This is the peer reviewd version of the followng article:
Robust area coverage with connectivity maintenance / Siligardi, L.; Panerati, J.; Kaufmann, M.; Minelli, M.; Ghedini, C.; Beltrame, G.; Sabattini, L 2019-:(2019), pp. 2202-2208. (Intervento presentato al convegno 2019 International Conference on Robotics and Automation, ICRA 2019 tenutosi a Palais des Congres de Montreal, can nel 2019) [10.1109/ICRA.2019.8793555].
Institute of Electrical and Electronics Engineers Inc.  Terms of use:
The terms and conditions for the reuse of this version of the manuscript are specified in the publishing policy. For all terms of use and more information see the publisher's website.
20/07/2024 22:20

(Article begins on next page)

# Robust Area Coverage with Connectivity Maintenance

Luca Siligardi<sup>†</sup>, Jacopo Panerati<sup>\*</sup>, Marcel Kaufmann<sup>\*</sup>, Marco Minelli<sup>†</sup>, Cinara Ghedini<sup>‡</sup>, Giovanni Beltrame<sup>\*</sup>, and Lorenzo Sabattini<sup>†</sup>

Abstract—Robot swarms herald the ability to solve complex tasks using a large collection of simple devices. However, engineering a robotic swarm is far from trivial, with a major hurdle being the definition of the control laws leading to the desired globally coordinated behavior. Communication is a key element for coordination and it is considered one of the current most important challenges for swarm robotics. In this paper, we study the problem of maintaining robust swarm connectivity while performing a coverage task based on the Voronoi tessellation of an area of interest. We implement our methodology in a team of eight Khepera IV robots. With the assumptions that robots have a limited sensing and communication range—and cannot rely on centralized processing-we propose a tri-objective control law that outperforms other simpler strategies (e.g. a potentialbased coverage) in terms of network connectivity, robustness to failure, and area coverage.

## I. INTRODUCTION

Lowering costs, collaborative performance, and augmented reliability through inherent redundancy are just some of the attractive qualities of multi-robot systems. Robot swarms, specifically, are very large multi-robot systems composed by moderately simple devices. They carry the promise of fully exploiting biomimetics and the economy of scale. Inspired by nature, swarm robotics can benefit from the application of knowledge from several different fields, including software engineering and distributed systems [1]. In multi-robot systems, a crucial element of effective collective performance is reliable communication. For any two robots to be able to talk, the underlying communication network must enforce global connectivity. In the literature, the value of the algebraic connectivity is often used as a proxy [2] (see Figure 1). Yet, preserving connectivity per se is typically not enough: we want robots to actually do something-and this is often a spatially distributed task. The problem of optimally deploying a group of mobile robots in a given environment is generally referred to as a coverage problem. This class of problems has applications in several domains, such as multi-robot systems used for search and rescue [3], deployment of mobile sensor networks [4], or ocean sensing and sampling [5].

In our previous work [6], we implemented a coverage task using a contribution based on the Lennard-Jones potential—a

†Università degli Studi di Modena e Reggio Emilia, Department of Sciences and Methods for Engineering, e-mail: 89071@studenti.unimore.it, {marco.minelli, lorenzo.sabattini}@unimore.it

\*Polytechnique Montréal, Department of Computer and Software Engineering, e-mail: {jacopo.panerati, marcel.kaufmann, giovanni.beltrame}@polymtl.ca

<sup>‡</sup>Instituto Tecnológico de Aeronáutica, Departamento de Computação Científica, e-mail: cinara@ita.br

molecular interaction model. Simulation results [7], however, suggest that a Voronoi tessellation-based coverage approach could help improve the robustness of the network—that is, the system's ability to mitigate the effects of node failures through predictive actions that avoid vulnerable topological configurations [8].

The contribution of this paper is two-fold: (i) first, we implement the methodology from [8]—in particular, its Voronoi tessellation-based coverage control—in a real multirobot setup; (ii) second, we compare our new results with those from a previous robotic implementation exploiting a simpler potential-based coverage approach. By doing so, we are able to (i) validate the insights obtained from simulations in [8] and (ii) establish the superior performance—especially in terms of robustness—of Voronoi-based coverage w.r.t. potential-based coverage. In what follows, Sections II to IV are dedicated to a review of the existing literature and the background theory of our methodology; Sections V to VI describe our robotic implementation and experiments; our findings are reported in Section VII; and Section VIII concludes the paper.

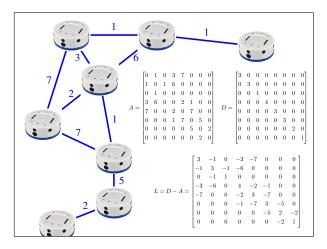


Fig. 1. Networking in multi-robot systems can be described with the aid of graph theory through the adjacency A, degree D, and Laplacian L matrices. The second-smallest eigenvalue of L is also called algebraic connectivity  $\lambda_2$  and it reveals whether the graph is connected.

## II. RELATED WORK

Juliá *et al.*'s survey paper [9] summarizes the main approaches proposed in the literature to spread groups of robots in an environment for exploration purposes. Several methods start by performing a segmentation of the environment and subsequently planning the motion of the robots to maximize

the coverage of the area [10]. Semantic information on the most relevant areas can be used, as described in [11], to provide guidance to the robots, thus achieving a non-uniform coverage of the environment. Deployment of the robots in the environment can be achieved by carefully combining attraction and repulsion control laws [12], exploiting, for instance, artificial potential fields [13], such as the one defined by Lennard-Jones [1] (see Equation 13).

While these methods are effective for guaranteeing stability of the group (e.g., cohesiveness, convergence), they generally do not provide any guarantee of uniformity or reliability in area coverage. Hence, several area segmentation methods have been developed [14] to assign each robot to a portion of the entire environment, in such a way that area is covered effectively and dependably. Techniques based on Voronoi tessellation are often used because they provide an optimal partitioning of the environment [15]. Furthermore, decentralized control strategies can be developed to asymptotically achieve area coverage based on centroidal Voronoi tessellation [16]. This makes the technique particularly suitable for multi-robot and swarm systems. Enhanced control strategies have been also developed for deploying robots to cover non-convex environments [17], [18].

As it is often the case in multi-robot applications, area coverage control strategies are usually developed under constraints entailed by the topology of the robots' communication graph. In particular, preservation of connectivity as the system evolves is often a desired feature. In real-robot systems, exchange of information can be based on limitedrange communication devices. Hence, mobility of the robots may lead to disconnections. Few works in the literature, when considering a multi-robot exploration problem, allow the communication graph to temporarily loose connectivity [19]–[21]. The path of the robots is, however, carefully planned so that connection is restored at some point in the future. While these approaches guarantee a certain level of flexibility, the motion of the robots needs to be carefully planned in advance, which can not always be achieved in unknown and harsh environments.

To overcome these issues, we need to impose constraints on the robots' motion to guarantee the preservation of the communication graph as the system explores. Several strategies can be found in the literature to preserve all the links of an initially connected communication graph [22], [23], or some global properties of the graph itself [24]–[26].

It is worth noting that, when dealing with real-world robotic systems, guaranteeing connectivity maintenance is often not enough—in particular when considering robots that are subject to failures. In fact, connectivity preservation *per se* does not prevent the system to evolve into configurations where a single point of failure can be detrimental for the overall graph connectivity. It is then necessary to devise robust control strategies to avoid the onset of special nodes whose failure could lead to network fragmentation.

#### III. SYSTEM MODEL

In this work, we consider a multi-robot system comprising N robots able to communicate with one other within a communication radius R. The resulting communication topology can be represented by an undirected graph G in which each robot is a node and each communication link between two robots is an edge. Let each robot's state be its position  $p_i \in \mathbb{R}^m$  and let  $p = \left[p_1^T \dots p_N^T\right]^T \in \mathbb{R}^{Nm}$  be the state vector of the multi-robot system. For the sake of generalization, we consider weighted graphs, where edge weights  $w_{ij}$  are defined as follows:

$$w_{ij} = \begin{cases} e^{-\left(\|p_i - p_j\|^2\right)/\left(2\sigma^2\right)} & \text{if } \|p_i - p_j\| \le R\\ 0 & \text{otherwise} \end{cases}$$
 (1)

with  $e^{-(R^2)/(2\sigma^2)}=\Delta$ , where  $\Delta$  is a small predefined threshold. Each robot is modelled as a single integrator system, whose velocity can be directly controlled:

$$\dot{p}_i = u_i, \tag{2}$$

where  $u_i \in \mathbb{R}^m$  is the control. Recent research tackle the problem of connectivity for nonholonomic robots [27], [28]. For each robot, the control input must be set so that a global objective can be achieved. In the context of multi-robot environments, very often robots need to cooperatively follow multiple goals. For example, connectivity maintenance is a preponderant factor for information exchange. When dealing with fallible robots, it is necessary to avoid vulnerable topological configurations to increase robustness. These objectives were extensively assessed in simulation [7], [8]. In this work, we aim at (i) validating our simulation results in a real robotic set-up and (ii) investigating whether such approach can outperform previous real-robot implementations [6].

#### IV. COMBINED CONTROL LAW

The following combined control law aims at providing means for robots in a multi-agent system to coordinate strategies to optimize multiple properties of their interconnect topology. The main goal is to improve the network topology with regard to connectivity maintenance, robustness to failure, and area coverage. Using the kinematic model in Equation 2, we consider each robot to be controlled by means of a control input defined as the superposition of three different terms:

$$u_i = \sigma u_i^c + \psi u_i^r + \zeta u_i^v \tag{3}$$

 $u_i^c$  is the connectivity maintenance control law;

 $u_i^r$  is the control law improving the robustness of the network to robots' failures;

 $u_i^v$  is the control law improving the area coverage;

 $\sigma, \psi, \zeta$  are control gains—setting them to zero leads to the removal of the effect of the corresponding law.

## A. Connectivity maintenance

In algebraic graph theory, the second-smallest eigenvalue of the Laplacian matrix of a graph  $\mathcal G$  is also called algebraic connectivity  $\lambda_2$  and it reveals whether/how connected the network is [2]. Imposing  $\epsilon > 0$  to be the desired lower-bound for the value of  $\lambda_2$ , we design a control strategy to ensure that  $\lambda_2$  never drops below  $\epsilon$ . As in [25], the following energy function can be used for a decentralized implementation:

$$V(\lambda_2) = \begin{cases} \coth(\lambda_2 - \epsilon) & \text{if } \lambda_2 > \epsilon \\ 0 & \text{otherwise} \end{cases}$$
 (4)

Referring to (2), the  $u_i^c$  control law is defined as follows:

$$u_{i}^{c} = -\frac{\partial V(\lambda_{2})}{\partial p_{i}} = -\frac{\partial V(\lambda_{2})}{\partial \lambda_{2}} \frac{\partial \lambda_{2}}{\partial p_{i}}$$
 (5)

## B. Robustness to robots' failures

A centralized formulation of a graph's robustness was introduced in [29]. Let  $[v_1,\ldots,v_N]$  be the list of nodes ordered by descending value of betweenness-centrality [29]. Let  $\varphi < N$  be the minimum index  $i \in [1,\ldots,N]$  such that, removing nodes  $[v_1,\ldots,v_i]$  leads to disconnecting the graph. Then, the robustness level  $\Theta$  is defined as:

$$\Theta = \frac{\varphi}{N} \tag{6}$$

Our decentralized robustness improvement strategy relies on a metric for estimating the magnitude of the topological vulnerability of a node by means of information acquired from its 1-hop and 2-hops neighbours. The vulnerability level of a node i regarding failures is given by:

$$P_{\theta}(i) = \frac{|Path_{\beta}(i)|}{|\Pi(i)|} \tag{7}$$

where  $|\Pi(i)|$  is the number of i's 1-hop and 2-hops neighbours, and  $|Path_{\beta}(i)|$  is the number of nodes that are exactly at 2-hops from node i and relying on at most  $\beta$  2-hops paths to communicate with i. The purpose of a control strategy is to increase the number of links of a potentially vulnerable node i towards its 2-hop neighbours that are in  $Path_{\beta}(i)$ . Let  $x_{\beta}^{i} \in \mathbb{R}^{m}$  be the barycentre of the positions of the robots in  $Path_{\beta}(i)$ , the control law for robustness improvement is defined as follows:

$$u_i^r = \xi_i \frac{x_{\beta}^i - p_i}{\|x_{\beta}^i - p_i\|} \alpha(t)$$
(8)

where  $\alpha(t) \in \mathbb{R}$  is the linear velocity of the robots. The parameter  $\xi_i$  is introduced to take into account the vulnerability state of a node i— $\xi_i = 1$  if node i identifies itself as vulnerable,  $\xi_i = 0$  otherwise—and it is defined as:

$$\xi_i = \begin{cases} 1 & \text{if } P_{\theta}(i) > r \\ 0 & \text{otherwise} \end{cases} \tag{9}$$

where  $r \in (0,1)$  is a random number drawn from a uniform distribution. It is worth noting that (7) provides a decentralized methodology for each robot to evaluate its vulnerability level. The control law  $u_i^c$  was proven in [25], [30] to guarantee positiveness of the generalized connectivity in a disturbance-free environment.

## C. Voronoi coverage

In general, the coverage problem states that robots should be distributed in the environment in a way that maximizes the total monitored area. Therefore, the efficiency of the control strategy can be directly measured as the portion of the environment that is covered by the mobile robots themselves and the network connectivity. Voronoi tessellations are commonly applied in coverage area problems [17], [31], [32]. A Voronoi tessellation is a subdivision of a plane into cells based on the proximity of a set of points. Let  $P = [p_1, p_2, \ldots, p_n]$  be a set of points in the plane. Define V(i), the Voronoi cell for  $p_i$ , to be the set of points q in the plane that are closer to  $p_i$  than to any other site. Thus, the Voronoi cell for  $p_i$  is defined by

$$V(i) = \{ q \mid ||p_i q|| < ||p_j q||, \forall j \neq i \}$$
 (10)

where  $\|pq\|$  denotes the Euclidean distance between points p and q [33]. Let V(i) be the Voronoi cell corresponding to a robot located at  $p_i$ . A team of N robots at positions  $P = [p_i]_{i=1}^N \in \mathbb{R}^{SN}$  navigate in a bounded polygonal environment  $\Omega \subseteq \mathbb{R}^S$ , where  $\Omega$  is a closed set with the boundary  $\partial \Omega$ . Given a positive density function  $\phi: \Omega \to \mathbb{R} > 0$ , the centroid of V(i) is defined as

$$C_{V_i} = \frac{1}{M_{V_i}} \int_{V_i} x \,\phi(x) \mathrm{d}x \tag{11}$$

where  $M_{V_i}$  is the cell mass [17]:  $M_{V_i} = \int_{V_i} \phi(x) \mathrm{d}x$ . Then, the Voronoi-based approach presented in [17] was adopted. The simple first-order dynamics can be expressed as:

$$u_i^v = \dot{p}_i \propto (C_{V_i} - p_i) \tag{12}$$

The overall control in Equation 3 was validated in simulation in fault-free and fault-prone scenarios using different gain combinations [7]. Results demonstrated the feasibility of having simultaneous controls to achieve more resilient networks able to enhance their sensing area while maintaining the network connectivity. The impact of failures on the network connectivity was minimized by having the robustness improvement control law active. It is also important to emphasize that the coverage mechanism based on Voronoi tessellation was able to produce a more robust topology regarding failures compared to scenarios where only the connectivity is active. Nonetheless, for successive failures the robustness mechanism is essential to avoid fragmentation.

## D. Lennard-Jones coverage

In [6], the control strategy from Equation 3 was implemented and evaluated for the first time in real robots substituting the Voronoi-based coverage contribution with a simpler potential-based diffusion approach. Rather than  $u_i^v$ , the control law exploited contribution  $u_i^{lj}$  defined as:

$$u_i^{lj} = -\iota \sum_{\forall k} \left( \left( \frac{a \cdot \delta^a}{x_{ik}^{a+1}} \right)^a - 2 \cdot \left( \frac{b \cdot \delta}{x_{ik}^{b+1}} \right)^b \right) \tag{13}$$

where  $x_{ik}$  is the distance between robots i, k and parameters  $\iota$  and  $\delta$  represent the depth and distance from the origin

of the potential's minimum, respectively; a and b were set to 4 and 2. The considerations concluding Subsection IV-C suggest that Voronoi-based coverage has the power to outperform this potential-based coverage approach. However, because the two approaches can results in different geometrical configuration at convergence (see Figure 2), one of the objectives of this work is to discover whether they can produce comparable are coverage.

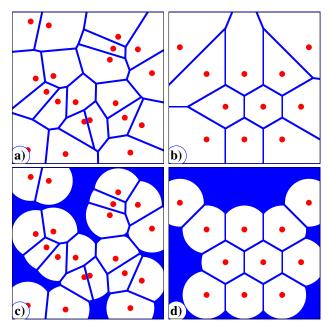


Fig. 2. Voronoi tessellation of a uniform random distribution of points (a) and an incomplete triangular lattice (b); disk coverage of a uniform random distribution of points (c) and an incomplete triangular lattice (d).

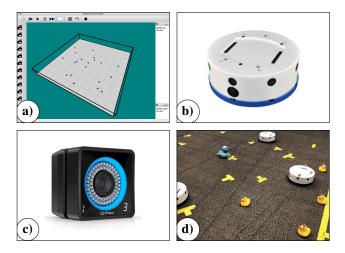


Fig. 3. ARGoS multi-physics simulator (a); K-team Khepera IV robot (b); OptiTrack Prime 13 camera (c); MIST Laboratory's robotic arena (d).

#### V. IMPLEMENTATION AND PORTING TO BUZZ

Coding of the control law described in Section IV was done in Buzz<sup>1</sup>. Buzz [34] is a multi-paradigm scripting

language designed to create composable programs for collections of heterogeneous robots. One of the advantages of using Buzz is the ability to rely on virtual stigmergy [35] for information dissemination. Preliminary simulation and debugging were carried out in the multi-physics environment of ARGoS [36] (see Figures 3-a and 4). Thanks to its virtual machine (VM), Buzz can run on multiple software and hardware platforms, thus, we were able to seamlessly transfer the Buzz code from ARGoS simulator to our robot of choice (i.e., K-team Khepera IV). With regard to the implementation's nitty-gritty, since robots can only use local coordinates, we elected a leader robot to spread the information necessary for all the robots to reason in a virtual common coordinates system. This is effectively done using Dijkstra's algorithm to compute the shortest paths between the leader and every other node. Both Dijkstra's algorithm and Voronoi tessellation have naive implementations running in quadratic time complexity w.r.t. the number of robots  $O(N^2)$  and more sophisticated implementations running in  $O(N \log(N))$  time.

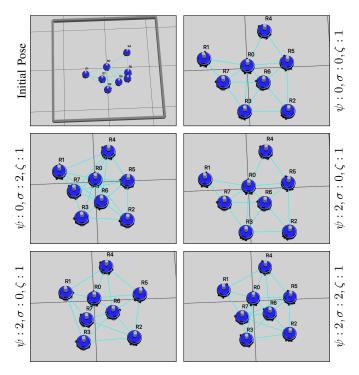


Fig. 4. Final configurations of a multi-robot system comprising eight footbot robots using different combinations of gains for Equation 3. They show the slightly different equilibria entailed by variations in these parameters. All simulations starts from a common initial pose (top-left) in ARGoS.

#### VI. ROBOTIC EXPERIMENTS

Going from simulations to hardware, sensible performance degradation can occur—the so-called "reality gap" [37]. Hence, the importance of actual robotic implementations. Our robot model lies on the assumptions that (i) robots have a limited communication range, (ii) they can only perceive information in their local coordinate systems, and (iii) they can exploit the "situated communication" model [38]. The robotic platform of our experiments is the K-team Khepera

https://github.com/MISTLab/Buzz

	s Sample Standard Deviation	s <sup>2</sup> Variance (Sample Standard)	$\sigma$ Population Standard Deviation	$\sigma^2$ Variance (Population Standard)	N	μ Mean (Average)	$SE_{ar{X}}$ Standard Err. of the Mean	Student's t-test
$\lambda_2$	0.1432075910	0.0205084141	0.1397562985	0.0195318229	21	0.8200303833	0.0312504583	0.29833
	0.4211228537	0.1773444579	0.3898840024	0.1520095353	7	1.0381683971	0.1591694774	3.23000
Θ	0.0396591355	0.0015728470	0.0387033532	0.0014979495	21	0.3842385914	0.0086543328	0.00248
	0.0692027649	0.0047890226	0.0640693107	0.0041048765	7	0.49587592	0.0261561866	0.002.00
Cov.	0.1742475767	0.0303622180	0.1700482229	0.0289163981	21	3.7055112233	0.0380239385	0.75813
0011	0.3807099197	0.1449400429	0.3524688958	0.1242343225	7	3.5969432957	0.1438948241	0.10010
Perf.	0.3851053739	0.1483061490	0.3758243625	0.1412439514	21	2.9907511114	0.0840368822	0.47998
	1.1542405955	1.3322713523	1.0686191433	1.1419468734	7	3.5595331971	0.4362619384	3.2.000

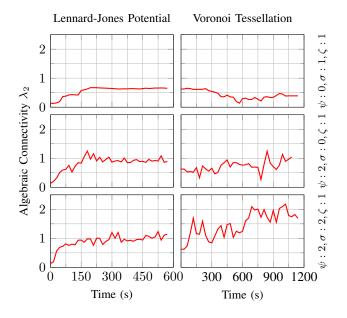
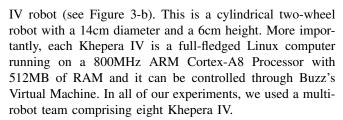


Fig. 5. Evolution of the value of algebraic connectivity  $\lambda_2$  in experiments with eight Khepera IV robots using Lennard-Jones potential-based (left) and Voronoi tessellation-based (right) coverage using different combinations of gains (see the rightmost y-axis) for the control law in Equation 3.



The tracking of the robots' positions is achieved through four OptiTrack Prime 13 cameras (shown in Figure 3-c). The monitored arena (see Figure 3-d) is a 2 meters by 2 meters square. The OptiTrack system captures the x and y positions of the robots, as well as their yaw. This information, in an absolute frame of reference, is then translated into local coordinates before being fed to each Khepera IV. Situated communication is emulated over a Wi-Fi network through blabbermouth<sup>2</sup>. This software accesses the infor-

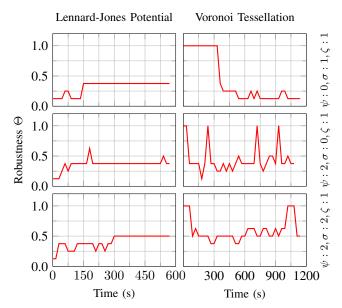


Fig. 6. Evolution of the value of robustness  $\Theta$  in experiments with eight Khepera IV robots using Lennard-Jones potential-based (left) and Voronoi tessellation-based (right) coverage using different combinations of gains (see the rightmost y-axis) for the control law in Equation 3.

mation made available by OptiTrack and distributes it to the robots, respecting the communication range—65cm in our experiments—and visibility constraints to re-create a fully distributed environment. This introduces a simplification, in that robots cannot obstruct each other's field of view.

We selected the most relevant combinations of gains  $(\sigma, \psi, \zeta)$ —whose static [39] and time-varying optimization [6] we studied before—and run over 20 new experiments lasting  $\sim 20'$  each. These experiments were evaluated against four performance metrics, i.e., algebraic connectivity  $\lambda_2$ , robustness  $\Theta$ , area coverage (in  $m^2$ ), and the optimization metric introduced in [6] to find the ideal gains  $\sigma, \psi, \zeta$ :

$$performance = \lambda_2(t)\mathcal{A}(t)$$
 (14)

where  $\lambda_2(t)$  and  $\mathcal{A}(t)$  are the algebraic connectivity and the area coverage at time t, respectively.

<sup>2</sup>https://github.com/MISTLab/blabbermouth

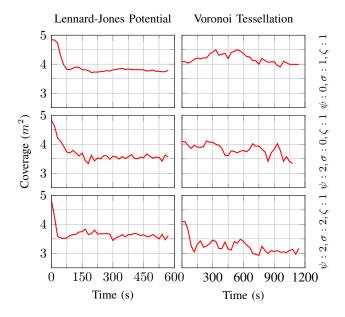


Fig. 7. Evolution of the value of coverage (in  $m^2$ ) in experiments with eight Khepera IV robots using Lennard-Jones potential-based (left) and Voronoi tessellation-based (right) coverage using different combinations of gains (see the rightmost y-axis) for the control law in Equation 3.

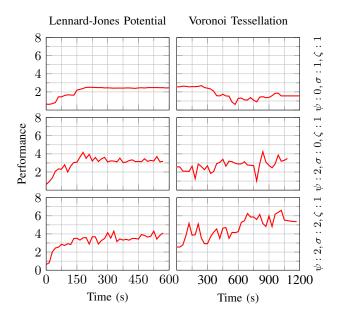


Fig. 8. Evolution of the value of the performance metric in experiments with eight Khepera IV robots using Lennard-Jones potential-based (left) and Voronoi tessellation-based (right) coverage using different combinations of gains (see the rightmost y-axis) for the control law in Equation 3.

## VII. DISCUSSION

A selection of most significant experiment runs is presented in Figures 5 to 9. Cumulative statistics for all the experiments are given in Table I. The figures, as well as the table, also contain an excerpt of the results of [6]. These were obtained using the same control law, gains  $\sigma$ ,  $\psi$ ,  $\zeta$ , and the Lennard-Jones potential-based coverage law in Equation 13.

The results confirm the simulation findings in [7]. One of the advantages of using Voronoi coverage is the improvement of the network robustness (see Figure 6). By increasing

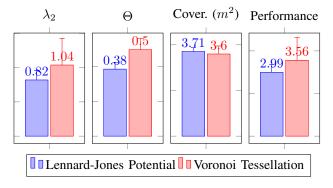


Fig. 9. Sample means  $\mu$  and population standard deviations  $\sigma$  (as error bars) of algebraic connectivity  $\lambda_2$ , robustness  $\Theta$ , coverage (in  $m^2$ ), and performance metric in experiments using Lennard-Jones potential-based (left) and Voronoi tessellation-based (right) coverage.

the coverage gain, the robustness level also improves—yet, Voronoi coverage per se would not be able to accommodate successive failures and this is when the robustness contribution matters. A possible explanation is that Voronoi coverage control, unlike Lennard-Jones coverage, is more gentle towards unevenly spaced configurations. On the other hand, we remarked that Voronoi tesselation-based coverage is sensitive to the way the cells are bounded. With  $\zeta = 1$ , a low  $\boldsymbol{\sigma}$  can lead to a good coverage performance at the expense of the value of  $\lambda_2$  without resulting in loss of connectivity. Another (expected) result is the overt tradeoff between algebraic connectivity and area coverage (see Figures 5 and 7). In fact,  $\sigma = 2$  has a negative impact on the area the robots can cover. We also observe that, with the setup from Section VI,  $\sim 4m^2$  is the coverage upper bound, where the robotic team starts to lose connectivity. With regard to the area coverage performance of the potential-based approach and the Voronoi tessellation-based one, we found that these are comparable—possibly with a slight advantage for the former (see Figure 7). Both connectivity and robustnessespecially the latter-improves when using Voronoi-based coverage instead. In Table I we also report the results of the Student's t-test confirming the statistical significance of the comparisons in Figure 9 for  $\lambda_2$  and  $\Theta$ , while implying that the difference in area coverages is likely inconsequential.

## VIII. CONCLUSIONS AND FUTURE WORK

In this work, we presented the results of the implementation in a real-life multi-robot system—comprising eight K-team Khepera IV robots—of a combined control law for the improvement of area coverage and network robustness that also preserves algebraic connectivity of a robotic team. The control law contribution improving area coverage exploited the Voronoi tessellation of the robots' arena. We compared our results with those of a previous implementation exploiting a different, potential-based approach to area coverage. In Section VII, we explained how our results both substantiate the finding achieved through simulation in [8] and suggest that Voronoi-based coverage outperforms the potential-based coverage in terms of robustness and connectivity with negligible detriment to the explored area.

#### REFERENCES

- [1] M. Brambilla, E. Ferrante, M. Birattari, and M. Dorigo, "Swarm robotics: a review from the swarm engineering perspective," *Swarm Intelligence*, vol. 7, no. 1, pp. 1–41, 2013.
- [2] C. Godsil and G. Royle, Algebraic Graph Theory. Springer, 2001.
- [3] G. Kantor, S. Singh, R. Peterson, D. Rus, A. Das, V. Kumar, G. Pereira, and J. Spletzer, "Distributed search and rescue with robot and sensor teams," in *Field and Service Robotics*. Springer, 2003, pp. 529–538.
- [4] A. Howard, M. J. Matarić, and G. S. Sukhatme, "Mobile sensor network deployment using potential fields: A distributed, scalable solution to the area coverage problem," in *Distributed Autonomous Robotic Systems* 5. Springer, 2002, pp. 299–308.
- [5] D. A. Paley, F. Zhang, and N. E. Leonard, "Cooperative control for ocean sampling: The glider coordinated control system," *IEEE Transactions on Control Systems Technology*, vol. 16, no. 4, pp. 735–744, 2008.
- [6] M. Minelli, M. Kaufmann, J. Panerati, C. Ghedini, G. Beltrame, and L. Sabattini, "Stop, think, and roll: Online gain optimization for resilient multi-robot topologies," in *Proceedings of the International Symposium on Distributed Autonomous Robotic Systems (DARS)*, Boulder, CO, Oct. 2018.
- [7] C. Ghedini, C. H. C. Ribeiro, and L. Sabattini, "A decentralized control strategy for resilient connectivity maintenance in multi-robot systems subject to failures," in *Proceedings of the International Symposium on Distributed Autonomous Robotic Systems (DARS)*, London, UK, nov. 2016.
- [8] C. Ghedini, C. H. Ribeiro, and L. Sabattini, "Toward efficient adaptive ad-hoc multi-robot network topologies," Ad Hoc Networks, vol. 74, pp. 57 – 70, 2018. [Online]. Available: http://www.sciencedirect.com/ science/article/pii/S1570870518300684
- [9] M. Juliá, A. Gil, and O. Reinoso, "A comparison of path planning strategies for autonomous exploration and mapping of unknown environments," *Autonomous Robots*, vol. 33, no. 4, pp. 427–444, 2012.
- [10] K. M. Wurm, C. Stachniss, and W. Burgard, "Coordinated multi-robot exploration using a segmentation of the environment," in *Intelligent Robots and Systems*, 2008. IROS 2008. IEEE/RSJ International Conference on. IEEE, 2008, pp. 1160–1165.
- [11] A. Quattrini Li, R. Cipolleschi, M. Giusto, and F. Amigoni, "A semantically-informed multirobot system for exploration of relevant areas in search and rescue settings," *Autonomous Robots*, vol. 40, no. 4, pp. 581–597, 2016.
- [12] V. Gazi and K. M. Passino, "Stability analysis of swarms," *IEEE Transactions on Automatic Control*, vol. 48, no. 4, pp. 692–697, April 2003.
- [13] N. E. Leonard and E. Fiorelli, "Virtual leaders, artificial potentials and coordinated control of groups," in *Decision and Control*, 2001. Proceedings of the 40th IEEE Conference on, vol. 3. IEEE, 2001, pp. 2968–2973.
- [14] A. Sangwan and R. P. Singh, "Survey on coverage problems in wireless sensor networks," *Wireless Personal Communications*, vol. 80, no. 4, pp. 1475–1500, 2015.
- [15] Q. Du and D. Wang, "The optimal centroidal voronoi tessellations and the gersho's conjecture in the three-dimensional space," *Computers & Mathematics with Applications*, vol. 49, no. 9-10, pp. 1355–1373, 2005.
- [16] J. Cortes, S. Martinez, T. Karatas, and F. Bullo, "Coverage control for mobile sensing networks," *IEEE Transactions on robotics and Automation*, vol. 20, no. 2, pp. 243–255, 2004.
- [17] A. Breitenmoser, M. Schwager, J. C. Metzger, R. Siegwart, and D. Rus, "Voronoi coverage of non-convex environments with a group of networked robots," in 2010 IEEE International Conference on Robotics and Automation, May 2010, pp. 4982–4989.
- [18] Y. Stergiopoulos, M. Thanou, and A. Tzes, "Distributed collaborative coverage-control schemes for non-convex domains," *IEEE Transactions on Automatic Control*, vol. 60, no. 9, pp. 2422–2427, 2015.
- [19] J. Banfi, A. Quattrini Li, I. Rekleitis, F. Amigoni, and N. Basilico, "Strategies for coordinated multirobot exploration with recurrent connectivity constraints," *Autonomous Robots*, vol. 42, no. 4, pp. 875–894, 2018
- [20] Y. Kantaros and M. M. Zavlanos, "Distributed intermittent connectivity control of mobile robot networks," *IEEE Transactions on Automatic Control*, vol. 62, no. 7, pp. 3109–3121, 2017.

- [21] G. A. Hollinger and S. Singh, "Multirobot coordination with periodic connectivity: Theory and experiments," *IEEE Transactions on Robotics*, vol. 28, no. 4, pp. 967–973, Aug 2012.
  [22] M. Ji and M. Egerstedt, "Distributed coordination control of multia-
- [22] M. Ji and M. Egerstedt, "Distributed coordination control of multiagent systems while preserving connectedness," *IEEE Transactions on Robotics*, vol. 23, no. 4, pp. 693–703, 2007.
- [23] A. Ajorlou, A. Momeni, and A. G. Aghdam, "A class of bounded distributed control strategies for connectivity preservation in multiagent systems," *IEEE Transactions on Automatic Control*, vol. 55, no. 12, pp. 2828–2833, 2010.
- [24] A. Gasparri, L. Sabattini, and G. Ulivi, "Bounded control law for global connectivity maintenance in cooperative multi-robot systems," *IEEE Transactions on Robotics*, vol. 33, no. 3, pp. 700–717, June 2017.
- [25] L. Sabattini, N. Chopra, and C. Secchi, "Decentralized connectivity maintenance for cooperative control of mobile robotic systems," *The International Journal of Robotics Research (SAGE)*, vol. 32, no. 12, pp. 1411–1423, October 2013.
- [26] P. Yang, R. A. Freeman, G. J. Gordon, K. M. Lynch, S. S. Srinivasa, and R. Sukthankar, "Decentralized estimation and control of graph connectivity for mobile sensor networks," *Automatica*, vol. 46, no. 2, pp. 390–396, 2010.
- [27] Y. Mao, L. Dou, H. Fang, and J. Chen, "Flocking of multi-robot systems with connectivity maintenance on directed graphs," *Journal* of Systems Engineering and Electronics, vol. 25, no. 3, pp. 470–482, June 2014.
- [28] W. Huang, Y. Wang, X. Yi, and X.-J. Yang, "Distributed coordination with connectivity maintenance for nonholonomic robots," *Computer Animation and Virtual Worlds*, vol. 29, no. 3-4, p. e1833, 2018, e1833 cav.1833. [Online]. Available: https://onlinelibrary.wiley.com/doi/abs/10.1002/cav.1833
- [29] C. Ghedini, C. Secchi, C. H. C. Ribeiro, and L. Sabattini, "Improving robustness in multi-robot networks," in *Proceedings of the IFAC* Symposium on Robot Control (SYROCO), Salvador, Brazil, aug. 2015.
- [30] P. Robuffo Giordano, A. Franchi, C. Secchi, and H. H. Bülthoff, "A passivity-based decentralized strategy for generalized connectivity maintenance," *The International Journal of Robotics Research*, vol. 32, no. 3, pp. 299–323, 2013.
- [31] A. Gusrialdi, T. Hatanaka, and M. Fujita, "Coverage control for mobile networks with limited-range anisotropic sensors," in *Decision and Control*, 2008. CDC 2008. 47th IEEE Conference on, Dec 2008, pp. 4263–4268.
- [32] J. Stergiopoulos and A. Tzes, "Voronoi-based coverage optimization for mobile networks with limited sensing range - a directional search approach," in 2009 American Control Conference, June 2009, pp. 2642–2647.
- [33] D. M. Mount, "Computational geometry," *Dept. of Computer Science University of Maryland*, 2005.
- [34] C. Pinciroli and G. Beltrame, "Buzz: An extensible programming language for heterogeneous swarm robotics," in *Proceedings of the IEEE/RSJ IROS 2016*. Los Alamitos, CA: IEEE Computer Society Press, Oct. 2016.
- [35] C. Pinciroli, A. Lee-Brown, and G. Beltrame, "A tuple space for data sharing in robot swarms," in proceedings of the 9th EAI International Conference on Bio-inspired Information and Communications Technologies. ICST, 2016, pp. 287–294.
- [36] C. Pinciroli, V. Trianni, R. O'Grady, G. Pini, A. Brutschy, M. Brambilla, N. Mathews, E. Ferrante, G. Di Caro, F. Ducatelle, M. Birattari, L. M. Gambardella, and M. Dorigo, "Argos: a modular, parallel, multiengine simulator for multi-robot systems," *Swarm Intelligence*, vol. 6, no. 4, pp. 271–295, 2012.
- [37] J. Panerati, L. Gianoli, C. Pinciroli, A. Shabah, G. Nicolescu, and G. Beltrame, "From swarms to stars: Task coverage in robot swarms with connectivity constraints," in 2018 IEEE International Conference on Robotics and Automation (ICRA), May 2018.
- [38] K. Støy, "Using situated communication in distributed autonomous mobile robotics," in *Proceedings of the Seventh Scandinavian Con*ference on Artificial Intelligence, ser. SCAI '01. Amsterdam, The Netherlands, The Netherlands: IOS Press, 2001, pp. 44–52.
- [39] J. Panerati, M. Minelli, C. Ghedini, L. Meyer, M. Kaufmann, L. Sabattini, and G. Beltrame, "Robust connectivity maintenance for fallible robots," *Autonomous Robots*, Nov 2018. [Online]. Available: https://doi.org/10.1007/s10514-018-9812-8