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1

Random Telegraph Noise in Resistive Random Access Memories: Compact Modeling and Advanced Circuit Design

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Abstract— In this work we report about the derivation of a physics-based compact model of Random Telegraph Noise (RTN) in HfO2-based Resistive Random Access Memory (RRAM) devices. Starting from the physics of charge transport, which is different in the high and low resistive states (HRS and LRS), we explore the mechanisms responsible for RTN exploiting a hybrid approach, based on self-consistent physics simulations and geometrical simplifications. Then, we develop a simple yet effective physics-based compact model of RTN valid in both states, which can be steadily integrated in state-of-the-art RRAM compact models. The RTN compact model predictions are validated by comparison with both a large experimental dataset obtained by measuring RRAM devices in different conditions, and data reported in the literature. In addition, we show how the model enables advanced circuit simulations by exploring three different circuits for memory, security, and logic applications.

Index Terms—RRAM; RTN; HRS; LRS; Compact Model; Variability; PUF; RNG; Verilog-A; Circuit Design

I. INTRODUCTION

HE relentless scaling of Complementary Metal Oxide Semiconductor (CMOS) technology is increasing the importance of phenomena associated with charge trapping/detrapping at discrete defect sites (either pre-existing in the virgin device or induced by stress), such as Stress-Induced Leakage Current (SILC) [1-3], Bias Temperature Instability (BTI) [4-6], and Random Telegraph Noise (RTN) [7-10]. Particularly, RTN represents a major reliability issue for conventional devices such as MOS transistors and their evolutions (e.g. FinFETs, GAA) [11-12], and for emerging devices such as the Resistive Random Access Memory (RRAM) [9-10]. In fact, RTN variability in RRAM can be wide enough to significantly shrink the read margin [9-10], especially in devices operated at low current levels for lowpower circuits. As RRAM technology is approaching the industrial stage, RTN mechanisms must be understood [7-10] and, possibly, mastered. This is essential to evaluate the technology potential and limitations for specific applications such as non-volatile memory (NVM) [13-16], neuromorphic computing [17-20], Physical Unclonable Function (PUF), and Random Number Generator (RNG) [21-23]. For instance, RTN effects are detrimental in multi-level NVM applications, reducing the read margin between adjacent bit distributions. RTN is an issue in neuromorphic circuits, in which it causes temporary and unpredictable random variations of the synaptic weight associated with the device. In addition, RNGs and PUFs performances can be adversely affected by RTN, worsening their figures of merit (e.g., randomness). Nevertheless, it has been suggested [24-25] to exploit the intrinsic randomness of RTN as an entropy source to realize RTN-based PUFs and RNGs, which could open new interesting perspectives. Finally, RRAM-based temperature sensors that exploit RTN have been proposed [26]. From the circuit designer perspective, it is therefore imperative to include RTN effects into RRAM models. Few attempts can be counted in the literature [27-30], and they typically address the phenomenon only in one of the two resistive states, i.e., either High- (HRS), or Low-Resistive State (LRS). Recently, we proposed a compact model for RTN in RRAM, valid in both resistive states, that correctly captures the statistics of the RTN properties (i.e., variations in amplitude and transition times) and the variability in the number of defects contributing to the RTN [31]. This model, implemented in Verilog-A, can be easily plugged in existing RRAM device models [13, 32-36], extending their potential. In this paper, we extend the work in [31] by including the details of the approach used to derive the compact model of RTN in HRS and LRS. In addition, we show how the proposed model enables: i) estimating the effect of RTN on the resistive states distribution; ii) evaluating how the randomness of a RRAM-based PUF circuit is affected by the presence of RTN; iii) designing the building block of an advanced RTN-based RNG circuit.

II. DEVICES, EXPERIMENTS, AND SIMULATIONS

A. Devices and Experiments

TiN/Ti/HfO₂/TiN RRAMs with a 5 nm thick HfO₂ layer are measured under different operating conditions [read voltage (V_{READ}), reset voltage (V_{RESET}), temperature (T), current compliance (I_C)] (Fig. 1). After forming, each device is switched from the LRS to the HRS and back to the LRS 100 times and RTN is measured in both HRS and LRS at each cycle applying V_{READ} . This results in a wide dataset where the

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Voltage (V)

Fig. 1 – (a) Schematic picture of the device and (b-c) of the RTN mechanism in HRS, showing the defects (b) de-activation and (c) activation. Coordinates (x-y-z), barrier thickness (t_b), and CF thickness (t_{co}), are reported. (d) Schematic picture of the RTN mechanism in LRS, showing the electrostatic coupling between a charged defect and the conductive filament. (e) Experimental I-V curves measured at 20 consecutive switching cycles on a TiN/Ti/HfO₂/TiN device using I_c =50µA and V_{RESET} =1.2V, displaying cycle-to-cycle variability. V_{RESET} , (i.e. the maximum absolute value of the voltage during the reset sweep), I_c , and V_{READ} are highlighted. Insets in (e) show a two-level RTN, related to a single trap, as detected in HRS (left) and in LRS (right). In the left plot, the statistical RTN parameters are evidenced [(i.e., the average capture time ($\overline{\tau_e}$), the average emission time ($\overline{\tau_e}$), the fluctuation amplitude, (ΔI)].

effects of RTN fluctuations are superimposed to the device-todevice and cycling variability. All the experiments are performed with a Keithley 4200-SCS, with the temperature being controlled by a dedicated thermo-chuck. The analysis of the RTN signals is performed by means of the Factorial Hidden Markov Model (FHMM) [37-38]. This statistical method allows decomposing the multi-level RTN signal into a superposition of two-level signals (i.e., components), each attributed to the activity of an individual defect. This allows correctly estimating the properties of each component from the complex multi-level RTN signal. These properties [i.e., the fluctuation amplitude (ΔI), the average capture ($\overline{\tau_c}$) and average emission ($\overline{\tau_e}$) times (inset of Fig. 1(e))] can be linked to the physical properties of the associated defect.

B. Simulations

Charge transport and RTN fluctuations are simulated using MDLab's Ginestra software [39], which accounts for the 3-D potential and temperature maps in the whole RRAM device, as well as the direct and the multi-phonon trap-assisted tunneling (DT and MP-TAT, respectively) charge transport [40]. The lattice relaxation and the electron-phonon coupling associated with the charge trapping at defect sites are also included. This

allows accounting for the atomic rearrangement around the defect occurring upon the charge trapping that strongly affects the charge trapping and de-trapping rates and the localized power dissipation at the defect site [40].

III. CHARGE TRANSPORT IN HFO2 RRAM

Developing a compact model for RRAM devices that includes the effects of RTN requires understanding the physical mechanisms dominating charge transport in the two resistive states. Indeed, in general, the RTN is a temporary alteration of the current flow [41], determined by different physical mechanisms in HRS and LRS [30, 41-42]. Therefore, it is mandatory to discuss the charge transport mechanism and its alterations separately for the two states.

A. Charge Transport in LRS

In LRS, the device is characterized by the presence of a full conductive filament (CF) shunting the two electrodes (Fig. 1d). It is accepted that the CF, created during the preliminary forming operation, is formed by tightly packed oxygen vacancy defects, and its size is controlled by the current compliance, I_c , used in the forming and set operations [30-36, 42]. In this resistive state, charge transport is due to drift of de-localized electrons drift in the CF [30-36, 42], consistently with the ohmic-like behavior generally observed in LRS. This charge transport mode is due to the nature of the CF, associated with the formation of a conductive sub-band [42].

B. Charge Transport in HRS

The reset operation, driving the device in HRS, leads to the partial re-oxidation of the CF, creating a dielectric barrier [30-36, 42], as shown in Fig. 1(a-b-c). The dielectric barrier thickness (t_b) is determined by the reset conditions (Fig. 1), i.e., V_{RESET} , and T. The HRS current is dominated by the electron MP-TAT at positively charged oxygen vacancy defects (Vo^+) in the re-oxidized tip of the CF (dielectric barrier in Fig. 1(a-b-c)) [32-33, 40-42].

IV. THE RANDOM TELEGRAPH NOISE MODEL

A complete RTN compact model must capture the inherent variability in the number of defects contributing to the RTN and in their statistical properties (ΔI , τ_c , τ_e). These all depend on the operating conditions and on the physical state of the device (i.e. HRS or LRS). In the following, we show how these features can be implemented in the model.

A. RTN Amplitude Statistical Model in HRS

The physical mechanism responsible for RTN in HRS is still under debate [43-46], but it is widely believed that is due to the temporary (de-)activation of Vo^+ defects, distributed in the barrier, assisting charge transport [29-30, 43, 46], as sketched in Fig. 1(b-c). The mechanisms leading to (de-)activation is also due to charge (de-)trapping in additional slow defects that do not participate to charge transport (supposedly oxygen interstitial atoms) [29-30, 43]. To gain further insights, we perform physics-based simulations of charge transport across a $10x10-nm^2$ defect-rich HfO₂ dielectric barrier with TiN electrodes (Fig. 2). Simulations are performed considering different applied voltage, barrier



Fig. 2 – Simulation of charge transport in a 10x10 nm² barrier. Projection of the 3D defects distribution on the x-z plane, see Fig. 1. Vo^+ defects (black squares) are randomly distributed in the barrier with a density of $N_T = 2 \cdot 10^{21}$ cm⁻³ [29-30, 43, 47]. Few Vo^+ defects (violet circles) in the middle of the barrier (±0.2 nm) assist >95% of the total current, regardless of the operating conditions. (a-b-c) $t_b = 0.5$ nm – 1.0 nm – 1.5 nm at $V_{READ} = 100$ mV and T = 25 °C. (d-e-f) $t_b = 1.5$ nm at $V_{READ} = 50$ mV – 100 mV and T = 25 °C.



Fig. 3 – Distribution of simulated $\Delta I/I$ in HRS obtained using kinetic Monte-Carlo simulations. The I-time traces related to a 10x10 nm² MIM device with TiN electrodes with a 1.0nm-thick barrier are simulated, including the effect of Vo^+ defects activation and de-activation. Vo^+ are randomly distributed in the barrier with a density of $N_T=2\cdot10^{21}$ cm⁻³ [29-30, 43, 47]. Simulations are performed in different conditions (V_{READ} , t_b , and T) and are repeated on 10 different device realizations by randomizing defects positions and energies (a total of 40 simulation runs). $\Delta I/I$ distribution is insensitive to operating conditions in agreement with experimental reports [29-30, 43]. Its statistical properties (μ and σ , with related uncertainties) are reported in the figure.

thickness, and temperature values. The presence of defects and of the trapped charge is self-consistently accounted for as described in Section II-B. For each simulation, we consider randomly distributed defects (using uniform spatial and energetic distributions [40]), and we estimate the $\Delta I/I_{HRS}$ by de-activating an individual, randomly selected, defect. In this context, ΔI is defined as the current contribution given by an individual Vo⁺ defect when active [29-30] (Fig. 1(b-c)), while the overall current, I, is the sum of all the current contributions. It is evident from Fig. 2 that a small fraction (violet circles) of all the Vo^+ defects in the barrier (black squares) is responsible for almost the whole HRS current (i.e., > 95 %), regardless of t_b (determined by reset conditions), V_{READ} , and T. This is because the current assisted by a defect is maximized when the defect has small and comparable $\overline{\tau_c}$ and $\overline{\tau_e}$, which is likely for the defects in the middle of the barrier. As such, since RTN is due to the random (de-)activation of these defects, the average $\Delta I/I_{HRS}$ (or equivalently $\Delta R/R_{HRS}$) is expected to be constant in every operating condition. Moreover, due to the random nature of the defects (de)activation, it is unlikely for the defects to be simultaneously all active or inactive, suggesting an average $\Delta I/I_{HRS} < 1$. Naturally, if an individual defect experiencing activation and de-activation drives more than half of the overall current (when active), then it will be possible for $\Delta I/I_{HRS}$ to be > 1. Devising a simple average formulation for the RTN amplitude in HRS requires estimating the average ΔI related to the (de-)activation of an individual defect, which strongly depends on the defect location, energy, cross-section, as well as on the local voltage and temperature profiles. Results are reported in Fig. 3, where the probability distribution of the resulting $\Delta I/I_{HRS}$ appears lognormal and invariant with operating conditions, in agreement with previous experimental reports [29-30, 43]. This lets writing:

$$M\left(\frac{\Delta R}{R}_{HRS}\right) \cong \frac{1}{2} \qquad \sigma\left(\frac{\Delta R}{R}_{HRS}\right) \cong 0.6$$
 (1)

Hence, despite the significant intrinsic variability and the complexity of the RTN mechanism, it is possible to conceive a simple statistical description of RTN fluctuations amplitude in HRS in every operating condition.

B. RTN Amplitude Statistics Model in LRS

In LRS, RTN is commonly attributed to electron trapping and de-trapping at individual defect sites in the proximity of the CF [i.e. within one electron Debye length (λ)] [44, 48-50]. The trapped charge perturbs the potential in its surroundings causing a screening effect on the portion of the CF close to the defect, which induces a resistance change (Figs. 1(d) and 4). As opposite to the HRS, the relative resistance change $(\Delta R/R_{LRS})$ depends on the CF geometry, i.e. its radius (r_{CF}) (assuming a cylindrical CF), and its thickness (t_{ox}) . For a large CF (i.e. $r_{CF} \gg \lambda$) the CF screened section is much smaller than the CF area, $S_{CF} = \pi r_{CF}^2$, causing a relatively small resistance change [44, 48-50]. As the CF gets smaller, the screened portion of the CF gets comparatively wider, with a larger impact on the average relative resistance (or, equivalently, current) change, as also reported in the literature [44, 48-50]. However, while the average effect is dependent on the CF size, the deviations from the average are CF-size independent, as they only depend on the distance between the defect and the CF edge. This results in the lognormal $\Delta I/I_{LRS}$ distribution having a slope, i.e., σ , of about 0.3 [44] that is invariant with the CF size (in turn controlled by I_C) [32-36]. Conversely, the median $\Delta I/I_{LRS}$ value changes with the CF size:

$$M\left(\frac{\Delta R}{R}_{LRS}\right) = f(S_{CF}) \qquad \sigma\left(\frac{\Delta R}{R}_{HRS}\right) \cong 0.3$$
 (2)

Therefore, once the relation between S_{CF} and the median $\Delta I/I_{LRS}$ is found, it is possible to estimate the ΔI of any RTN current fluctuation regardless of the resistive state and the operating conditions. For this reason, we will focus on the description of $f(S_{CF})$. To this point, performing physics-based simulations in LRS would result in a huge computational burden due to the presence of the full CF. Instead we exploit the CF geometry to calculate the relative resistance change $\Delta R/R_{LRS}$ induced in the CF by a charge trapped at a close defect site. Still, $\Delta R/R_{LRS}$ depends on many variables: i) the distance between the defect and the CF edge; ii) the local CF cross-section and its composition; iii) the effective screening



Fig. 4 – Schematic of RTN mechanism in LRS. Defects close to the CF ($r < \lambda$) cause a screening effect on a portion of the CF, inducing a resistance change. (a) No screening ($r > \lambda$). (b) Screening on a wide-area CF. (c) Simplified geometrical framework with (d) its top view and (e) its front view.

length of an electron in a complex medium; iv) the coupling between the electric field of the trapped electron and a portion of the CF. Therefore, a compact formulation can be obtained only by introducing some reasonable simplifying assumptions. We assume an ohmic-like charge transport in the CF, justified by the linear I-V relation typically observed in LRS (Fig. 1(e)), and a uniform CF composition, i.e., a constant CF resistivity (ρ_{CF}) in space. In addition, we consider the CF geometrically uniform (i.e., a prism-shaped CF with arbitrary base profile). Though the exact shape of the CF is currently under debate in the scientific community, this assumption is extremely useful in easing calculations and is frequently adopted [32-36]. To simplify the problem, here we assume an individual defect site placed at the edge of the CF (i.e. we assume zero distance between the defect and the CF edge), as shown in Fig. 4. This defect site, when filled with an electron, exhibits the maximum screening effect on the CF. Moreover, we consider that the trapped charge produces uniform screening in a spherical region around itself, and no screening beyond this region. In addition, we consider the screened portion of the CF to be completely unavailable to charge transport (i.e. we consider its resistance to be infinite). The full CF resistance with no screening effect, (R_{LRS}) , and the relative resistance change induced in the CF by the trapped charge $(\Delta R/R_{LRS})$, can be written as:

$$R_{LRS} = \frac{\rho_{CF} \cdot t_{ox}}{S_{CF}} \qquad \frac{\Delta R}{R}_{LRS} = \frac{R_{LRS}^* - R_{LRS}}{R_{LRS}}$$
(3)

where R_{LRS}^{*} is the resistance of the CF when the screening effect occurs. In the case of a cylindrical filament, calculating this term is complex, as it requires two difficult steps. The first requires calculating the intersection volume between a cylinder (i.e., the CF) and a sphere (i.e., the electric field of the trapped charge). This can be accomplished by using an analytic expression that requires solving numerically elliptic integrals [51], which makes its implementation tedious. The second is the calculation of the resistance of an irregular 3D structure, which may require numerical techniques. Here, to simplify calculations (Fig. 4(c-d-e)), we consider the CF to be a prism with a square base and cross-section S_{CF} , i.e., side r_{CF} . This allows rewriting eq. (3) as $R_{LRS} = \rho_{CF} \cdot t_{ox} / r_{CF}^2$. In addition, we simplify the spherical electric field of the trapped charge to a cube with side r_t , a parameter accounting for the effective screening length of the trapped charge in this

simplified framework, related to λ [44, 48-50]. It is worth noting that r_t can be used as a fitting parameter, effectively compensating for the assumption of zero distance between the CF and the trapped charge. Under these conditions, the $\Delta R/R_{LRS}$ in eq. (3) can be written in terms of r_t and of the CF properties (t_{ax} , r_{CF} , ρ_{CF}):

$$\frac{\Delta R}{R_{LRS}} = \frac{\left[\frac{\rho_{CF} \cdot (t_{ox} - r_t)}{r_{CF}^2} + \frac{\rho_{CF} \cdot r_t}{r_{CF}^2 - \frac{r_t^2}{2}}\right] - \frac{\rho_{CF} \cdot t_{ox}}{r_{CF}^2}}{\frac{\rho_{CF} \cdot t_{ox}}{r_{CF}^2}}$$
(4)

Some mathematical operations allow rewriting eq. (4) as:

$$\frac{\Delta R}{R}_{LRS} = \frac{r_t^3}{2t_{ox} \cdot \left(r_{CF}^2 - \frac{r_t^2}{2}\right)} \cong \frac{r_t^3}{2t_{ox} \cdot r_{CF}^2} = \frac{r_t^3}{2t_{ox} \cdot S_{CF}} \quad (5)$$

which is the formula to estimate the relative resistance change (or equivalently, relative current change, $\Delta I/I_{LRS}$) induced in the CF by a trapped charge at a close defect site. In the last passage, $r_{CF}^2 \gg r_t^2/2$ was assumed.

C. RTN Capture and Emission Times

The complete statistical model for the RTN fluctuation amplitude developed so far must be accompanied by a model to estimate $\tau_{c,e}$ of each defect contributing to the RTN. This is necessary to reproduce the RTN signals over time, allowing transient simulations to be performed with the proposed compact model. Since the physical mechanism causing RTN is associated with charge (de-)trapping in both resistive states, we calculate for each defect the related $\overline{\tau_c}$ and $\overline{\tau_e}$ using the MP-TAT compact formalism adopted in [30-31, 52]. These formulae, described in [52], require defining V, T, and the defect distance from the electrodes (d). In turn, the latter is determined by the defect vertical position within the dielectric barrier when the device is in HRS, or alongside the CF within the whole insulating layer when the device is in LRS). Since charge carriers can be captured from (and emitted to) either the top or the bottom electrodes, $\overline{\tau_c}$ and $\overline{\tau_e}$ are calculated for both cases (two possible capture and two possible emission processes), and the minimum value is considered, as it is representative of the most likely event between the two. In

$$\tau_c \propto e^{\left(\frac{d}{\lambda_c}\right)} e^{\left(\frac{E_c(V)}{kT}\right)}; \ \tau_e \propto e^{\left(\frac{d}{\lambda_e}\right)} e^{\left(\frac{E_e}{kT}\right)} \tag{6}$$

addition, it is necessary to specify a few defect properties (e.g., thermal ionization energy, relaxation energy) effectively lumped in the typical capture (λ_c) and typical emission (λ_e) lengths, and the capture (E_c) and emission (E_e) activation energies that only depend on the defect typology [30-31, 40, 52] (mainly oxygen ions in HRS and Vo^+ in LRS). These parameters are calculated exploiting ab-initio calculations (i.e. Density Functional Theory or Molecular Dynamics), see [30-31, 40, 52] and references within.

D. Model Validation and Implementation

The compact model proposed here has been validated by comparison with an extensive experimental dataset (Fig. 5). Five devices with a 5 nm HfO₂ layer were formed at different I_C values (ranging from 40 μ A to 150 μ A), and then cycled through HRS and LRS for 100 times to collect RTN data in



Fig. 5 – Experimental $\Delta I/I$ vs. *I* (symbols) in HRS (left) and LRS (right) at different operating conditions (*Ic*, *V*_{RESET}, *T*) for five devices (different symbols) with a 5nm HfO₂ layer. Model predictions (dashed lines) are in excellent agreement with real data. The extracted σ values of the normal distributions associated with the lognormal $\Delta I/I$ distributions in HRS and LRS agree with the values extracted from simulations and used in the compact model (the $\pm 3\sigma$ predictions plotted as $\Delta R/R$ vs. *R* (dashed line) agree with RTN data in HRS and LRS taken from the literature (symbols) [41, 44-45]. Data from devices based on different materials (i.e. NiO and Cu) are also reported, showing a good agreement with the model predictions.

both resistive states, also accounting for the effects of cycleto-cycle and device-to-device variability, see Section II-A. In addition, the experiment was repeated for all devices at different V_{RESET} and T. The experimental $\Delta I/I$ vs. I scatter plot is reported in Fig. 5 along with the compact model prediction, which is found to be in excellent agreement with experimental data. The extracted σ values of the $\Delta I/I$ distributions in HRS and LRS agree with the values extracted from simulations and used in the compact model. This is further confirmed by the fact that almost the entire experimental dataset falls within the $\pm 3\sigma$ predictions reported as grey dashed lines in Fig. 5. Moreover, the compact model prediction is also in excellent agreement with data taken from recent literature for HfO₂ RRAM and for devices made of different materials (e.g. Cu and NiO RRAM) [41, 44-45]. This is consistent with the compact model not depending on the CF resistivity, and suggests that the same (or a similar) RTN mechanism may hold for devices employing different materials. In this respect, it is noteworthy that r_t can be used, with the other parameters unchanged, to compare the "strength" of the RTN in LRS in RRAM devices made of different materials. The r_t value used in our simulations is $r_t \approx 1.7$ nm, comparable to λ [48]. Moreover, reproducing the $\Delta I/I$ vs. I curves allows estimating ρ_{CF} from eq. (3-5), which assumes a value of $\approx 10 \text{ k}\Omega \cdot \text{nm}$, in agreement with values reported in the literature [30, 42-43]. In addition, the inherent ability to deal with multiple defects allows the model to reproduce the 1/f noise resulting from the superposition of many RTN signals [28, 30, 43].

The compact model proposed here can be effortlessly integrated into existing RRAM device compact models [32-36], as it requires very few inputs that are easily provided by compact device models, i.e. t_{ax} , the device resistance (*R*), *V*, *T*, the current simulation time, *t*, S_{CF} , and t_b (Fig. 1). The algorithm has been implemented in Verilog-A, and tested



Fig. 6 – Simulations of resistance switching and RTN readout in HRS and LRS. An RRAM with $R_{LRS} \approx 15 \text{ k}\Omega$ is considered. The compact device model used in this simulation [32-33] has been extended with the RTN module. The voltage waveform in (a) is applied to perform the reset ($V_{RESET} = 1 \text{ V}$), the set ($V_{SET} = 1.5 \text{ V}$), and the readout operation ($V_{READ} = 100 \text{ mV}$) for two consecutive cycles. The readout current (b) shows RTN signals in both states, zoomed in (c-f). The cycle-to-cycle variability of RTN is correctly accounted for, as highlighted by the different RTN patterns obtained in the same resistive states in two consecutive cycles.

using an existing RRAM device model [32-33], extended with the proposed RTN model. The results of RTN readout simulations in HRS and LRS are reported in Fig. 6. The details of its implementation are described in details elsewhere [31].

V. APPLICATIONS AND CIRCUIT DESIGN

The proposed model allows considering the presence of RTN in circuit simulations, which is advantageous in the design of circuits for many applications. Here we discuss some examples: a) RTN-aware design of RRAM memory circuits and b) PUFs, c) design of RTN-based RNGs.

A. RTN-aware Design of Multi-bit Memory Circuits

In the design of a RRAM array for memory application, it is imperative to guarantee an adequate margin between adjacent bit distributions. Nevertheless, the presence of RTN reduces the read margin between neighboring distributions, especially if fast read operation is required (i.e., zero or small averaging time). Therefore, a compact model that can account for the effects of RTN is highly desirable, especially for the design of multi-bit cell arrays. This is clarified in Fig. 7, where we report the comparison between simulations that include and exclude the effects of RTN, respectively. We simulated 100 full switching cycles of an individual cell, repeating the simulation for two different VRESET values, namely 1.0 V and 1.6 V. This allows building the HRS resistance distributions, accounting for the cycling variability. The read current is detected at each cycle by applying $V_{READ} = 100 \text{ mV}$ using an averaging time of 100 µs. Regardless of the reset condition, the distribution with RTN is clearly more stretched than the one without RTN. Tail states appear due to RTN fluctuations, which can be detrimental for multi-bit memory applications as they reduce the margin between adjacent bit distributions, potentially leading to read failures. In the example of Fig. 7, simulations not accounting for the RTN would predict a tiny but non-zero margin between the two obtained distributions using $V_{RESET} = 1.0$ V and $V_{RESET} = 1.6$ V. Nevertheless, our



Fig. 7 – HRS resistance (read at $V_{READ} = 100$ mV) distributions obtained by cycling an individual cell 100 times with (red symbols) and without (black symbols) RTN, for $V_{RESET} = 1.0$ V (circles) and 1.6 V (squares). The presence of RTN broadens the resistance distribution and results in tail states as well as deviations from a pure lognormal trend.

simulations show that these two reset conditions cannot be safely assigned to two distinct logic states due to their RTNinduced overlap, which would lead to failures. This effectively reduces the number of bits that can be stored in a cell.

B. The impact of RTN on a 128-bit RRAM-based PUF

The stochastic behavior and intrinsic variability of RRAM devices can be exploited to realize PUF circuits for hardware security [21-23] (Fig. 8(a)). The performance of RRAM-based PUF circuits strongly depends on RRAM reliability, severely affected by noise issues and read instabilities [23]. This is particularly true when HRS is chosen to implement PUF because of the wider resistance distribution and of the lower power consumption than in LRS [23]. Consequently, it is important to deploy compact models able to evaluate the performance of PUF circuits in the presence of RTN. The effect of RTN on the performance of a 128-bit RRAM-based PUF is here investigated briefly. Initially, an individual cell is instantiated in LRS, with $I_C = 100 \ \mu$ A. Then the cell is cycled 100 times between HRS and LRS, using a 1 ms ramped voltage down to -1.7V for the reset operation. When the cell is in the HRS, the current at $V_{READ} = 100$ mV is detected, allowing the estimation of the median value of the current in HRS that will serve as reference. A 128-bit PUF circuit is then instantiated and all the devices are initially set to the LRS, and then driven to the HRS. The information related to the resistive state of the 128-bit string of devices is then digitized by comparing each device's current with the reference one. Obviously, when the RTN is not considered, the read current is constant over time but it may strongly vary over time when RTN is considered. Therefore, the detected value of the read current depends on the adopted reading scheme (Fig. 8(b)). In this work, we evaluated the performance of the PUF circuit and the effect of RTN performing the read operation with two different averaging time values, 1 s and 100 µs, respectively. The randomness of the PUF circuit (i.e., the percentage of logic "0"s or "1"s in the response) is assessed for 100 responses. Simulations without considering RTN (Fig. 8(c,d)), result in a randomness distribution centered almost at 50%, as expected [21-23]. Nevertheless, when the effect of RTN is considered, the randomness distribution may be significantly shifted, depending on the reading scheme. A long averaging time (e.g., 1 s) reduces the probability of bit flipping, smearing out the effect of wide RTN fluctuations (Fig. 8(c)).



Fig. 8 – (a) Schematic of the 1T1R cells implemented in PUF matrix. (b) Simulated RTN waveform in HRS (blue line – sampled at 100 μ s), showing multi-level fluctuations, and its value averaged over 1 s (red line). (c-d) Randomness distributions with (red) and without (grey) the effect of RTN considering an averaging time during readout of (c) 1 s and (d) 100 μ s.

Conversely, when a short averaging time of 100 μ s is selected, the average of the randomness distribution is found at about 42%, limiting the reliability of the PUF circuit (Fig. 8(d)). In this framework, the compact model can be used to select the best reading scheme by trading-off the impact of RTN with time and power constraints. Still, advanced phenomena not yet included in the model such as defect volatility and anomalous RTN [46] could affect the performance of PUFs as well. These features will be included in future extensions of the model.

C. Design of an RTN-based RNG Circuit

Recently, the presence of RTN signals in RRAM devices has drawn attention, as their inherent randomness can be exploited as a possible source of entropy for RNG circuits [24-25]. Nevertheless, a proper design of such circuits can be attained only by introducing suitable compact models, as the one proposed in this work. The circuit topology we explore (Fig. 9(a)) finds implementation in high reliability systems for the generation of truly random numbers [24]. The circuit, composed of the RRAM device in HRS and a series transistor, a buffer with a high-pass filter, and a Schmitt trigger, has been implement in Cadence Virtuoso[™]. We included an RRAM device initialized in HRS, with $t_b = 1$ nm. The compact device model used here [32-33] has been extended with the proposed compact RTN model. The results of a transient simulation are shown in Fig. 9(b-c). The application of a constant voltage, V_{READ} , to the top electrode of the RRAM causes voltage RTN fluctuations to appear at the buffer input (Fig. 9(b)). The RTN pattern is transferred to the high-pass filter (to get rid of unwanted DC and low frequency components) and is fed to the Schmitt trigger. The reference voltage V_{REF} regulates the amount of hysteresis that the comparator can withstand. The randomness in the RTN signal produces a random bit stream at the output of the comparator (Fig. 9(c)), achieving a noteworthy randomness value of nearly 50%. The output voltage can be fed to analog-to-digital converters for further processing. The simulation of this circuit topology shows the



Fig. 9 – (a) Schematic of the Random Number Generator circuit based on the RTN in the RRAM device. A device in HRS with $t_b = 1$ nm is considered. The compact device model used here is found in [32-33] and has been extended with the proposed RTN module. (b) RTN voltage fluctuations as detected at the transistor drain terminal. (c) The random RTN pattern is reproduced at the circuit output, giving a random stream with an excellent randomness (50.8%).

potential of the proposed model for advanced circuit design. For instance, the model can be used to estimate the best operating conditions for the RRAM device to optimize the randomness and the uniqueness of the output bit stream.

VI. CONCLUSIONS

In this paper, we developed a physics-based compact model for RTN in RRAM, valid in both HRS and LRS, by combining refined physics-based simulations with reasonable geometrical simplifications. The model correctly considers the complex physical mechanisms at the basis of RTN in both resistive states. Its predictions are validated on a wide experimental dataset retrieved by measuring many devices in different conditions. Moreover, the model successfully captures the trends reported in the literature by other research groups. The RTN model can be seamlessly integrated into RRAM compact models. The potential of the model as a tool for advanced circuit design is clarified by showing how it can be used to *i*) design RTN-resilient multi-bit memory cells, *ii*) choose the optimal reading scheme to minimize RTN effects on RRAMbased PUF circuits, *iii*) design an RTN-based RNG circuit.

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