# Search for the decay $\boldsymbol{K}_{S} \rightarrow \pi^{0} \gamma \gamma$ 

## NA48 Collaboration

A. Lai, D. Marras

Dipartimento di Fisica dell'Università e Sezione dell'INFN di Cagliari, I-09100 Cagliari, Italy.
R. Batley, A. Bevan, R.S. Dosanjh, T.J. Gershon, G.E. Kalmus ${ }^{1)}$, D.J. Munday, E. Olaiya, M.A. Parker, T. White, S.A. Wotton Cavendish Laboratory, University of Cambridge, Cambridge, CB3 0HE, U.K2).
G. Barr, G. Bocquet, A. Ceccucci, T. Cuhadar-Dönszelmann, D. Cundy, N. Doble, V. Falaleev, L. Gatignon, A. Gonidec, B. Gorini, G. Govi, P. Grafström, W. Kubischta, A. Lacourt, M. Lenti ${ }^{3}$, A. Norton, S. Palestini, B. Panzer-Steindel, G. Tatishvili ${ }^{4}$, H. Taureg, M. Velasco, H. Wahl CERN, CH-1211 Geneva 23, Switzerland.
C. Cheshkov, P. Hristov ${ }^{5}$, V. Kekelidze, D. Madigojine, N. Molokanova, Yu. Potrebenikov, A. Tkatchev, A. Zinchenko Joint Institute for Nuclear Research, Dubna, Russian Federation.
I. Knowles, C. Lazzeroni, V. Martin, R. Sacco, A. Walker

Department of Physics and Astronomy, University of Edinburgh, JCMB King's Buildings, Mayfield Road, Edinburgh, EH9 3JZ, U.K.
M. Contalbrigo, P. Dalpiaz, J. Duclos, P.L. Frabetti, A. Gianoli, M. Martini, L. Masetti, F. Petrucci, M. Savrié

Dipartimento di Fisica dell'Università e Sezione dell'INFN di Ferrara, I-44100 Ferrara, Italy.
A. Bizzeti ${ }^{6}$, M. Calvetti, G. Collazuol, G. Graziani, E. Iacopini

Dipartimento di Fisica dell'Università e Sezione dell'INFN di Firenze, I-50125 Firenze, Italy.
H.G. Becker, M. Eppard, H. Fox, K. Holtz, A. Kalter, K. Kleinknecht, U. Koch,
L. Köpke, P. Lopes da Silva, P. Marouelli, I. Pellmann, A. Peters, B. Renk, S.A. Schmidt, V. Schönharting, Y. Schué, R. Wanke, A. Winhart, M. Wittgen Institut für Physik, Universität Mainz, D-55099 Mainz, Germany ${ }^{7}$ ).

[^0]J.C Chollet, L. Fayard, L. Iconomidou-Fayard, J. Ocariz, G. Unal, I. Wingerter Laboratoire de l'Accélératur Linéaire, IN2P3-CNRS, Université de Paris-Sud, 91898 Orsay, France ${ }^{8)}$.
G. Anzivino, P. Cenci, E. Imbergamo, P. Lubrano, A. Mestvirishvili, A. Nappi, M. Pepe, M. Piccini

Dipartimento di Fisica dell'Università e Sezione dell'INFN di Perugia, I-06100 Perugia, Italy.
R. Carosi, R. Casali, C. Cerri, M. Cirilli, F. Costantini, R. Fantechi, S. Giudici, I. Mannelli, G. Pierazzini, M. Sozzi

Dipartimento di Fisica dell'Università, Scuola Normale Superiore e Sezione dell'INFN di Pisa, I-56100 Pisa, Italy.
J.B. Cheze, J. Cogan, M. De Beer, P. Debu, A. Formica, R. Granier de Cassagnac, E. Mazzucato, B. Peyaud, R. Turlay, B. Vallage DSM/DAPNIA - CEA Saclay, F-91191 Gif-sur-Yvette Cedex, France.
M. Holder, A. Maier, M. Ziolkowski

Fachbereich Physik, Universität Siegen, D-57068 Siegen, Germany ${ }^{9}$.
R. Arcidiacono, C. Biino, N. Cartiglia, R. Guida, F. Marchetto, E. Menichetti, N. Pastrone

Dipartimento di Fisica Sperimentale dell'Università e Sezione dell'INFN di Torino, I-10125 Torino, Italy.
J. Nassalski, E. Rondio, M. Szleper, W. Wislicki, S. Wronka Soltan Institute for Nuclear Studies, Laboratory for High Energy Physics, PL-00-681 Warsaw, Poland ${ }^{10)}$.
H. Dibon, G. Fischer, M. Jeitler, M. Markytan, I. Mikulec, G. Neuhofer, M. Pernicka, A. Taurok, L. Widhalm

Österreichische Akademie der Wissenschaften, Institut für Hochenergiephysik, A-1050 Wien, Austria.
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## Abstract

A search for the decay $K_{S} \rightarrow \pi^{0} \gamma \gamma$ has been made using the NA48 detector at the CERN SPS. Using data collected in 1999 during a 40-hour run with a high-intensity $K_{S}$ beam, an upper limit for the branching ratio $B R\left(K_{S} \rightarrow \pi^{0} \gamma \gamma, z \geq 0.2\right)<$ $3.3 \times 10^{-7}$ has been obtained at $90 \%$ confidence level, where $z=m_{\gamma \gamma}^{2} / m_{K_{0}}^{2}$.

## 1 Introduction

The study of the decays $K_{S, L} \rightarrow \pi^{0} \gamma \gamma$ is useful to test the predictions of the Chiral Perturbation Theory $(\chi P T)$ on branching ratios and $q^{2}$-spectra [1]. At present the branching ratio for the decay $K_{L} \rightarrow \pi^{0} \gamma \gamma$ has been measured precisely [2], while the corresponding $K_{S}$ decay has not yet been observed. $\chi P T$ predicts a branching ratio for $K_{S} \rightarrow \pi^{0} \gamma \gamma$ of $3.8 \times 10^{-8}$ with the cut-off $z=m_{\gamma \gamma}^{2} / m_{K_{0}}^{2} \geq 0.2$, to avoid the region with the pion pole which dominates the total rate [1]. The amplitude can be calculated precisely as it is non-vanishing in lowest order Chiral Perturbation Theory and expected to be quite insensitive to higher order corrections. With sufficient statistics, the chiral structure of weak vertices could be tested experimentally in the high- $q^{2}$ region from a comparison with the predicted $q^{2}$-spectrum.

## 2 Experimental set-up and data taking

The NA48 detector, originally designed to measure the direct CP-violation parameter $\epsilon^{\prime} / \epsilon$ in neutral kaon decays with simultaneous $K_{L}$ and $K_{S}$ beams, was used to collect data for studies on rare $K_{S}$ decays during a test run in 1999 with a high-intensity $K_{S}$ beam. This beam had an intensity about 200 times higher than the one used in the $\epsilon^{\prime} / \epsilon$ runs. The present analysis is based on data collected during this 40-hour high-intensity $K_{S}$ run. Neutral kaons were produced by a primary beam of $450 \mathrm{GeV} / c$ protons, extracted from the SPS accelerator during a 2.4 s spill every 14.4 s and impinging with an angle in the vertical plane of 4.2 mrad on a 2 mm diameter, 400 mm long beryllium target, at an intensity of $\sim 6 \times 10^{9}$ protons per pulse. The target was followed by a sweeping magnet and a 0.36 cm diameter collimator to define a narrow beam of neutral kaons and hyperons. The beginning of the fiducial volume was set 500 cm downstream of the centre of the target, 1 m before the end of the collimator. The fiducial volume was contained in an 89 $m$ long, evacuated steel cylinder and followed by the main NA48 detector. The neutral particles of the beam were contained in a 156 mm diameter carbon-fibre pipe linked to the evacuated cylinder and passing through the detector, in order to avoid interactions of neutrons and photons from the beam. A detailed description of the detector and beam lines can be found elsewhere [3].

In the present analysis the following sub-detectors were used: a magnetic spectrometer composed of four drift chambers, two upstream and two downstream of a dipole magnet, for vetoing charged particles; seven anti-counter rings (AKL) of iron and plastic scintillator, for vetoing photons outside the acceptance of the main detector; a quasihomogeneous electromagnetic liquid-krypton calorimeter (LKr), to measure energy, position and time of electromagnetic showers generated by photons; a sampling hadron calorimeter (HAC) composed of 96 steel and scintillator planes. The electromagnetic calorimeter is composed of 13212 readout tower cells of $2 \times 2 \mathrm{~cm}^{2}$ cross section and $27 X_{0}$ depth each. The energy resolution is [4]

$$
\begin{equation*}
\frac{\sigma(E)}{E} \simeq \frac{0.09}{E} \oplus \frac{0.032}{\sqrt{E}} \oplus 0.0042 \tag{1}
\end{equation*}
$$

with E in GeV . The position and time resolutions for a single photon are better than 1 mm and 500 ps , respectively, for energies greater than 25 GeV . The overall energy scale was determined by a fit of the position of an anti-counter (AKS) used during $\epsilon^{\prime} / \epsilon$ runs.

Events satisfying the trigger conditions for $\gamma \gamma$ or $3 \pi^{0}$ events were selected, since no dedicated trigger for $\pi^{0} \gamma \gamma$ (and $2 \pi^{0}$ ) decays was set up during the special high-intensity $K_{S}$ run. The trigger decisions were based on quantities reconstructed from orthogonal

|  | Cond. $\gamma \gamma$ | $D_{\gamma \gamma}$ | Cond. $3 \pi^{0}$ | $D_{3 \pi^{0}}$ | $N_{2 \pi^{0}}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| a | zv $<12 \mathrm{~m} ;$ no peak cut | 3 | npx $>4$ or npy $>4$ or $\mathrm{npx}=\mathrm{npy}=4$ | 1 | $\sim 5 \times 10^{4}$ |
| b | zv $<9 \mathrm{~m} ;$ no peak cut | 3 | npx $>4$ or npy $>4$ or npx $=$ npy $=4$ | 1 | $\sim 3.4 \times 10^{5}$ |
| c | zv $<9 \mathrm{~m} ;$ no peak cut | 3 | npx $>4$ or npy $>4$ | 1 | $\sim 3.4 \times 10^{5}$ |
| d | zv $<9 \mathrm{~m} ;$ no peak cut | 2 | npx $>4$ or npy $>4$ | 1 | $\sim 1.5 \times 10^{6}$ |
| e | zv $<9 \mathrm{~m} ;$ npx,npy $=1,2$ | 1 | npx $>4$ or npy $>4$ | 1 | $\sim 1.1 \times 10^{6}$ |

Table 1: Conditions and downscaling factors $D$ for $\gamma \gamma$ and $3 \pi^{0}$ triggers, for different parts of the run. $\mathrm{zv}=z_{v e r t e x}^{\text {trig }}-6 \mathrm{~m}$ is the position of the decay vertex starting from the beginning of the decay region, npx and npy the number of energy peaks in $x$ and $y$ projection respectively, in a time window of 20 ns . In the rightmost column the number of $2 \pi^{0}$ events after all selection cuts satisfying $\gamma \gamma$ or $3 \pi^{0}$ trigger conditions is given.
projections of the energy deposit in the electromagnetic calorimeter [5]. The trigger for both $\gamma \gamma$ and $3 \pi^{0}$ decays required:

1. the total deposited energy $E_{t o t}=E_{L K r}+E_{H A D}$ being larger than 50 GeV ;
2. the centre of gravity of the event, computed from the first moments $M_{1, x}$ and $M_{1, y}$ of the energy in each projection,

$$
\begin{equation*}
\text { c.o.g }{ }^{\text {trig }}=\frac{\sqrt{M_{1, x}^{2}+M_{1, y}^{2}}}{E_{L K r}}, \tag{2}
\end{equation*}
$$

being less than 15 cm from the beam axis;
3. the decay vertex of the $K^{0}$, computed from the second moments $M_{2, x}$ and $M_{2, y}$,

$$
\begin{equation*}
z_{v e r t e x}^{\text {trig }}=z_{L K r}-\frac{\sqrt{E_{L K r}\left(M_{2, x}+M_{2, y}\right)-\left(M_{1, x}^{2}+M_{1, y}^{2}\right)}}{m_{K}}, \tag{3}
\end{equation*}
$$

being less than 15 m downstream from the end of the collimator. This corresponds to about $2.5 K_{S}$ lifetimes, since the $K_{S}$ have a mean energy of 110 GeV . In equation $3, z_{L K r}$ is the $z$ coordinate of the electromagnetic calorimeter with respect to the target and $m_{K}$ is the kaon mass.
The $3 \pi^{0}$ trigger required also at least 4 energy peaks in each projection. The cuts on the vertex for the $\gamma \gamma$ trigger and on the maximum number of energy peaks for the $3 \pi^{0}$ trigger were varied during the run, while the downscaling factors were adjusted according to the obtained rate. The different trigger conditions and downscaling factors are summarised in Table 1.

The trigger efficiency for $K_{S} \rightarrow 2 \pi^{0}$ decays was computed using a minimum bias trigger which did not involve the electromagnetic calorimeter: for the first part of the run (conditions a-d in Table 1) it was ( $98.52 \pm 0.06$ )\%, while it decreased to $(22.0 \pm 0.2) \%$ for condition e. About one third of the statistics used for this analysis was collected under this last condition. The trigger efficiency for $K_{S} \rightarrow \pi^{0} \gamma \gamma$ events was assumed to be the same as for $2 \pi^{0}$ events. Possible differences were studied from simulation and considered as systematic uncertainties.

## 3 Event selection

To select $K_{S} \rightarrow \pi^{0} \gamma \gamma$ candidates, events with at least four electromagnetic clusters were considered. Each cluster was required to satisfy the following conditions:

1. the energy had to be greater than 3 GeV and less than 100 GeV ;
2. each cluster had to be well inside the calorimeter acceptance, more than 15 cm and less than 113 cm from the axis of the beam pipe;
3. the distance from any dead cell of the calorimeter had to be greater than 2 cm ;
4. the distance from any other cluster in the event with an energy greater than 1.5 GeV had to be greater than 10 cm .
For each event, all combinations of four clusters passing the pre-selection described above were considered. For each combination, the following selection criteria were applied:
5. the time of each cluster $\left(t_{c l}\right)$ had to be within $\pm 3 \mathrm{~ns}$ of the event time $\left(t_{a v 4}\right)$ computed as the average of $t_{c l}$ weighted over the energy;
6. no other cluster (not belonging to the combination considered) with an energy greater than 1.5 GeV had to be found within $\pm 5 \mathrm{~ns}$ of the event time, to reduce the effect of accidental background;
7. the sum of the four cluster energies had to be greater than 70 GeV and less than 170 GeV ;
8. in order to distinguish $\pi^{0} \gamma \gamma$ decays from $2 \pi^{0}$ decays, a $\chi^{2}$ variable was defined [6]:

$$
\begin{equation*}
\chi_{2 \pi^{0}}^{2}=\left[\frac{\left(m_{\gamma \gamma}+m_{\gamma \gamma}^{\prime}\right) / 2-m_{\pi^{0}}}{\sigma_{+}}\right]^{2}+\left[\frac{\left(m_{\gamma \gamma}-m_{\gamma \gamma}^{\prime}\right) / 2}{\sigma_{-}}\right]^{2} \tag{4}
\end{equation*}
$$

where $m_{\gamma \gamma}$ and $m_{\gamma \gamma}^{\prime}$ are the invariant masses of the two $\gamma \gamma$ pairs and $\sigma_{ \pm}$the resolutions of $\left(m_{\gamma \gamma} \pm m_{\gamma \gamma}^{\prime}\right) / 2$ measured from the data. For each combination of four clusters the $\gamma \gamma$ pairs giving the lowest $\chi^{2}$ were considered and, if more than one combination of four clusters satisfied the first three requirements, the one with the lowest $\chi^{2}$ was selected.
Further requirements were then applied to each event:

1. to define a good event, cuts in the centre of gravity and decay vertex position of the kaon were used. The centre of gravity

$$
\begin{equation*}
\text { c.o.g. }=\frac{\sqrt{\left(\sum_{i} E_{i} x_{i}\right)^{2}+\left(\sum_{i} E_{i} y_{i}\right)^{2}}}{\sum_{i} E_{i}} \tag{5}
\end{equation*}
$$

with $E_{i}, x_{i}, y_{i}$ respectively the energy, x and y coordinates in the LKr for the $i$-th cluster, had to be less than 7 cm ;
2. the decay vertex

$$
\begin{equation*}
z_{v e r t e x}=z_{L K r}-\frac{1}{m_{K^{0}}} \sqrt{\sum_{i, j<i} E_{i} E_{j} \cdot\left[\left(x_{i}-x_{j}\right)^{2}+\left(y_{i}-y_{j}\right)^{2}\right]}, \tag{6}
\end{equation*}
$$

was required to be within the first 9 m of the decay volume, in order to reject background from $K_{L} \rightarrow 3 \pi^{0}$ events with missing or overlapped photons;
3. events with signals in the drift chambers within $\pm 10 \mathrm{~ns}$ of the event time or with overflows in chamber 1,2 or 4 within $\pm 250$ ns were rejected. The overflow condition is generated in the drift chamber readout whenever more than seven hits in a plane are detected within 100 ns , in order to avoid recording events with high hit multiplicity;
4. in order to reject events with overlapping showers, an energy-dependent clusterwidth cut was applied, using a parametrisation taken from $K_{S} \rightarrow 2 \pi^{0}$ decays;
5. events with signals in any of the AKL rings within $\pm 3 \mathrm{~ns}$ of the event time were rejected;
6. if the energy deposited in the hadron calorimeter was greater than 3 GeV , events were rejected if any HAC signal was found in a time window of $\pm 15 \mathrm{~ns}$ around the event time.

## $4 \quad$ Background rejection

Background to $K_{S} \rightarrow \pi^{0} \gamma \gamma$ may come from misreconstructed $K_{S} \rightarrow 2 \pi^{0}$ with four clusters in the acceptance; from $K_{S} \rightarrow 2 \pi^{0}$ with three clusters in the acceptance and one random cluster accidentally in time; from $K_{S} \rightarrow \pi^{0} \pi_{D}^{0}$ with one lost particle and one misidentified charged particle; from $K_{L} \rightarrow 3 \pi^{0}$ with two lost or overlapped photons; and from $K_{L} \rightarrow \pi^{0} \gamma \gamma$.

### 4.1 Background from misreconstructed $K_{S} \rightarrow 2 \pi^{0}$

To define a good $\pi^{0} \gamma \gamma$ event, the $\gamma \gamma$ pair with invariant mass closest to the nominal $\pi^{0}$ mass was required to be within $\pm 3 \mathrm{MeV} / c^{2}$ of the nominal $\pi^{0}$ mass, corresponding to about 3 standard deviations of the resolution. $K_{S} \rightarrow 2 \pi^{0}$ events with misreconstructed cluster energy due to non-Gaussian tails in the energy resolution were simulated and found to be concentrated in a region with $\chi_{2 \pi^{0}}^{2}$ below 300 . Therefore a $\chi_{2 \pi^{0}}^{2}$ greater than 300 was required for the $\pi^{0} \gamma \gamma$ candidates. In order to compare data and simulation a control region with $50<\chi_{2 \pi^{0}}^{2}<300$ was defined and the distribution in $\chi_{2 \pi^{0}}^{2}$ is shown in Fig. 1 left. The cut on $\chi_{2 \pi^{0}}^{2}$ discards about $8 \%$ of signal events (Fig. 1 right). The remaining $\gamma \gamma$ pair had to satisfy the requirement $z=m_{\gamma \gamma}^{2} / m_{K_{0}}^{2} \geq 0.2$, in order to reject background from $2 \pi^{0}$ events and to be able to compare the result with the prediction made by $\chi P T$, which is given with the cut-off $z>0.2$. After all cuts, $2 K_{S} \rightarrow \pi^{0} \gamma \gamma$ candidates were selected.

From Monte Carlo simulation the background from $K_{S} \rightarrow 2 \pi^{0}$ decays with four clusters in the acceptance is expected to be less than 0.5 events at $90 \%$ C.L., which corresponds to a rejection factor of at least $4 \times 10^{7}$.

### 4.2 Background from $K_{S} \rightarrow 2 \pi^{0}$ with three clusters in the acceptance and one random cluster in time

Using simulated $K_{S} \rightarrow 2 \pi^{0}$ events and events in the data selected by a random trigger, the background from $K_{S} \rightarrow 2 \pi^{0}$ decays with three clusters in the acceptance and one random cluster accidentally in time was estimated to be $3.0 \pm 0.1_{\text {stat }}$ events. Random events were assumed to have a flat distribution in time with respect to the average time of the 3 clusters of the $2 \pi^{0}$ event $\left(t_{a v 3}\right)$ and were overlayed to the simulated $K_{S} \rightarrow 2 \pi^{0}$ with three clusters in the acceptance to reconstruct a $K_{S} \rightarrow \pi^{0} \gamma \gamma$ candidate. One of the 2 selected $K_{S} \rightarrow \pi^{0} \gamma \gamma$ candidates in the data contains one cluster for which the time is compatible with the distribution of the random cluster in background simulation. For the other $K_{S} \rightarrow \pi^{0} \gamma \gamma$ candidate, the farthest in-time cluster from the event time has the same probability to be a random cluster or to be part of an event with four photons in the acceptance of the calorimeter (Fig. 2).

### 4.3 Background from $K_{S} \rightarrow \pi^{0} \pi_{D}^{0}$ and $K_{L} \rightarrow 3 \pi^{0}$

Applying all the selection criteria described above to simulated $K_{S} \rightarrow \pi^{0} \pi_{D}^{0}$ and $K_{L} \rightarrow 3 \pi^{0}$ events, no candidate remains, corresponding to a rejection factor of at least $2.5 \times 10^{6}$ for $K_{S} \rightarrow \pi^{0} \pi_{D}^{0}$ and of at least $7.5 \times 10^{5}$ for $K_{L} \rightarrow 3 \pi^{0}$. The background from
$K_{S} \rightarrow \pi^{0} \pi_{D}^{0}$ is expected to be less than 0.2 events, while the background from $K_{L} \rightarrow 3 \pi^{0}$ is expected to be less than 0.1 events.

### 4.4 Background from $K_{L} \rightarrow \pi^{0} \gamma \gamma$

A non reducible source of background is given by the decay $K_{L} \rightarrow \pi^{0} \gamma \gamma$, which cannot be distinguished from the signal. Using the branching fraction measured by the NA48 experiment [2], the background from this channel was computed to be about 0.1 events.

## 5 Normalisation and acceptance evaluation

The decay $K_{S} \rightarrow 2 \pi^{0}$ was chosen as the normalisation channel. Since the two decays differ only in the invariant mass of one $\gamma \gamma$ pair and were collected by the same trigger, systematic uncertainties are expected to cancel in the ratio. The same selection criteria were applied, with the only exceptions of $\chi_{2 \pi^{0}}^{2}$, which had to be less than 27 , and the invariant masses of the $\gamma \gamma$ pairs, which had to be within $\pm 3 \mathrm{MeV} / c^{2}$ of the nominal $\pi^{0}$ mass, considering the pairing which gives the lowest $\chi^{2}$. After all cuts, $3.3 \times 10^{6} K_{S} \rightarrow 2 \pi^{0}$ decays were selected, with an acceptance of $17.3 \%$ computed from a Monte Carlo sample, which included non-Gaussian tails in the energy resolution of the calorimeter, but had no accidentals and no simulation of the trigger. The comparison between data and Monte Carlo simulation in the $\chi_{2 \pi^{0}}^{2}$ and $z_{\text {vertex }}$ distributions for selected $K_{S} \rightarrow 2 \pi^{0}$ events is shown in Fig. 3. At high values of $z_{\text {vertex }}$ a slight inefficiency appears in the data due to the decay vertex cut at trigger level. Correcting for this inefficiency, data and simulation are in better agreement at high $z_{\text {vertex }}$. The correction is, however, not applied to the data in the analysis, since the trigger inefficiency is assumed to be the same for signal and normalisation channel.

The total number of $K_{S}$ with an energy between 70 and 170 GeV and decaying in the first 8 m of the decay region was measured from $K_{S} \rightarrow 2 \pi^{0}$ events to be $(4.1 \pm 0.2) \times 10^{8}$, taking into account the losses of statistics due to trigger downscaling ( $\sim 27 \%$ ) and to rejection of events with accidental in-time hits in the drift chambers or in the AKL ( $\sim 55 \%$ ). This flux was also computed, as a cross check, using the decay $K_{L} \rightarrow 3 \pi^{0}$, which however is statistically less significant, and found to be $(3.9 \pm 0.4) \times 10^{8}$. The two results are compatible within the error, which is due to the statistics used to compute acceptance and trigger efficiency and to the uncertainty on the branching ratios. The total number of $K_{S}$ is not used in the limit computation, since the same trigger efficiency is assumed for signal and normalisation channel.

For the signal an acceptance of $15.6 \%$ was determined from simulation where the amplitude predicted in $\chi P T$ [1] was used. The acceptance as a function of $z$ is shown in Fig. 4. The cut on $z \geq 0.2$ is expected to introduce a negligible systematic uncertainty, since the acceptance for the signal is nearly flat in that region of $z$.

## 6 Systematic uncertainties

The following effects were studied:

1. the background estimation was checked with an independent method based only on data. The background from $K_{S} \rightarrow 2 \pi^{0}$ decays with three clusters in the acceptance and one random cluster accidentally in time was assumed to have a flat distribution in the region $3 \mathrm{~ns}<\left|t_{c l}-t_{a v 4}\right|<6 \mathrm{~ns}$ for the farthest in-time cluster and to be the only class of background to be found in that region after applying most of the selection criteria. The expected background was then extrapolated from the
sidebands to the signal region and found to be $37 \pm 6_{\text {stat }}$ events. The expectation given by the simulation, applying the same selection, was $46 \pm 2_{\text {stat }}$ events. The two results are compatible within the statistical error and the relative difference of $24 \%$ is computed as systematic uncertainty.
2. the different cut on $\chi_{2 \pi^{0}}^{2}$ between signal and normalisation, together with a slightly different resolution of the best reconstructed $\pi^{0}$ mass between data and simulation, produced a systematic uncertainty of $0.6 \%$ on the ratio of acceptances when a window of $\pm 3 \mathrm{MeV} / c^{2}$ is used for the cut on the $\gamma \gamma$ invariant masses;
3. from simulation the relative difference in the trigger efficiency between $K_{S} \rightarrow \pi^{0} \gamma \gamma$ and $K_{S} \rightarrow 2 \pi^{0}$ was computed to be about $1.7 \%$;
4. not including the effect of non-Gaussian tails in the simulation produced an increase in the single acceptances of about $5 \%$, while the variation in the ratio was $1.5 \%$;
5 . the uncertainty of $0.9 \%$ on the $K_{S} \rightarrow 2 \pi^{0}$ branching ratio gives a systematic uncertainty of the same amount;
5. the statistical error on the simulated sample is about $0.5 \%$;
6. varying the selection cuts had a negligible effect on the result.

The total systematic uncertainty was computed as the sum in quadrature of the individual uncertainties and estimated to be $24.1 \%$. The effect on the result is an increase of the BR limit of about $6 \%$ [7].

## 7 Result and conclusions

Applying all the selection criteria, $2 K_{S} \rightarrow \pi^{0} \gamma \gamma$ candidates were found and $3.1 \pm 0.1_{\text {stat }} \pm 0.7_{\text {syst }}$ background events were expected, mainly from $K_{S} \rightarrow 2 \pi^{0}$ decays with three clusters in the acceptance and one random cluster accidentally in time. The acceptance was computed to be $\alpha_{\pi^{0} \gamma \gamma}=15.6 \%$ for the signal and $\alpha_{2 \pi^{0}}=17.3 \%$ for the normalisation channel, in which $N_{2 \pi^{0}}=3.3 \times 10^{6}$ events were selected. The same trigger efficiency was used for the two decays. Using $N_{\pi^{0} \gamma \gamma}<3.14$, which corresponds to a confidence level of $90 \%$ when 2 events are seen and 3.1 background events are expected with a systematic uncertainty of $24 \%[7,8]$, an upper limit for the branching ratio of the decay $K_{S} \rightarrow \pi^{0} \gamma \gamma$ was calculated:

$$
B R\left(K_{S} \rightarrow \pi^{0} \gamma \gamma, z \geq 0.2\right)=\frac{N_{\pi^{0} \gamma \gamma}}{N_{2 \pi^{0}}} \cdot \frac{\alpha_{2 \pi^{0}}}{\alpha_{\pi^{0} \gamma \gamma}} \cdot B R\left(K_{S} \rightarrow 2 \pi^{0}\right)<3.3 \times 10^{-7} \text { at } 90 \% \text { C.L. }
$$

with $z=\frac{m_{\gamma \gamma}^{2}}{m_{K_{0}}^{2}}$.
This is the first upper limit on this branching ratio to be published. It lies about one order of magnitude higher than the branching ratio predicted by Chiral Perturbation Theory.

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Figure 1: Left: $\chi_{2 \pi^{0}}^{2}$ distribution for data (squares) and background simulation (solid lines) in $\chi_{2 \pi^{0}}^{2}$ control region, before the cut on $z$. Distributions are normalised to the $K_{S}$ flux. Right: $\chi_{2 \pi^{0}}^{2}$ distribution for data (squares), background simulation for misreconstructed $K_{S} \rightarrow 2 \pi^{0}$ (filled histogram) and $K_{S} \rightarrow \pi^{0} \gamma \gamma$ simulation (solid line). For the $K_{S} \rightarrow \pi^{0} \gamma \gamma$ simulation the normalisation is arbitrary.


Figure 2: $\left|t_{c l}-t_{a v 4}\right|$ for the farthest in-time cluster from the event time in $2 \pi^{0}$ decays in the data (left) and for the random cluster in background simulation (right). For the random cluster a flat distribution in $\left|t_{c l}-t_{a v 3}\right|$ was assumed. The full square and triangle represent max $\left(\left|t_{c l}-t_{a v 4}\right|\right)$ for each of the two selected events.


Figure 3: $\chi_{2 \pi^{0}}^{2}$ (left) and $z_{v e r t e x}$ (right) distributions of the selected $K_{S} \rightarrow 2 \pi^{0}$ events for data (squares) and simulation (solid line). In the left plot the complete selection has been applied except the $\chi_{2 \pi^{0}}^{2}$ cut and the distributions are normalised to the total number of events. In the right plot the complete selection has been applied except the $z_{\text {vertex }}$ cut and the distributions are normalised to the bin with the maximum number of events. The data distribution corrected for the trigger inefficiency (triangles) shows a better agreement with the simulation at high values of $z_{\text {vertex }}$.


Figure 4: Acceptance as a function of $z=m_{\gamma \gamma}^{2} / m_{K^{0}}^{2}$ for $K_{S} \rightarrow \pi^{0} \gamma \gamma$ simulated events.


[^0]:    ${ }^{1)}$ Based at Rutherford Appleton Laboratory, Chilton, Didcot,OX11 0QX, U.K.
    ${ }^{2)}$ Funded by the U.K. Particle Physics and Astronomy Research Council.
    ${ }^{3)}$ On leave from Sezione dell'INFN di Firenze, I-50125 Firenze, Italy.
    ${ }^{4)}$ On leave from Joint Institute for Nuclear Reaserch, Dubna, 141980, Russian Federation
    ${ }^{5)}$ Present address: EP, CERN, CH-1211, Geneva 23, Switzerland
    ${ }^{6}$ ) Dipartimento di Fisica dell'Universita' di Modena e Reggio Emilia, via G. Campi 213/A I-41100 Modena, Italy
    ${ }^{7}$ ) Funded by the German Federal Minister for Research and Technology (BMBF) under contract

