# Measurement of the $\bar{B}_{s}^{0} \rightarrow D_{s}^{-} D_{s}^{+}$and $\bar{B}_{s}^{0} \rightarrow D^{-} D_{s}^{+}$Effective Lifetimes 

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#### Abstract

The first measurement of the effective lifetime of the $\bar{B}_{s}^{0}$ meson in the decay $\bar{B}_{s}^{0} \rightarrow D_{s}^{-} D_{s}^{+}$is reported using a proton-proton collision data set, corresponding to an integrated luminosity of $3 \mathrm{fb}^{-1}$, collected by the LHCb experiment. The measured value of the $\bar{B}_{s}^{0} \rightarrow D_{s}^{-} D_{s}^{+}$effective lifetime is $1.379 \pm 0.026 \pm 0.017 \mathrm{ps}$, where the uncertainties are statistical and systematic, respectively. This lifetime translates into a measurement of the decay width of the light $\bar{B}_{s}^{0}$ mass eigenstate of $\Gamma_{L}=0.725 \pm 0.014 \pm 0.009 \mathrm{ps}^{-1}$. The $\bar{B}_{s}^{0}$ lifetime is also measured using the flavor-specific $\bar{B}_{s}^{0} \rightarrow$ $D^{-} D_{s}^{+}$decay to be $1.52 \pm 0.15 \pm 0.01 \mathrm{ps}$.


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A central goal in quark-flavor physics is to test whether the Cabibbo-Kobayashi-Maskawa mechanism [1,2] can fully describe all relevant weak decay observables, or if physics beyond the standard model (SM) is needed. In the neutral $B$ meson sector, the mass eigenstates do not coincide with the flavor eigenstates as a result of $B \bar{B}$ mixing. In addition to measurable mass splittings between the mass eigenstates [3], the $B_{s}$ system also exhibits a sizeable difference in the decay widths $\Gamma_{L}$ and $\Gamma_{H}$, where the subscripts $L$ and $H$ refer to the light and heavy mass eigenstates, respectively. This difference is due to the large decay width to final states accessible to both $B_{s}^{0}$ and $\bar{B}_{s}^{0}$. In the absence of $C P$ violation, the mass eigenstates are also eigenstates of $C P$. The summed decay rate of $B_{s}^{0}$ and $\bar{B}_{s}^{0}$ to the $C P$-even $D_{s}^{+} D_{s}^{-}$final state can be written as [4]

$$
\begin{align*}
\Gamma_{\bar{B}_{s}^{0} \rightarrow D_{s}^{-} D_{s}^{+}}(t)+\Gamma_{B_{s}^{0} \rightarrow D_{s}^{+} D_{s}^{-}}(t) \propto & \left(1+\cos \phi_{s}\right) e^{-\Gamma_{L} t} \\
& +\left(1-\cos \phi_{s}\right) e^{-\Gamma_{H} t}, \tag{1}
\end{align*}
$$

where $\phi_{s}$ is the ( $C P$-violating) relative weak phase between the $\bar{B}_{s}^{0}$ mixing and $b \rightarrow c \bar{c} s$ decay amplitudes.

The untagged decay rate in Eq. (1) provides a probe of $\phi_{S}, \Gamma_{L}$, and $\Gamma_{H}$ in a way that is complementary to direct determinations using $C P$ violating asymmetries [5]. Since $\phi_{s}$ is small, Eq. (1) is well approximated by a single exponential

$$
\begin{equation*}
\Gamma_{\bar{B}_{s}^{0} \rightarrow D_{s}^{-} D_{s}^{+}}(t)+\Gamma_{B_{s}^{0} \rightarrow D_{s}^{+} D_{s}^{-}}(t) \propto e^{-t / \tau_{\bar{B}_{s}^{0} \rightarrow D_{s}^{-} D_{s}^{+}}^{e l}} \tag{2}
\end{equation*}
$$

which defines the $\bar{B}_{s}^{0} \rightarrow D_{s}^{-} D_{s}^{+}$effective lifetime, where $\tau_{\bar{B}_{s}^{s} \rightarrow D_{s}^{-} D_{s}^{+}}^{\mathrm{eff}}=\left(1 / \Gamma_{s}\right)\left[1-y_{s} \cos \varphi_{s}+\mathcal{O}\left(y_{s}^{2}\right)\right] \quad[4,6]$.

[^0]Here, $\quad y_{s} \equiv \Delta \Gamma_{s} /\left(2 \Gamma_{s}\right), \quad \Delta \Gamma_{s} \equiv \Gamma_{L}-\Gamma_{H} \quad$ and $\quad \Gamma_{s} \equiv$ $\left(\Gamma_{H}+\Gamma_{L}\right) / 2$. In this formulation, we have assumed that direct $C P$ violation is negligible in the $\bar{B}_{s}^{0} \rightarrow D_{s}^{-} D_{s}^{+}$decay, in accord with SM expectations. Using the measured value of $\phi_{s}=0.01 \pm 0.07 \pm 0.01 \mathrm{rad}$ [5], which is in good agreement with the SM expectation of $-0.0363_{-0.0015}^{+0.0016} \mathrm{rad}$ [7], it follows that $\tau_{\bar{B}_{s}^{0} \rightarrow D_{s}^{-} D_{s}^{+}}^{\mathrm{eff}} \simeq \Gamma_{\mathrm{L}}^{-1}$.

The most precise measurement to date of the effective lifetime in a $C P$-even final state used $\bar{B}_{s}^{0} \rightarrow K^{+} K^{-}$ [8] decays, and yielded a value $\tau_{\bar{B}_{s}^{0^{\prime}} \rightarrow K^{+} K^{-}}^{\text {enf }}=1.455 \pm$ 0.046 (stat) $\pm 0.006$ (syst) ps. Loop contributions, both within, and possibly beyond the SM, are expected to be significantly larger in $\bar{B}_{s}^{0} \rightarrow K^{+} K^{-}$than in $\bar{B}_{s}^{0} \rightarrow D_{s}^{-} D_{s}^{+}$. These contributions give rise to direct $C P$ violation in the $\bar{B}_{s}^{0} \rightarrow K^{+} K^{-}$decay [9], which lead to differences between $\tau^{\text {eff }}$ in these two $C P$ final state decays, making a comparison of their effective lifetimes interesting. Measurements have also been made in $C P$-odd modes, such as $\bar{B}_{s}^{0} \rightarrow$ $J / \psi f_{0}(980)$ [10,11] and $\bar{B}_{s}^{0} \rightarrow J / \psi K_{S}^{0}$ [12]. The most precise value is from the former, yielding $\tau_{\bar{B}_{s}^{0} \rightarrow J / \psi f_{0}(980)}^{\mathrm{eff}^{\prime}}=$ $1.700 \pm 0.040$ (stat) $\pm 0.026$ (syst) ps [10]. Constraints from these measurements on the ( $\Delta \Gamma_{s}, \phi_{s}$ ) parameter space are given in Refs. $[4,13]$. Improved precision on the effective lifetimes will enable more stringent tests of the consistency between the direct measurements of $\Delta \Gamma_{s}$ and $\phi_{s}$, and those inferred using effective lifetimes.

In this Letter, the $\bar{B}_{s}^{0} \rightarrow D_{s}^{-} D_{s}^{+}$time-dependent decay rate is normalized to the corresponding rate in the $B^{-} \rightarrow$ $D^{0} D_{s}^{-}$decay, which has similar final state topology and kinematic properties, and a precisely measured lifetime of $\tau_{B^{-}}=1.641 \pm 0.008 \mathrm{ps}$ [14]. As a result, many of the systematic uncertainties cancel in the measured ratio. The relative rate is then given by

$$
\begin{equation*}
\frac{\Gamma_{\bar{B}_{s}^{0} \rightarrow D_{s}^{-} D_{s}^{+}}(t)+\Gamma_{B_{s}^{0} \rightarrow D_{s}^{+} D_{s}^{-}}(t)}{\Gamma_{B^{-} \rightarrow D^{0} D_{s}^{-}}(t)+\Gamma_{B^{+} \rightarrow \bar{D}^{0} D_{s}^{+}}(t)} \propto e^{-\alpha_{s u} t}, \tag{3}
\end{equation*}
$$

where $\alpha_{s u}=1 / \tau_{B_{s}^{\prime} \rightarrow D_{s}^{-}}^{\mathrm{eff}} D_{s}^{+}-1 / \tau_{B^{-}}$. A measurement of $\alpha_{s u}$ therefore determines $\tau_{\bar{B}_{s}^{0} \rightarrow D_{s}^{-} D_{s}^{+}}^{\text {eff }}$.

The $\bar{B}_{s}^{0}$ meson lifetime is also measured using the flavorspecific, Cabibbo-suppressed $\bar{B}_{s}^{0} \rightarrow D^{-} D_{s}^{+}$decay. Its timedependent rate is normalized to that of the $B^{0} \rightarrow D^{-} D_{s}^{+}$ decay. In what follows, the symbol $B$ without a flavor designation refers to either a $B^{-}, \bar{B}^{0}$, or $\bar{B}_{s}^{0}$ meson, and $D$ refers to either a $D^{0}, D^{+}$, or $D_{s}^{+}$meson. Unless otherwise indicated, charge conjugate final states are included.

The measurements presented use a proton-proton ( $p p$ ) collision data sample corresponding to $3 \mathrm{fb}^{-1}$ of integrated luminosity, $1 \mathrm{fb}^{-1}$ recorded at a center-of-mass energy of 7 TeV , and $2 \mathrm{fb}^{-1}$ at 8 TeV , collected by the LHCb experiment. The LHCb detector [15] includes a highprecision tracking system that provides a momentum measurement with relative uncertainty of about $0.5 \%$ and impact parameter (IP) resolution of $20 \mu \mathrm{~m}$ for tracks with large transverse momentum $\left(p_{\mathrm{T}}\right)$. A pair of ringimaging Cherenkov detectors [16] provide charged hadron identification. Photon, electron, and hadron candidates are discriminated using a calorimeter system consisting of scintillating-pad and preshower detectors, and electromagnetic and hadronic calorimeters. Muons are identified by a system composed of alternating layers of iron and multiwire proportional chambers [17].

The trigger [18] consists of a hardware stage, based on information from the calorimeter and muon systems, followed by a software stage, which applies a full event reconstruction $[18,19]$. Of the $B$ meson candidates considered in this analysis, about $60 \%$ are triggered at the hardware level by one or more of the final state particles in the signal $B$ decay. The remaining $40 \%$ are triggered due to other activity in the event. The software trigger requires a two-, three- or four-track secondary vertex with a large $p_{\text {T }}$ sum of the tracks and a significant displacement from the primary $p p$ interaction vertices ( PVs ). At least one track should have $p_{\mathrm{T}}>1.7 \mathrm{GeV} / c$ and $\chi_{\mathrm{IP}}^{2}$ with respect to any PV greater than 16 , where $\chi_{\mathrm{IP}}^{2}$ is defined as the difference in $\chi^{2}$ of a given PV reconstructed with and without the considered particle included.

Proton-proton collisions are simulated using Pythia [20] with a specific LHCb configuration [21]. Decays of hadronic particles are described by EvtGen [22], in which final state radiation is generated using Рнотоs [23]. The interaction of the generated particles with the detector and its response are implemented using the Geant 4 tool kit [24] as described in Ref. [25].

Signal $\bar{B}_{s}^{0} \rightarrow D_{s}^{-} D_{s}^{+}$candidates are reconstructed using four final states: (i) $D_{s}^{+} \rightarrow K^{+} K^{-} \pi^{+}, D_{s}^{-} \rightarrow K^{-} K^{+} \pi^{-}$, (ii) $D_{s}^{+} \rightarrow K^{+} K^{-} \pi^{+}, D_{s}^{-} \rightarrow \pi^{-} \pi^{+} \pi^{-}$, (iii) $D_{s}^{+} \rightarrow K^{+} K^{-} \pi^{+}$, $D_{s}^{-} \rightarrow K^{-} \pi^{+} \pi^{-}$, and (iv) $D_{s}^{+} \rightarrow \pi^{+} \pi^{-} \pi^{+}, D_{s}^{-} \rightarrow \pi^{-} \pi^{+} \pi^{-}$. In the normalization mode, $B^{-} \rightarrow D^{0} D_{s}^{-}$, only the final state $D^{0} \rightarrow K^{-} \pi^{+}, D_{s}^{-} \rightarrow K^{-} K^{+} \pi^{-}$is used. For the $\bar{B}_{s}^{0} \rightarrow$ $D^{-} D_{s}^{+}$decay and the corresponding $B^{0}$ normalization mode, the $D^{-} \rightarrow K^{+} \pi^{-} \pi^{-}, D_{s}^{+} \rightarrow K^{+} K^{-} \pi^{+}$final state is
used. Loose particle identification (PID) requirements are imposed on kaon and pion candidates, with efficiencies typically in excess of $95 \%$. The $D$ candidates are required to have masses within $25 \mathrm{MeV} / c^{2}$ of their known values [14] and to have vertex separation from the $B$ vertex satisfying $\chi_{\mathrm{VS}}^{2}>2$. Here $\chi_{\mathrm{VS}}^{2}$ is the increase in $\chi^{2}$ of the parent ( $B$ ) vertex fit when the ( $D$ meson) decay products are constrained to come from the parent vertex, relative to the nominal fit. To suppress the large background from $\bar{B}_{s}^{0} \rightarrow$ $D_{s}^{+} \pi^{-} \pi^{+} \pi^{-}$decays, $D_{s}^{-} \rightarrow \pi^{-} \pi^{+} \pi^{-}$candidates are required to have $\chi_{\mathrm{VS}}^{2}>6$. As the signatures of $b$-hadron decays to double-charm final states are similar, vetoes are employed to suppress the cross-feed resulting from particle misidentification, following Ref. [26]. For the $D_{s}^{+} \rightarrow$ $K^{+} \pi^{-} \pi^{+}$decay, an additional veto to suppress cross feed from $D^{+} \rightarrow K^{-} \pi^{+} \pi^{+}$with double misidentification is employed, which renders this background negligible. Potential background to $D_{s}^{+}$decays from $D^{*+} \rightarrow D^{0} \pi^{+}$ with $D^{0} \rightarrow K^{+} K^{-}, \pi^{+} \pi^{-}$is also removed by requiring the mass difference, $M\left(D^{0} \pi^{+}\right)-M\left(D^{0}\right)>150 \mathrm{MeV} / c^{2}$. The production point of each $B$ candidate is taken as the PV with the smallest $\chi_{\mathrm{IP}}^{2}$ value. All $B$ candidates are refit taking both $D$ mass and vertex constraints into account [27].

The efficiencies of the PID and veto requirements are evaluated using dedicated $D^{*+} \rightarrow D^{0} \pi^{+}, D^{0} \rightarrow K^{-} \pi^{+}$ calibration samples collected at the same time as the data. The kinematic distributions of kaons and pions from the calibration sample are reweighted using simulation to match those of the $B$ decays under study. The combined PID and veto efficiencies are $91.4 \%$ for $B^{-} \rightarrow D^{0} D_{s}^{-}$, $88.0 \%$ for $\left(\bar{B}_{s}^{0}, B^{0}\right) \rightarrow D^{-} D_{s}^{+}$, and $86.5 \%, 90.8 \%, 86.6 \%$, and $95.9 \%$ for the $\bar{B}_{s}^{0} \rightarrow D_{s}^{-} D_{s}^{+}$final states (i)-(iv), respectively.

To further improve the signal-to-background ratio, a boosted decision tree (BDT) [28,29] algorithm using seventeen input variables is employed. Five variables from the $B$ candidate are used, including $\chi_{\mathrm{IP}}^{2}$, the vertex fit $\chi_{\mathrm{vtx}}^{2}$ (with $D$ mass, and vertex constraints), the $\mathrm{PV} \chi_{\mathrm{VS}}^{2}, p_{\mathrm{T}}$, and a $p_{\mathrm{T}}$ imbalance variable [30]. For each $D$ daughter, $\chi_{\mathrm{P}}^{2}$, the flight distance from the $B$ vertex normalized by its uncertainty, and the maximum distance between the trajectories of any pair of particles in the $D$ decay, are used. Last, for each $D$ candidate, the minimum $p_{\mathrm{T}}$, and both the smallest and largest $\chi_{\mathrm{IP}}^{2}$, among the $D$ daughter particles are used. The BDT uses simulated decays to emulate the signal and wrong-charge final states from data with masses larger than $5.2 \mathrm{GeV} / c^{2}$ for the background. Here, wrong charge refers to $D_{s}^{ \pm} D_{s}^{ \pm}, D^{ \pm} D_{s}^{ \pm}$, and $D^{0} D_{s}^{+}$combinations, where in the latter case we remove candidates within $30 \mathrm{MeV} / \mathrm{c}^{2}$ of the $B^{+}$mass [14], to remove the small doubly Cabibbosuppressed decay contribution to this final state. The selection requirement on the BDT output is chosen to maximize the expected $\bar{B}_{s}^{0} \rightarrow D_{s}^{-} D_{s}^{+}$signal significance, corresponding to signal and background efficiencies of about $97 \%$ and $33 \%$, respectively. More than one candidate


FIG. 1. Ratio of selection efficiencies for $B^{-} \rightarrow D^{0} D_{s}^{-}$relative to $\bar{B}_{s}^{0} \rightarrow D_{s}^{-} D_{s}^{+}$decays as a function of decay time. The uncertainties shown are due to finite simulated sample sizes.
per event is allowed, but after all selections the fraction of events with multiple candidates is below $0.25 \%$ for all modes.

For the lifetime analysis, we consider only $B$ candidates with reconstructed decay time less than 9 ps . The decay time is computed after a kinematic fit that applies both $D$ mass and all vertex constraints. Signal efficiencies as functions of decay time are determined using simulated decays after all selections, except those that involve PID, as described above. The resulting $B^{-}$to $\bar{B}_{s}^{0}$ relative efficiency as a function of decay time is shown in Fig. 1, where six decay time bins with widths ranging between 1 and 3 ps are used. For the $\bar{B}_{s}^{0} \rightarrow D_{s}^{-} D_{s}^{+}$decay, the efficiency used in the ratio is the weighted average of the $D_{s}^{+} D_{s}^{-}$final states (i)-(iv), where the weights are obtained from the observed yields in data. The efficiency accounts for the migration between bins, which is small since the resolution on the reconstructed time of $\sim 50 \mathrm{fs}$ is much less than the bin width. Moreover, the time resolution is nearly identical for the signal and normalization modes, and is independent of the reconstructed lifetime. The relative efficiency is consistent with being independent of decay time; however, the computed bin-by-bin efficiencies are used to correct the data.

The mass distributions for the signal, summed over the four final states, and the normalization modes, are shown in Fig. 2, along with the results of binned maximum likelihood fits. The $B$ signal shapes are each modeled using the sum of two Crystal Ball (CB) functions [31] with a common mean. The shape parameters are fixed from fits to simulated signal decays, with the exception of the resolution parameter, which is found to be about $15 \%$ larger in data than simulation. The shape of the low-mass background from partially reconstructed decays, where either a photon or pion is missing, is obtained from simulated decays, as are the cross-feed background shapes from $B^{0} \rightarrow D^{-} D_{s}^{+}$and $\Lambda_{b}^{0} \rightarrow \Lambda_{c}^{+} D_{s}^{-}$decays $\left(\bar{B}_{s}^{0} \rightarrow D_{s}^{-} D_{s}^{+}\right.$ channel only). An additional peaking background due to $B \rightarrow D K^{-} K^{+} \pi^{-}$decays is also included in the fit. Its shape is obtained from simulation and the yield is fixed to be $1 \%$ of the signal yield from a fit to the $D$ mass sidebands. The combinatorial background shape is described by an exponential function with the shape parameter fixed to the value obtained from a fit to the mass spectrum of wrong-charge candidates. All yields, except that of the $B \rightarrow D K^{-} K^{+} \pi^{-}$, are freely varied in the fit to the full data sample.

In total, we observe $3499 \pm 65 \quad \bar{B}_{s}^{0} \rightarrow D_{s}^{-} D_{s}^{+}$and $19432 \pm 140 B^{-} \rightarrow D^{0} D_{s}^{-}$decays. The data are split into the time bins shown in Fig. 1, and each mass distribution is fitted with the CB widths fixed to the values obtained from the full fit. The independence of the signal shape parameters on decay time is validated using simulated decays. The ratios of yields are then computed, and corrected by the relative efficiencies shown in Fig. 1. Figure 3 shows the efficiency-corrected yield ratios as a function of decay time. The data points are placed at the average time within each bin assuming an exponential form $e^{-t /(1.5 \mathrm{ps})}$. Fitting an exponential function to the data yields the result $\alpha_{s u}=0.1156 \pm 0.0139 \mathrm{ps}^{-1}$. The $\chi^{2}$ of the fit is 6.2 for 4 degrees of freedom. The uncertainty in the fitted slope due to using the value of 1.5 ps to get the average time in each bin is negligible. Using the known $B^{-}$lifetime, $\tau_{\bar{B}_{s}^{0} \rightarrow D_{s}^{-} D_{s}^{+}}^{\text {eff }}$ is determined to be $1.379 \pm 0.026$ (stat) ps.


FIG. 2 (color online). Mass distributions and fits to the full data sample for (left) $\bar{B}_{s}^{0} \rightarrow D_{s}^{-} D_{s}^{+}$and (right) $B^{-} \rightarrow D^{0} D_{s}^{-}$candidates. The points are the data and the curves and shaded regions show the fit components.


FIG. 3 (color online). Efficiency corrected yield ratio of $\bar{B}_{s}^{0} \rightarrow$ $D_{s}^{-} D_{s}^{+}$relative to $B^{-} \rightarrow D^{0} D_{s}^{-}$as a function of decay time, along with the exponential fit. The uncertainties are statistical only.

As a cross-check, the full analysis is applied to the $B^{-} \rightarrow D^{0} D_{s}^{-}$and $B^{0} \rightarrow D^{-} D_{s}^{+}$decays, treating the former as the signal mode and the latter as the normalization mode. The fitted value for $\alpha \equiv 1 / \tau_{B^{0}}-1 / \tau_{B^{-}} \quad$ is $0.0500 \pm 0.0076 \mathrm{ps}^{-1}$, in excellent agreement with the expected value of $0.0489 \pm 0.0042$ [14]. This check indicates that the relative lifetime measurements are insensitive to small differences in the number of charged particles or lifetimes of the $D$ mesons in the final state. The $B^{0} \rightarrow D^{-} D_{s}^{+}$mode could have also been used as a normalization mode for the $\bar{B}_{s}^{0} \rightarrow D_{s}^{-} D_{s}^{+}$time-dependent rate measurement, but due to limited simulated sample sizes it would have led to a larger systematic uncertainty.

As the method for determining $\tau_{\bar{B}_{s}^{0} \rightarrow D_{s}^{-} D_{s}^{+}}^{\text {eff }}$ relies on ratios of yields and efficiencies, many systematic uncertainties cancel. The robustness of the relative acceptance is tested by subdividing the sample into mutually exclusive subsamples based on (i) center of mass energy, (ii) $D_{s}^{-} D_{s}^{+}$final states, and (iii) the hardware trigger decision, and searching for deviations larger than those expected from the finite sizes of the samples. The results from all checks were found to be within one standard deviation of the average. Based on the largest deviation, we assign a 0.010 ps systematic uncertainty due to the modeling of the relative acceptance. The statistical precision on the relative acceptance, as obtained from simulation, contributes an uncertainty of 0.011 ps . Using a different signal shape to fit the data leads to 0.003 ps uncertainty. If the combinatorial background shape parameter is allowed to freely vary in each time bin fit, we find a deviation of 0.001 ps from the nominal value of $\tau_{\overline{B_{s}^{0}} \rightarrow D_{s}^{-}}^{\text {eff }} D_{s}^{+}$, which is assigned as a systematic uncertainty. Because of the presence of a nontrivial acceptance function, the result of fitting a single exponential to the untagged $B_{s}^{0}$ decay time distribution does not coincide precisely with the formal definition of the effective lifetime [32]. The deviation between $\tau_{\bar{B}_{s}^{0} \rightarrow D_{s}^{-} D_{s}^{+}}^{\mathrm{eff}}$ and the single exponential fit
is at most 0.001 ps [32], which is assigned as a systematic uncertainty. The precision on the $B^{-}$lifetime leads to 0.008 ps uncertainty on the value of $\tau_{\bar{B}_{s}^{0} \rightarrow D_{s}^{-} D_{s}^{+}}^{\mathrm{eff}}$. Summing these deviations in quadrature, we obtain a total systematic uncertainty of 0.017 ps . In converting to a measurement of $\Gamma_{L}$, an additional uncertainty due to a small $C P$-odd component of expected size $1-\cos \phi_{s}=$ $(0.1 \pm 3.2) \times 10^{-3}$ [5] leads to a negative bias no larger than $-0.001 \mathrm{ps}^{-1}$. This is included in the $\Gamma_{L}$ systematic uncertainty.

The value of $\tau_{\bar{B}_{s}^{0} \rightarrow D_{s}^{-} D_{s}^{+}}^{\mathrm{eff}}$ and the corresponding decay width of the light $\bar{B}_{s}^{0}$ mass eigenstate are determined to be

$$
\begin{aligned}
\tau_{\bar{B}_{s}^{0} \rightarrow D_{s}^{-} D_{s}^{+}}^{\mathrm{eff}} & =1.379 \pm 0.026 \pm 0.017 \mathrm{ps} \\
\Gamma_{L} & =0.725 \pm 0.014 \pm 0.009 \mathrm{ps}^{-1}
\end{aligned}
$$

where the first uncertainty is statistical and the second is systematic. These are the first such measurements using the $\bar{B}_{s}^{0} \rightarrow D_{s}^{-} D_{s}^{+}$decay. The measured effective lifetime represents the most precise measurement of the width of the light $\bar{B}_{s}^{0}$ mass eigenstate, and is about 1 standard deviation lower than the value obtained using $\bar{B}_{s}^{0} \rightarrow K^{+} K^{-}$decays [8]. Compared to the $\bar{B}_{s}^{0} \rightarrow D_{s}^{-} D_{s}^{+}$decay, which is dominated by tree-level processes, the $\bar{B}_{s}^{0} \rightarrow K^{+} K^{-}$decay is expected to have larger relative contributions from SMloop amplitudes [4,33,34], and, therefore, one should not naively average the effective lifetimes from these two decays. Moreover, if non-SM particles contribute additional amplitudes, their effect is likely to be larger in $\bar{B}_{s}^{0} \rightarrow$ $K^{+} K^{-}$than in $\bar{B}_{s}^{0} \rightarrow D_{s}^{-} D_{s}^{+}$decays [35].

The value of $\Gamma_{L}$ obtained in this analysis may be compared to the value inferred from the time-dependent analyses of $J / \psi K^{+} K^{-}$and $J / \psi \pi^{+} \pi^{-}$decays. Using the values $\Gamma_{s}=0.661 \pm 0.004 \pm 0.006 \mathrm{ps}^{-1}$ and $\Delta \Gamma_{s}=$ $0.106 \pm 0.011 \pm 0.007 \mathrm{ps}^{-1} \quad[5]$, we find $\Gamma_{L}=0.714 \pm$ $0.010 \mathrm{ps}^{-1}$, in good agreement with the value obtained from $\tau_{\bar{B}_{s}^{\mathrm{eff}}}^{\mathrm{eff}} D_{s}^{-} D_{s}^{+}$.

The effective lifetime of the flavor-specific $\bar{B}_{s}^{0} \rightarrow D^{-} D_{s}^{+}$ decay is also measured, using the $B^{0} \rightarrow D^{-} D_{s}^{+}$decay for normalization. The technique is identical to that described above, with the simplification that the relative efficiency equals 1 , since the final states are identical. Effects due to the mass difference between the $\bar{B}_{s}^{0}$ and $B^{0}$ mesons are negligible. A tighter BDT selection is imposed to optimize the expected signal-to-background ratio, which results in signal and background efficiencies of $87 \%$ and $11 \%$, respectively. The mass spectrum and the corresponding fit are shown in Fig. 4, where the fitted components are analogous to those described previously. A total of $230 \pm$ $18 \bar{B}_{s}^{0} \rightarrow D^{-} D_{s}^{+}$and $21195 \pm 147 B^{0} \rightarrow D^{-} D_{s}^{+}$decays are obtained. The time bins are the same as above, except the $6-9 \mathrm{ps}$ bin is dropped, since the yield in the signal mode beyond 6 ps is negligible. The relative decay rate is fitted to


FIG. 4 (color online). Mass distribution and fits to the full data sample for $\bar{B}_{s}^{0}$ and $B^{0}$ decays into the $D^{-} D_{s}^{+}$final state. The points are the data and the curves and shaded regions show the fit components.
an exponential form $\mathcal{C} e^{-\beta t}$, where $\mathcal{C}$ is a normalization constant. The fitted value of $\beta$ is $0.000 \pm 0.068 \mathrm{ps}^{-1}$. The systematic uncertainty due to the signal shape is 0.007 ps , obtained by using a different signal shape function. The exponential background shape is fixed in the nominal fit using $D^{ \pm} D_{s}^{ \pm}$candidates, and a systematic uncertainty of 0.010 ps is determined by allowing its shape parameter to vary freely in the fit. In determining the effective lifetime, an uncertainty of 0.007 ps due to the limited precision of the $B^{0}$ lifetime [14] is also included. The resulting effective lifetime in the $\bar{B}_{s}^{0} \rightarrow D^{-} D_{s}^{+}$mode is

$$
\tau_{\bar{B}_{s}^{\mathrm{eff}} \rightarrow D^{-} D_{s}^{+}}^{\mathrm{e}}=1.52 \pm 0.15 \pm 0.01 \mathrm{ps}
$$

This is the first measurement of the $\bar{B}_{s}^{0}$ lifetime using the $\bar{B}_{s}^{0} \rightarrow D^{-} D_{s}^{+}$decay. Its value is consistent with previous direct and indirect measurements of the $\bar{B}_{s}^{0}$ lifetime in other flavor-specific decays.

In summary, we report the first measurement of the $\bar{B}_{s}^{0} \rightarrow$ $D_{s}^{-} D_{s}^{+}$effective lifetime and present the most precise direct measurement of the width of the light $B_{s}$ mass eigenstate. Their values are $\tau_{\bar{B}_{\dot{0}}^{\mathrm{eff}} \rightarrow D_{s}^{-} D_{s}^{+}}^{\mathrm{e}}=1.379 \pm 0.026 \pm 0.017 \mathrm{ps}$ and $\Gamma_{L}=0.725 \pm 0.014 \pm 0.009 \mathrm{ps}^{-1}$. The $\Gamma_{L}$ result is consistent with the value obtained from previously measured values of $\Delta \Gamma_{s}$ and $\Gamma_{s}$ [5]. We also determine the average $\bar{B}_{s}^{0}$ lifetime to be $1.52 \pm 0.15 \pm 0.01 \mathrm{ps}$ using the $\bar{B}_{s}^{0} \rightarrow D^{-} D_{s}^{+}$decay, which is consistent with other measurements.

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