and viscosity at 263 264 atmospheric pressure can be obtained from the oil data sheet. In order to define the heat transfer, also oil thermal properties have been detailed. Brucker and Majdalani [20] 265 proposed empirical correlations pressure and temperature dependant to calculate 266 specific heat c_{poil} and thermal conductivity k_{oil} of an oil similar to the one used in the 267 268 piston water pump.

269
$$k_{oil} = C_0 + C_1 \cdot \left\{ V_{oil_ref} \right\} \cdot \left[1 - 0.101 \cdot \left(T_{oil_ref} \right) \cdot \left(V_{oil_ref} \right)^3 \right]^{-7.6}$$
(16)

270
$$c_{P_{oil}} = \left[C_2 + C_3 \cdot \left(T_{oil_ref}\right) \cdot \left(V_{oil_ref}\right)^{-4}\right] / \rho_{oil}$$
 (17)

The oil volume and temperature at actual conditions are V_{oil} and T_{oil} while V_{oil_ref} and 271 T_{oil_ref} are related to reference values; C_0 , C_1 , C_2 and C_3 are empirical coefficients and 272 ρ_{oil} is the oil density. During the working condition of the pump, the oil in the crankcase 273 274 is constantly at atmospheric pressure; thus, the two equation can be simplified because the $V_{oil}/V_{oil_{ref}}$ ratio is equal to 1. In fact, the pump has a breather plug and the model 275 accounts for it by means of an air inlet at the atmospheric pressure (see Fig. 2). Thus, 276 only air can enter the crankcase but both oil and air can exit. In particular, a very small 277 278 amount of oil can exit from the breather plug, if it is thrown to the plug by the moving rod. All the other surfaces are considered as "wall" (no mass transfer is allowed by the 279 boundaries between internal crankcase and the environment). 280



Fig. 2. Lumped parameter model, layout of the whole pump

- 284
- 285 2.4 Heat transfer model

286 Once calculated the dissipated power due to friction and modelled the two-phases fluid 287 mixture, heat transfer must be defined. From the surfaces interested by power 288 dissipation, the heat is transferred to the fluid. Heat transfer between the two phases are 289 automatically included, as well as convection between the fluid and the crankcase 290 internal walls. In order to account for the thermal power transferred (W_{cond}) through the walls due to the conduction phenomenon, Eq. 18 is used: $T_{wall_{int}}$ and $T_{wall_{ext}}$ are, 291 292 respectively, the internal and external wall temperature, S_{wall_int} is the heat transfer surface and R_{wall} the wall thermal resistance. 293

294
$$W_{cond} = \left(T_{wall_int} - T_{wall_ext}\right) \cdot S_{wall_int} / R_{wall} = \left(T_{wall_int} - T_{wall_ext}\right) \cdot S_{wall_int} / \left(S_{wall} / k_{wall}\right) (18)$$

The wall thermal resistance R_{wall} has been evaluated based on the wall thickness s_{wall} and the thermal conductivity k_{wall} of the metal. Afterwards, the thermal power W_{conv} is dissipated towards the environment (natural convection) and it can be calculated as

proposed in Eq. 19.

299
$$W_{conv} = \left(T_{wall_ext} - T_{env}\right) \cdot S_{wall_ext} \cdot h_{wall_ext}$$
(19)

- 300 The environment is at atmospheric pressure and its temperature is T_{env} , the transfer
- 301 surface is the external area S_{wall_ext} of the crankcase and h_{wall_ext} is the heat transfer
- 302 coefficient. In order to define this parameter, a non-dimensional approach is used. It is
- possible to evaluate the Nusselt number Nu_{wall_ext} as a function of the Reynolds number Re_{wall ext} and of the environment Prantl number Pr_{env} (see Apeendix B). Once obtained
- Nu_{wall_ext} the heat transfer coefficient can be calculated according to Eq. 20, where
- l_{wall_ext} , the near transfer coefficient can be calculated according to Eq. 20, where l_{wall_ext} is a characteristic length of the transfer surface and k_{env} is the thermal
- 307 conductivity of the environment.
- $\sum_{k=1}^{\infty} N_{k} = -\frac{h}{k} \sum_{k=1}^{\infty} \frac{h}{k} = -\frac{h}{k} \left(\frac{h}{k} \frac{h}{k} \right)$

308
$$Nu_{wall_ext} = (h_{wall_ext} \cdot l_{wall_ext}) / k_{env} = f(\operatorname{Re}_{wall_ext}, \operatorname{Pr}_{env})$$
 (20)

The connecting function must be chosen based on the transfer surface shape, the flow conditions, the validity range of the non-dimensional numbers. Brucker and Majdalani [20] shown a comprehensive table of Nusselt number correlations for all these parameters. Equation 21 had been proposed by Churchill and Chu [21] and it was developed for natural convection from a planar surface and for $10^0 < Ra < 10^9$.

314
$$Nu_{wall_ext} = 0.68 + \frac{0.67 \cdot Ra_{wall_ext}^{1/4}}{\left(1 + 0.67 \cdot \Pr_{env}^{-9/16}\right)^{4/9}}$$
 (21)

- 315 where Ra_{wall_ext} is the Rayleigh number, obtained by multiplying the Grashof number,
- 316 Gr_{wall_ext} , referred to the external crankcase surface and the Prandtl number, Pr_{env} , of the 317 external ambient (see Appendix B). In order to calculate the Grashof number, the
- 219 volumetric thermal expansion coefficient of the sir h has to be taken into account.
- 318 volumetric thermal expansion coefficient of the air b_{env} has to be taken into account:

319
$$b_{env} = -\frac{1}{\rho_{env}} \cdot \left(\frac{\partial \rho_{env}}{\partial T_{env}}\right)_p = \frac{1}{\rho_{env}} \cdot \frac{p_{env}}{Rg \cdot T_{env}^2} = \frac{1}{T_{env}}$$
 (22)

- As proposed by Incropera and DeWitt [18], the air can be considered as an ideal fluid for the evaluation of the volumetric thermal expansion coefficient; thus, it can be assumed to be equal to approximately 1/T, where *T* is the absolute temperature of the gas (see Eq. 22).
- 324

325 3. LUMPED PARAMETER MODEL

In order to obtain a complete analysis of the overall machine, a lumped and distributed 326 parameter model is constructed. Indeed, the developed 2D CFD model designed to 327 describe the thermo-fluid dynamic behaviour of the lubricating system but is not 328 applicable for a detailed study of the pump due to the high computational effort. In 329 other words, an overall CFD model that includes both lubricating system and pumping 330 zone, will cause an high computational resource request and long-time simulations; 331 thus, a lumped and distributed parameter approach is the best compromise between 332 computational effort and results' accuracy in order to develop a model that can be able 333 334 to show the results in an admissible time and ensuring a good predictive capability.

As depicted by Fig. 2, the model of the pump is constructed connecting two main parts: the pumping side, where the operating fluid, water, is addressed by the piston chamber evolution from the suction to the delivery, and the mechanical side, where the lubricating system is placed. The model accounts for the thermo-dynamics behaviour of both sides; in particular, the heat transfer between the pump cylinder head and the

- 340 water, the crankcase and the pump cylinder head, the lubricating fluid and the
- 341 crankcase, are included. There are parameters that can not be fixed on the basis of
- 342 geometrical or physical information: in order to obtain these data, such as the
- 343 convective heat transfer coefficient of each wall, the 2D CFD simulation is
- fundamental. On the other hand, the lubricating system simulation requires to fix the
- heat transferred from the crankcase to the pump cylinder head. Thus, the CFD
- 346 lubricating system model and the lumped parameter model of the pump are deeply
- 347 dependant each other and they need to be simultaneously developed.
- 348
- 349 3.1 Pumping side model

The piston chamber evolution of each of the three pistons, properly phased, is accounted for by this part of the model. Particular care is devoted to the modelling of the opening characteristic of the suction and delivery automatic valves by means of an accurate geometrical definition; in addition to this, the spring displacement –force relationship and the moving parts mass are also included. To complete the layout, the suction and delivery line are considered, as well as the tank at the atmospheric pressure value and an orifice used as pump load.

357 The hydraulic behaviour predicted by the model is tailored by means of experimental data, in terms of load pressure and flow rate and volumetric efficiency. The heat transfer 358 between the pumping side and the mechanical side is permitted by means of the 359 360 crankcase - pump cylinder head contact interface and by the ceramic piston part - metal piston part contact interface; these contact interfaces accounted for conduction, as well 361 as convection phenomena. In fact, while the pump cylinder head and the ceramic piston 362 363 part are cooled by the water flow, the crankcase and the metal piston part are in contact 364 with the oil and they are hooted by the power dissipation due to the friction, as explained above. In addition, there is an amount of energy that is released as heat due to 365 the friction between the ceramic piston part and the seal; this thermal power $P_{f ring}$ is 366 included in the model and it is calculated by means of the approach described in the 367 368 Paragraph 2.2.

In order to define the thermal power transferred by the pump cylinder head towards the 369 370 environment, the heat transfer coefficient must be calculated. The numerical approach employed is the same used for the crankcase in the CFD model, based on the Nusselt 371 number correlation of Eq. 21. As said above, the pump cylinder head is cooled by the 372 373 water flow. The internal geometry of the component is really complex, but, as an 374 approximation, it is possible to calculate the hydraulic diameter d_h and to consider the 375 convection phenomenon as referred to a turbulent flow in circular tubes; in other words, 376 the Nusselt number Nuhead int is simulated by means of the Dittus-Boelter equation (as shown by Incropera and DeWitt [18]): 377

378
$$Nu_{head_int} = 0.023 \cdot \operatorname{Re}_{head_int}^{4/5} \cdot \operatorname{Pr}_{water}^{nc}$$
 (23)

Where Re_{head_int} is the Reynolds number of the internal duct of the pump cylinder head, using the hydraulic diameter d_h as characteristic length l (see Appendix B), Pr_{env} is the water Prantl number and nc is a exponent equal to 0.4 for flow heating and 0.3 for flow cooling. Eq. 23 is normally used for small temperature difference and for the range of conditions: $0.6 \le Pr \le 160$, $Re \ge 10^4$, $l/d \ge 10$. Also the ceramic piston part is cooled by water: the contact surface is a circular area that is moved inside the piston chamber. It is very difficult to define the flow condition. On the basis of the Reynolds number Re_{cer_p} ,

it is not possible to recognize a fully developed turbulent flow; thus, a correlation

validated for mixed condition on a flat plate and for $0.6 \le Pr \le 60, 5*10^5 < Re < 10^8$,

388 (Incropera and DeWitt [18]), can be used in order to obtain an average value of Nusselt

number Nu_{cer_p} , and, consequently, an average value of heat transfer coefficient:

390
$$\overline{Nu}_{cer_p} = (0.037 \cdot \operatorname{Re}_{cer_p}^{4/5} - 871) \cdot \operatorname{Pr}_{water}^{1/3}$$
 (24)

In the model, the conduction between two components is automatically calculated based on the material properties and the geometrical characteristic of the contact surface. In addition, it is possible to set a contact thermal resistance for cases where the surface roughness must be considered.

395

396 3.2 Mechanical side model

397 This part of the model focuses on the heat transferred between lubricating fluid and mechanical components by means of convection; the model includes also the 398 conduction between the parts in contact. As mentioned above, each conduction interface 399 requires the geometrical parameters and the involved material properties. The 400 401 dissipation of mechanical power due to friction is considered by means of the approach 402 described in the Paragraph 2.2 in the CFD model; more in details, P_{f_rbe} and P_{f_rse} are addressed to the rod as well as $P_{f_{jb}}$ is referred to the metal piston part and $P_{f_{nb}}$ regards 403 404 the needle bearings.

The lubricating fluid is composed of air and oil. The lumped parameter approach normally does not let the user to model a multiphase fluid; thus, two different virtual volumes (one of air and one of oil) are employed. The sum of the two volume is equal to the internal volume of the crankcase. Each volume can transfer heat with all the components that are in contact with the lubricating fluid, by means of various interfaces of area S_{eff} :

411 $S_{eff} = nd \cdot S_{geo}$ (25)

412 Where S_{geo} is the geometrical area and *nd* is a coefficient of covered area, obtained from 413 the CFD simulation and equal to the surface average of the oil mass fraction (*nd*_{oil}) and 414 the air mass fraction (*nd*_{air}). Thus, each contact interface is divided in two surfaces, one 415 of area S_{eff_oil} referred to the oil and one of area S_{eff_oil} referred to the air.

The thermal power transferred from the crankcase to the environment is described by 416 417 means of the same approach (Eq. 21) used in the CFD model, while the heat transferred between the lubricating fluid (both air and oil) and each crankcase wall is modelled by 418 means of the Eq. 24. Each wall of the crankcase is considered as a flat plat and is 419 420 characterized by different geometry and oil/air distribution; the flow is described by a Reynolds number too low for a fully developed turbulent condition, thus, the Nusselt 421 number correlation (Eq. 24) proposed seems to be a good approach to obtain the related 422 heat transfer coefficient. In fact, air and oil are continually mixed inside the crankcase 423 424 by the moving parts, but the fluid does not reach an average velocity sufficiently high to 425 be in turbulent condition. For the same reason, also the Nusselt number referred to the

426 contact surface between the bearings and the lubricating fluid is calculated with the
427 same approach (Eq. 24). The surface is the area between the bearing external
428 circumference and the shaft external circumference. The heat transferred from the shaft
429 to the lubricating fluid is accounted for by means of an approach validated for rotating
430 cylinder in a cross flow (Incropera and DeWitt [18]):

431
$$\overline{Nu}_{sh_oil} = 0.193 \cdot \operatorname{Re}_{sh_oil}^{0.618} \cdot \operatorname{Pr}_{oil}^{1/3}$$
 (26)

Where *Re_{sh oil}* is the rotational Reynolds number of the oil dragged by that shaft (see 432 433 Appendix B) and *Proil* is the Prandtl number of the oil. This correlation is used for the range of conditions $0.7 \le Pr$, $4*10^3 \le Re \le 4*10^4$ and it can be employed for both oil and 434 air. For the contact surface between the rod and the lubricating fluid, the heat transfer 435 436 coefficient is obtained by the 2D CFD simulation, as well as the one referred the interface between the metal piston part and the lubricating fluid. The 2D CFD model is 437 438 also used, as said above, to calculate the coefficients of covered area for both oil and air, 439 regarding all the considered contact surfaces.

440 4. CFD MODEL RESULTS

The results of the CFD model of the lubricating system in terms of heat transfer coefficient and oil and air distribution are then employed in the lumped and distributed numerical model.

In the CFD model, the rotational speed used is one thousand rpm and the employed time step is 0.1 millisecond; thus, angular time step is smaller than one degree. A breather plug is included in the geometry in order to maintain the atmospheric pressure of the fluid volume inside the crankcase. Afterwards, the initial temperature value is set equal to the ambient temperature, while the initial oil and air distribution is shown in Fig. 3a. The oil mass fraction is equal to the 50% of the volume.

450 On the right side of the picture, a rectangular shape can be noticed that is a fictitious volume separated from the main volume by the piston. This volume is requested by the 451 overset mesh technique in order to correctly describe the piston movement, but it is not 452 referred to the real cylinder. In fact, in the real machine, on this side of the piston there is 453 water, that is to say, the pumped fluid. This fictitious volume has the same initial pressure, 454 temperature and air-oil distribution of the main volume but it is physically separated from 455 456 the crankcase volume, thus, the air and oil in this region do not influence the fluid dynamic behaviour of the crankcase volume. In order to highlight this point, an open 457 boundary is included in the simulation at the left side of the fictitious volume: after few 458 crankshaft revolutions the volume is almost full of air at the environment conditions. 459

- 460 While the rod and the piston position at the BDC (bottom dead centre) are shown in the
- Fig. 3a and in the Fig. 3d, Fig. 3c depicts the machine in the TDC configuration (top dead centre) and an arbitrary angular position is chosen in Fig. 3b.



464 Figure 3- Volume fraction of oil in the crankcase, referred to a) initial condition; b) after
465 3.41 s c) after 6.03 s; d) after 210 s.

Fig. 3b displays the air-oil volume fraction after 3.4 seconds; the oil and air are mixed
but a separation between the fluids can be still identified. A similar phenomenon can be
noticed also in Fig. 3c, i.e. simulation time equal to 6 seconds which corresponds to 100
revolutions. The last picture, Fig. 3d, shows the oil volume fraction distribution when
the system has reached a steady state condition, i.e. simulation time 210 s; the air and
the oil are completely mixed.

472 In all the presented pictures, there is a no recirculating zone where oil is almost fixed, in 473 the right-lower side, under the cylinder. A good oil recirculation is one of the most important goal for lubricating system design, so, if this behaviour will be confirmed also 474 475 by the three-dimensional simulations, the crankcase geometry should be modified in 476 order to avoid it. During the transient period, a small amount of oil can escape through the breather plug, as confirmed by experimental test, but after a few seconds these oil 477 losses are no more observable. The oil amount in the fictitious volume, starting from the 478 initial value, in a few revolutions decreased rapidly. Only a thin oil layer is still 479 480 observable in the steady-state phase. As said above, this fictitious volume has no relation with the real cylinder, because the pumped fluid is water. 481

The results obtained from this 2D CFD model are compared to experimentalmeasurements and a good agreement is obtained from a qualitatively point of view.

In fact, it is not possible to strictly compare the numerical data achieved from the 2D

485 CFD model to the experimental data: converting from 3D to 2D, the crankcase walls 486 parallel to the model plane are neglected. In other words, the crankcase area able to 487 transfer heat form the fluid inside to the environment is different from the one of the 488 real geometry. The thermal power introduced in the model due to friction is reduced to 489 account for this consideration. In fact, the time duration of the numerical thermal 490 transient is minor that the real one, but the numerical mean value of the oil temperature 491 in steady-state condition is quite close to the experimental value.

492 Thus, the 2D model can not be used to predict exactly the punctual temperature 493 evolution of the lubricating system but the qualitatively good agreement between numerical results and measurements lets the user to usefully employ the model to 494 495 estimate the heat transfer coefficient and the air-oil distribution of each surface. These data are introduced in the lumped and distributed parameter model to obtain a predictive 496 497 model of the pump. This approach, based on the use of a 2D CFD model and a lumped parameter model, has a computational effort minor than a complete 3D CFD model; 498 thus, the combined approach demonstrated to be a reliable tool to achieve the numerical 499 results with good accuracy. 500

501 5. LUMPED PARAMETER MODEL RESULTS

502 The lumped and distributed numerical model of the whole pump is tailored in two steps. 503 Firstly, the pumping side is accounted in the analysis and the measurements are 504 compared with the numerical results in terms of load pressure and flow rate. More in 505 details, the discharge coefficient and the friction parameter of each valve are introduced 506 and regulated in order to obtain a good agreement between numerical and experimental 507 data. Particular care is devoted to the angular phasing of the three pistons: in Fig. 4a the volume evolution of the three piston chambers are shown. Figs. 4b and 4c depicts the 508 509 instantaneous and the mean values of load pressure and flow rate. The curves are very close to the measurements; thus, the model is able to describe the fluid dynamics 510 behaviour of the pumping side and it is possible to calculate the volumetric efficiency, 511 that is equal to the experimental value and higher than 90%. 512



Figs. 4. Pumping side analysis: a) Phasing of piston chamber volume; b) load flow rate;
c) load pressure

516

517 Once the pumping side is tailored and validated, the mechanical side of the pump model 518 can be completed. In particular, the heat transfer coefficient and the air-oil distribution 519 of each surface of the internal geometry of the crankcase are achieve from the 2D CFD 520 model and they are employed in the lumped parameter model in order to enhance the 521 accuracy.

522 The validation of the whole pump model is achieved comparing the numerical results

523 with the measurements carried out by means of thermocouples type K, placed in

524 different positions of the crankcase, on the external walls and in the internal oil volume.

525 The experimental oil temperature curve has been obtained as a mean of the

526 measurements carried out and it has been used to tailor the numerical model. Water and

527 air temperature are monitored, and the ambient temperature is recorded too. Both

528 transient and steady-state operations are considered.

- 529 Afterwards, a thermographic camera is adopted in order to obtain a complete
- temperature distribution of the external walls of the machine. The device used is a
- 531 Optris PI 600 thermocamera characterized by a spectral range of $7.5-1.3 \,\mu$ m, a
- temperature range from -20°C to 900°C and an optical resolution of 160x120 pixel; the
- 533 frequency is 120 Hz.

534 Fig. 5 shows the thermal images in different positions: the temperature reported at the top of each image (e.g., 34.6°C in Fig. 4a) is relative to the average value of all the pixel 535 that compose the T1 probe box. In the case shown in Figs. 5a and 5b, the camera is 536 positioned in front of the crankcase cover, the opposite part of the pump cylinder head 537 side. By monitoring the heating transient, it is possible to observe how the hottest parts, 538 539 the needle bearings and the shaft, progressively transfer thermal power from the middle plane to the upper and the lower side, until the wall is almost at the same temperature 540 (in steady-state condition, see Fig. 5b). This consideration about the uniformity of the 541 temperature confirms that the lumped parameter approach can be used to describe the 542 543 system with a good accuracy: indeed, if the temperature distribution on each component is uniform, the error due to the description of each part as an numerical element 544 characterized by a single temperature value, is very limited. Fig. 5c shows the whole 545 546 crankcase from a different view in the steady state condition: in particular, the cooling 547 effect of the pump cylinder head (where the water flows) can be observed on the left side. The effect is restricted to a narrow zone but it can not be neglected: for this reason, 548 549 the lumped and distributed parameter model is referred to the whole pump and it account for both thermal power dissipation between the crankcase and the environment 550 551 and between the crankcase and the pump cylinder head.



Figs. 5. Thermographic analysis: a) crankcase cover after a few seconds; b) crankcase
cover in steady-state condition; c) whole pump in steady-state condition

555 As mentioned above, the experimental campaign is carried out to tailor and validate the numerical model of the pump. Fig. 6 shows the comparison between the measured oil 556 557 temperature and the numerical one, as well as the numerical air temperature. More in details, the model can not consider a multiphase fluid; thus, two separated fluids are 558 559 included and so, two numerical temperatures are obtained. Each phase is able to 560 exchange thermal power with the surfaces which are in contact, on the basis of the air/oil distribution obtained from the 2D CFD model. Two volumes are used, one for the 561 air and the other one for the oil. Each volume is equal to the 50% of the internal volume 562 of the crankcase. Nevertheless, in Fig. 6 it is possible to observe that le two numerical 563 temperatures are perfectly overlapped, as a consequence of the model reliability. In fact, 564 even if air and oil have no direct interfaces in the model, they are in contact with the 565 same surfaces and it seems physically correct that the two curves are equal. In 566 particular, due to the strongly different thermo physical properties of the two fluids, the 567 thermal equilibrium is mainly influenced by the oil. Thus, the comparison is based on 568 the oil temperature: the agreement is excellent for the steady-state condition (the error is 569 570 around the 2%) but the numerical curve increases faster than the experimental one in the transient phase. This is due, on the one hand, to the 3D effect of the heat transfer 571 572 phenomenon, that the lumped model can not consider, and on the other hand, to the 573 employed data logger. In fact, in order to remove the noise from the signal, the data logger automatically applies a moving average to the raw data. This increases the 574 575 quality of the signal, but it introduces a delay. Both the 3D effect and the signal 576 treatment influence are more significant during the transient phase than the steady-state phase. In order to enhance the lifetime of the pump, it is very important to avoid too 577 high temperature when the machine operates continuously; thus, it is possible to accept 578 579 a quite poor agreement between numerical and experimental data in the transient phase because, in the steady state condition, the agreement is very good. The overheating risk 580 regards only the mechanical side of the pump. In fact, observing Figs. 4 and 6, the 581 hydraulic transient of the pumping side is strongly minor than the thermal transient of 582 the mechanical side: after a few seconds, the load flow rate and pressure are in steady 583 state condition, while the oil temperature of the lubricating system requires more than 584 4000 s to be stable. Thus, the lubricating system temperature does not influence directly 585 586 the operating point of the pump: the pumping side temperature is fixed by the water 587 flow.





Figure 6. Comparison between measured and calculated oil temperature

590 6. CONCLUSIONS

591 This paper has presented a numerical approach for the prediction of the thermo fluid 592 dynamics behaviour of a piston water pump. Particular care has been devoted to the 593 lubricating system model and to the heat transferred from the internal crankcase to the 594 environment. A 2D CFD model of the system has been constructed, accounting for the 595 thermal power released by friction, the mixing of the two fluids (oil and air) in the 596 crankcase volume, the moving parts (rod and piston) described by means of the overset 597 mesh technique.

598 The outputs of the 2D CFD model, in terms of heat transfer coefficient and air/oil

distribution of each surfaces, have been passed to a lumped and distributed parameter 599 model of the whole pump, properly designed to describe both the operating point of the 600 pumping side and the thermal condition of the mechanical side. Conduction and 601 convection phenomena between the pump cylinder head and the crankcase, and between 602 603 the crankcase and the environment have been included. The model has been tailored and 604 validated using experimental data carried out by means of two different measurements 605 technique: thermocouples analysis and thermography. The employed thermocamera has 606 highlighted that the temperature of each component has a uniform distribution, 607 confirming the most important hypothesis for the use of the lumped parameter

608 approach.

609 The numerical results, in terms of oil temperature, have been compared with the

acquired data and a good agreement has been found, especially in the steady-state

611 condition. Simulation and measurements have confirmed that the water flow has a

612 cooling effect on the pumping side and the temperature in this zone is fixed by the

613 water. In fact, the operating point of the pump is not influenced by the thermal transient

of the lubricating system. On the other hand, even if the crankcase is partially cooled by

the conduction between the component itself and the pump cylinder head, this

616 phenomenon is not sufficient to maintain the mechanical side temperature under the 617 overheating limit without adopting a lubricating system.

618 Combing the 2D CFD lubricating system model and the lumped parameter model of the 619 whole pump, the user can achieve all the information needed to properly design the 620 machine and in particular the lubricating system. The approach is able to ensure a good 621 accuracy in an acceptable time: both the operating point and the thermo fluid dynamics 622 behaviour of the pump are described and the computational effort is minor than the one 623 referred to a complete 3D CFD model.

624

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629

630

632 LIST OF NOTATIONS

а	Thermal diffusivity	m ² /s
Ar	Cross section area	m^2
b	Volumetric thermal expansion coefficient	K-1
\overline{c}	Mean radial clearance	m
С	Coefficient	-
C_0	First coefficient of <i>k</i> _{oil} correlation	0.053W/(m*K)
C_1	Second coefficient of <i>k</i> _{oil} correlation	0.026W/(m*K)
C_2	First coefficient of c_{poil} correlation	1.17*10 ⁶ J/(m ³ *K)
<i>C</i> ₃	Second coefficient of <i>c</i> _{poil} correlation	0.39*10 ⁶ J/(m ³ *K)
c_p	Specific heat	J/(kg*K)
d	Diameter	m
F	Force	Ν
g	Gravitational constant	m/s ²
Gr	Grashof number	-
h	Heat transfer coefficient	W/(m ² *K)
k	Thermal conductivity	W/(m*K)
l	Length	m
М	Torque	N*m
n	Number of	-
nc	Convection exponent	-
nd	Coefficient of covered area	-
Nu	Nusselt number	-
р	Pressure	Pa
Р	Power	W
Per	Perimeter	m
Pr	Prandtl number	-
Q	Flow rate	m ³ /s
r	Radius	m
R	Thermal resistance between the internal and the external case wall	K*m ² /W
Ra	Rayleigh number	-

Reynolds number	-
Perfect gas law constant	J/(mol*K)
Wall thickness	m
Surface area	m^2
Time	s
Temperature	K
Velocity	m/s
Volume	m ³
Thermal power transferred through the wall	W
Thermal power transferred between the wall and the environment	W
Position referred to the <i>Y</i> axis	m
Velocity referred to the <i>Y</i> axis	m/s
Position referred to the <i>X</i> axis	m
Velocity referred to the X axis	m/s
Angle between crank and piston axis	rad
Angle between rod and piston axis	rad
Rod rotational speed	rad/s
Efficiency	-
Ratio between crank and rod length	-
Density	Kg/m ³
Dynamic viscosity	Pa*s
Crankshaft rotational speed	rad/s
	Reynolds numberPerfect gas law constantWall thicknessSurface areaTimeTemperatureVelocityVolumeThermal power transferred through the wallThermal power transferred between the wall and the environmentPosition referred to the Y axisVelocity referred to the X axisAngle between crank and piston axisAngle between rod and piston axisRod rotational speedEfficiencyRatio between crank and rod lengthDensityCrankshaft rotational speed

633 Subscripts

Point A - connecting rod small end
Air
Point B - connecting rod big end
Crank
Ceramic
Effective
Environment
External
Geometrical
Friction

h	hydraulic
head	Pump cylinder head
hm	Hydro-mechanical
hyd	Hydraulic
int	Internal
jb	Journal box
J	Point J – generic rod point
max	Maximum value
mech	Mechanical
nb	Needle bearing
oil	Oil
р	Piston
r	Connecting rod
ref	Reference value
ring	Seal placed in the cylinder wall
rbe	Rod big end
rse	Rod small end
SUC	Suction
sh	Shaft
tot	Total
vol	Volumetric
wall	Crankcase wall
water	Water

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695

696 APPENDIX A

$$\alpha = \omega \cdot t \tag{A.1}$$

$$\sin \beta = (r_c / l_r) \cdot \sin \alpha = \lambda \cdot \sin \alpha \tag{A.2}$$

$$\sin^2 \beta = \lambda^2 \cdot \sin^2 \alpha \tag{A.3}$$

$$\sin^2\beta + \cos^2\beta = \lambda^2 \cdot \sin^2\alpha + \cos^2\beta \tag{A.4}$$

$$\cos\beta = \sqrt{1 - \lambda^2 \cdot \sin^2\alpha} \tag{A.5}$$

$$x = (r_c + l_r) - r_c \cdot \cos\alpha - l_r \cdot \cos\beta = r_c \left[(1 + 1/\lambda) - \cos\alpha - (1/\lambda) \cdot \sqrt{1 - \lambda^2 \cdot \sin^2\alpha} \right]$$
(A.6)

$$\dot{x} = \frac{dx}{dt} = \frac{dx}{d\alpha} \cdot \frac{d\alpha}{dt} = r_c \cdot \omega \cdot \left[\sin\alpha + \frac{\lambda \cdot \sin\alpha \cdot \cos\alpha}{\sqrt{1 - \lambda^2 \cdot \sin^2\alpha}}\right] = r_c \cdot \omega \cdot \left[\sin\alpha + \frac{\lambda \cdot \sin 2\alpha}{2 \cdot \sqrt{1 - \lambda^2 \cdot \sin^2\alpha}}\right]$$
(7)

$$\beta = \arcsin(\lambda \cdot \sin \alpha) \tag{A.7}$$

$$\frac{d\beta}{dt} = \frac{1}{\sqrt{1 - \lambda^2 \cdot \sin^2 \alpha}} \cdot \lambda \cdot \cos \alpha = \lambda \cdot \frac{\cos \alpha}{\cos \beta}$$
(A.8)

$$\dot{\beta} = \frac{d\beta}{dt} = \frac{d\beta}{d\alpha} \cdot \frac{d\alpha}{dt} = \lambda \cdot \omega \cdot \frac{\cos \alpha}{\cos \beta} = \lambda \cdot \omega \cdot \frac{\cos \alpha}{\sqrt{1 - \lambda^2 \cdot \sin^2 \alpha}}$$
(6)

697

698 APPENDIX B

699
$$\operatorname{Re}_{wall_ext} = \left(v_{env} \cdot \rho_{env} \cdot l_{wall_ext} \right) / \mu_{env}$$
 (B.1)

700
$$\operatorname{Pr}_{env} = \mu_{env} / (\rho_{env} \cdot a_{env})$$
(B.2)

701
$$Gr_{wall_ext} = g \cdot b_{env} \cdot (T_{wall_ext} - T_{env}) \cdot l_{wall_ext} \cdot \rho_{env} / \mu_{env}$$
(B.3)

702
$$Ra_{wall_ext} = \Pr_{env} \cdot Gr_{wall_ext}$$
 (B.4)

$$703 \qquad d_h = 4 \cdot Ar / Per \tag{B.5}$$

704
$$\operatorname{Re}_{sh_oil} = (\omega \cdot \rho_{oil} \cdot d_{sh}) / \mu_{oil}$$
 (B.6)