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Tensile Constitutive Behaviors of FR mortars and HPFRCs

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Abstract

Fiber reinforced mortars (FRMs) and high performance fiber reinforced concretes (HPFRCs) are today widely used as repair and strengthening composites for existing structures, with particular reference to bridges and other concrete structures. Once a strengthening material is available for the market, there is the need of quickly and inexpensively testing its physical characteristics to ensure engineers that the product meets the designer's requirements. Such testing methods, although simple, must be able to correctly characterize the ductility, the tensile strength, the flexural strength as well as to establish a correlation between such parameters. This paper deals with the characterization of the mechanical properties and the ductility indexes of three commercial FRCs. The study focuses on the correlations between the ductility and both the direct and indirect tensile strengths. The obtained experimental data were compared with those provided by a model based on the "Composite Material Theory" (CMT), showing good agreement.

Keywords: Metal-matrix composites; Mechanical properties; Damage mechanics; Mechanical testing

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1. Introduction

The technology of steel fiber reinforced concrete (SFRC) has much evolved in the past years thanks to a great number of researches performed both on the fiber-based materials [6, 13, 27, 29, 15, 32, 26, 28, 39] and on the applications [16, 1, 3, 23, 2]. New shapes and types of steels have been developed to improve the fibers and, in turn, the SFRC performances[4, 5, 12, 31]¹. The mixing procedures of SFRC have been shortened and simplified over the years. SFRC is today largely used to repair and strengthen existing structures (e.g. bridge decks, piers, etc.)². When SFRCs are used as repair and strengthening materials, their mechanical behavior must be known a priori by the designer. The success of the SFRC has promoted the development of a number of commercial products that nowadays are commercially available and produced on large scale and according to precise technical data sheets. The mechanical performances of these commercial FRCs are affected by many parameters, with particular reference to the type of fibers, fibers dosages, geometry of tested specimens, fibers aspect ratio and the test methods also [14, 38, 25, 11, 10, 30]. Laboratory tests characterizing certain properties of SFRC (such as tensile strength, ductility and flexural strengths) are often time consuming and expensive. These characterization procedures are therefore ill-adapted to the need of a rapid and cheap performances control and validation that are usually required by the designers. To aid the practitioners and simplify the procedures, some technical guidelines have been developed and recently adopted in codes [33, 40, 41, 36, 37, 42, 43, 44, 45, 46, 47].

This paper deals with the mechanical characterization of three different SFRCs, two of which are UHPFRCs. The experimental tests have been made according to standard protocols in order to assess the compressive strength, direct tensile strength and flexural strength of the composites. In particular, compressive strength tests on cubic specimens, direct tensile tests on dog-bone specimens and four-point bending flexural tests, performed both on notched and un-notched prismatic specimens, were carried out. The behavior in terms of ductility was assessed accordingly.

The paper is organized as follows. A description about the procedures used to perform the investigation is provided in Section 2. In particular, in

¹Recent studies about FRCs based on synthetic fibers can be found in [17, 24].

²An important issue concerning the mechanical interaction in time between the hosting structure and the reinforcement is addressed in [8, 7, 9].

34 such a Section the experimental tests are described in some detail. Informa-
 35 tion about the concrete mixtures tested are also given in this Section. The
 36 main results provided by the experimental tests are reported and discussed
 37 in Section 3. Finally, conclusions are drawn in Section 4.

38 2. Materials and methods

39 In the present work the mechanical behavior of three different types of
 40 commercial FRCs (termed hereinafter “A”, “B” and “C”), are investigated
 41 through a standard procedure. For each type of mortar the producer pre-
 42 scribes in detail the following items³:

- 43 • Dosages of admixtures (inerts, water/cement ratio, plasticizers, accel-
 44 erators, etc.);
- 45 • Quantity and type of steel fibers (hooked or straight, aspect ratio, etc.);
- 46 • Mixing, flowing and curing procedures.

47 The mix design for getting 1 m³ of each mortar under testing is shown in
 48 Table 1. The solid part (binders and granular skeleton) of each mortar is
 49 different even if all of them were named “premix” by the producers. In fact,
 50 the producers supply the premix in sacks or big-bags that have to be used
 51 as a unit, i.e. a sack cannot be partially used.

material	kg in 1 m ³ of composite		
	A (HPC)	B (UHPC)	C(UHPC)
Premix	2226	2296	1970
Superplasticizer	22.3	43.13	39
Accelerator	-	10	-
Water	231	184	195
Hooked steel fibers 30/0.35 mm	130 (1.7 %)	-	-
Straight steel fibers 20/0.3 mm	-	195 (2.5 %)	-
Straight steel fibers 13/0.175 mm	-	-	296 (3.8 %)

Table 1: Mix design for the SFRCs under testing.

52 A premix usually contains cement, sands and pozzolans. The companies
 53 producing these mortars do not provide the composition of the premix and

³A recent study about a polymer-based mortar for retrofitting is performed in [20].

54 the nature of the compounds and chemicals. Each premix comes with a
 55 superplasticizer used to obtain the target water/cement ratio (that can be
 56 as low as 0.2). The superplasticizer is used at high dosage to increase the
 57 strength, enhance the durability and give high workability [48]. In the “B”
 58 mortar the manufacturers advise to add a set and hardening accelerator to
 59 shorten the dormant period and to speed up the hydration process. The type
 60 of fibers used for these concretes is usually chosen according to the target
 application.



Figure 1: Steel fibers used in the mortars: a) Hooked fibers 30/0.35 mm; b) Straight fibers 20/0.3 mm; c) Straight fibers 13/0.175 mm.

61

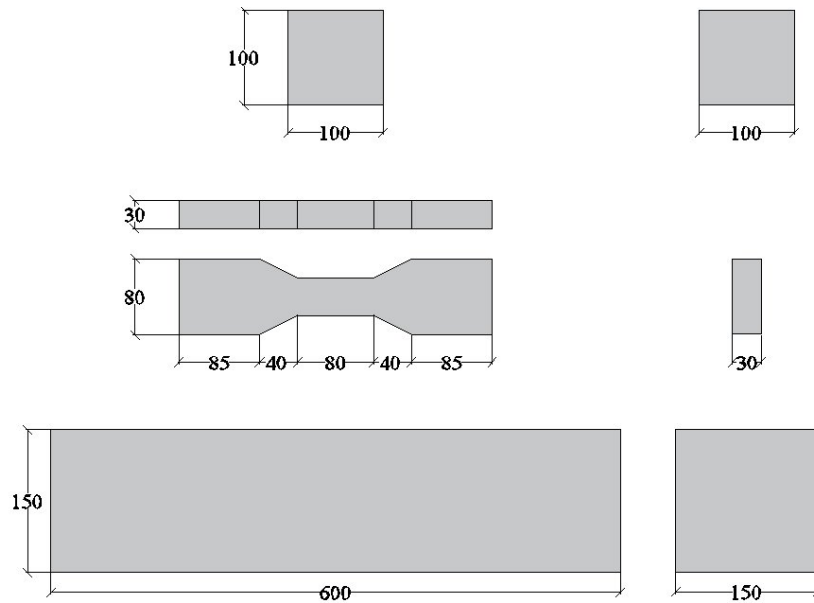


Figure 2: Specimen dimensions.

62 For structural applications steel fibers are usually preferred (see Fig. 1).
 63 Mixing HPC and UHPC requires the use of high intensity mixers. In this
 64 study a 1.5 kW high shear Zyklos rotating pan mixer was used to manufacture
 65 standard specimens to test tensile, flexural and compressive strengths. The
 66 types of tested specimens and their dimensions are shown in Fig. 2.

67 Compressive strength test on cubic specimens, direct tensile test on dog-
 68 bone specimens and four-point bending flexural tests, both on notched and
 69 un-notched prismatic specimens, were carried out. Standard tests configura-
 70 tions are shown in Fig. 3.

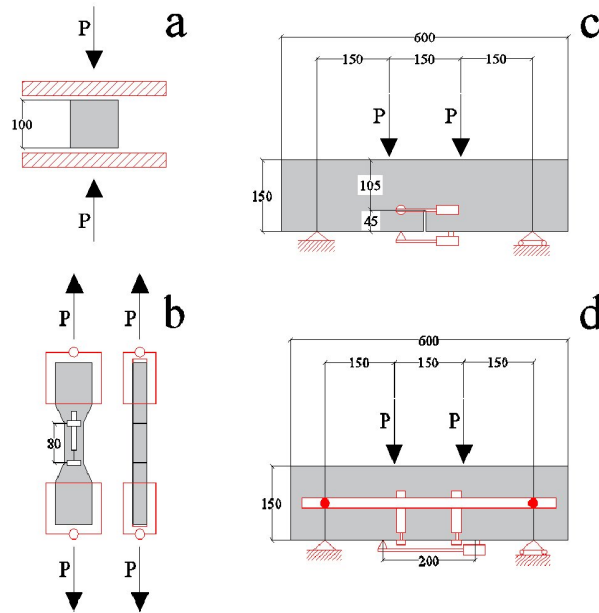


Figure 3: a) Compression test on cubic specimen; b) Direct tensile test on dog-bone specimen; c) Four-point bending test on notched beam specimen; d) Four-point bending test on un-notched beam specimen.

71 *2.1. Compression tests*

72 A compression machine Perrier type 138-5000 kN, as shown in Fig. 4(a),
 73 was used for the compression tests according to [49, 50, 51]. The loading
 74 speed of the compression machine was set to 6 kN/sec.

75 *2.2. Direct tensile test*

76 A machine Walter Bai type LVF-200 kN was used for the direct tensile
 77 test on dog-bone specimens. The rate of the axial elongation was set equal

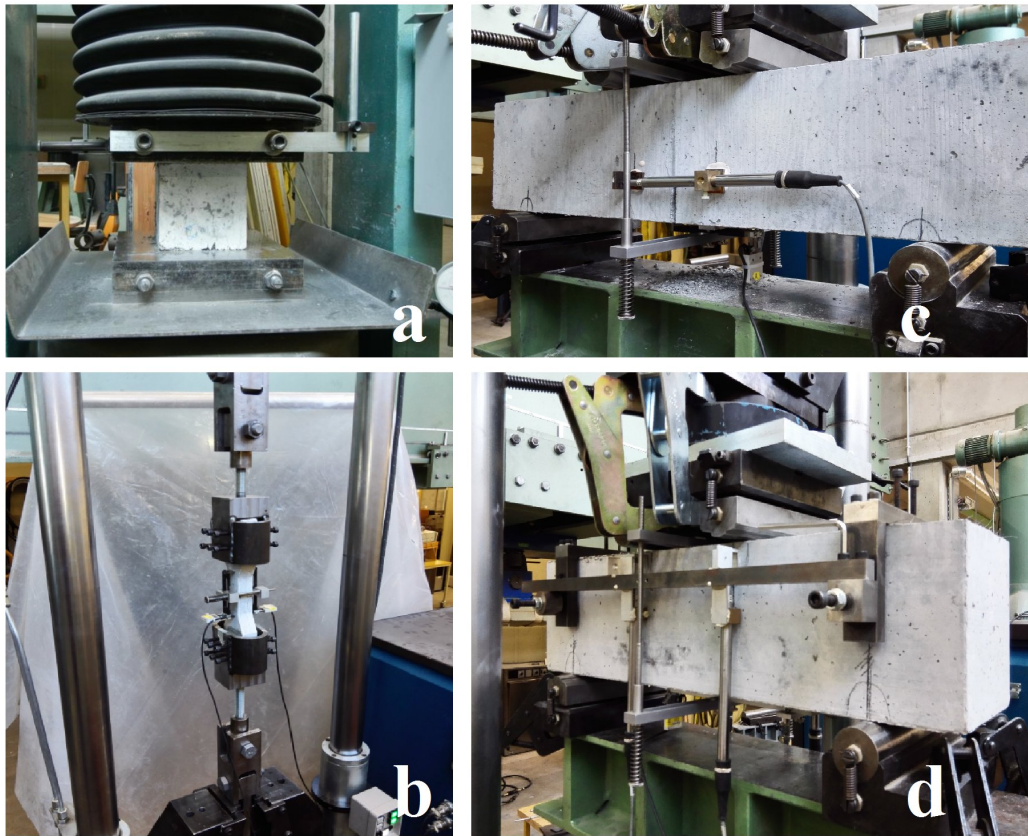


Figure 4: Test machines: a) Machine Perrier type 138-5000 kN used to perform compression tests on cubic specimens; b) Machine Walter Bai type LVF-200 kN used to direct tensile test; c) four-point bending test on notched beams; d) four-point bending test on un-notched beams.

78 to 0.05 ± 0.01 mm/min according to the guidelines and codes employed for
79 performing the experimental investigation [42, 52, 53]. Carrying out direct
80 tensile tests, the specimens must be loaded along their main axis. This is
81 necessary to prevent that bending occurs. A double hinge mechanism was
82 designed specifically to keep the specimen and the load axis aligned. Fur-
83 thermore, it is important to avoid any sliding between the machines clamps
84 and the specimens in order to ensure that the entire load is transferred to the
85 specimen. For this purpose an aluminium plate was glued to the specimen's
86 surface as proposed by [53] and a special clamp was designed to have the
87 maximum grip on the aluminium plate as illustrated in Fig. 4(b). When

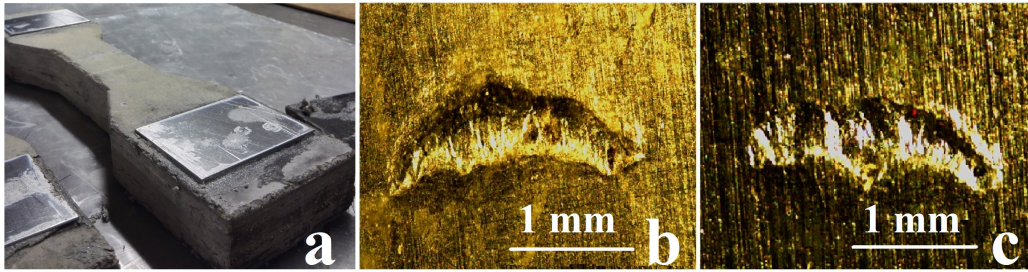


Figure 5: Some pictures related to the direct tensile test: a) Aluminum plate glued on the dog-bone specimen; b) Holes in the aluminum plate before tensile test; c) in the aluminum plate after tensile test.

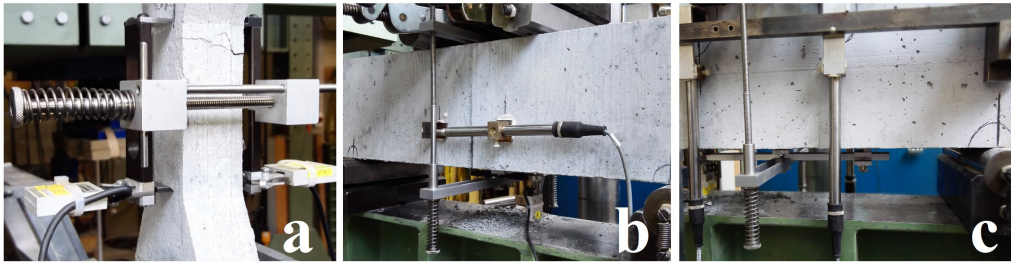


Figure 6: Some pictures related to the extensometers used during the experimental tests: a) The extensometer is placed along the 80 mm characteristic lengths specimen; b) The extensometer is placed at the bottom of the notched beam along 100 mm characteristic length and two LVDT are placed on the sides; c) The extensometer is placed at the bottom of the un-notched beam along 200 mm characteristic length and four LVDT are placed under the rollers loading.

88 comparing the grooves on the aluminium plate glued on specimens prior and
 89 after a direct tensile test (Fig. 5) it can be noted that there are no signs
 90 of groove deformation and therefore no sign of slipping. As previously men-
 91 tioned, the test was carried out by controlling the specimen's axial elongation
 92 rate. A high precision extensometer was placed in each side of the specimens.
 93 The average of the real time elongations measured by the two sensors per-
 94 mitted to the traction machine to keep the programmed rate of deformation
 95 according to [42], see Fig. 6(a).

96 2.3. Four-point bending flexural test

97 The machine Walter Bai type LVF-200 kN was used for carrying out the
 98 four-point bending flexural tests as well. A standard prismatic specimen

99 is placed on two standard cylindrical supports (see Fig. 4(c)) and loaded
 100 through two top rollers placed above the specimen. The distances of the
 101 rollers and the supports were compliant with standards [51, 52, 54]. The
 102 specimens were sawed in the middle section in order to produce a 45 mm deep
 103 v-shaped notch according to [42, 51, 54]. Notched specimens are preferred
 104 by norms for the softening materials because the position of the flexural
 105 crack is known. The crack opening is measured both in the bottom and
 106 in the side of the specimen. Bottom measurement is called Crack Mouth
 107 Opening Displacement (CMOD), and side measurement is called Crack Tip
 108 Opening Displacement (CTOD). The loading speed is controlled by setting
 109 a rate of 0,05 mm/min for the CMOD is imposed until reaching a value of
 110 crack opening of 3.5 mm. Sensors used to monitor the CMOD and CTOD
 111 are respectively one extensometer and two LVDT displacement transducers
 112 with a 100 mm gauge length (Fig. 6(b)). Tests on prismatic un-notched
 113 specimen (Fig.4(d)) have been performed as well according to [52]. In these
 114 tests the gauge length of the sensor was 200 mm and four LVDTs were used
 115 to measure the localized displacement under the top rollers, see Fig. 6(c).

116 3. Results and discussion

117 Each test series encompasses several tests. To avoid confusion, a system
 118 of samples identification was conceived and is displayed in Table 2 with an
 119 example. Three FRC types have been investigated and they are labeled
 120 “A”, “B” and “C”. All of these mortars are commercially available. “A”
 121 and “C” specimens were cast in four different days and on slightly different
 122 environmental conditions. “B” specimens were cast in two different days. The
 123 samples are shown in Fig. 2.

C. . . .	type of FRC	A, B, C
. .2. .	day of casting	1, 2, 3, 4, 5
	beam specimen	1, 2, 3
. . . .8	dog-bone specimens	4, 5, 6
	cube specimen	7, 8, 9

Table 2: Specimen identification.

124 3.0.1. Compressive behavior

125 Strength was tested on 100 x 100 x 100 mm standardly cured cubes. The
126 peak value, the average value and the coefficient of variation (COV) of the
127 measured compressive stress acting on the sample have been calculated (see
128 Table 3):

$$f_{ci} = \frac{P_i}{A_i}, \quad f_{Cm} = \frac{\sum_{i=1}^n f_{Ci}}{n}, \quad COV = 100 \cdot \frac{\sigma}{n}, \quad (1)$$

129 being f_{Ci} the cubic compression in tension of a specimen; P_i the maximum
130 load recorded during the test; A_i the cross section area of the uniformly
131 loaded specimen; R_{cm} the average value of the tension in a campaign of n
132 specimens; σ the standard deviation and n the number of specimens.

133 The samples of all series shown a similar type of failure. As shown in Fig.
134 7 the fibers, randomly oriented in the cement matrix, have a higher level of
135 confinement which prevented the classical pyramid failure (usual for plane
136 concrete cubes). It is important to note the beneficial effect of the fibers
137 which avoid the separation of the specimen into separate pieces⁴.

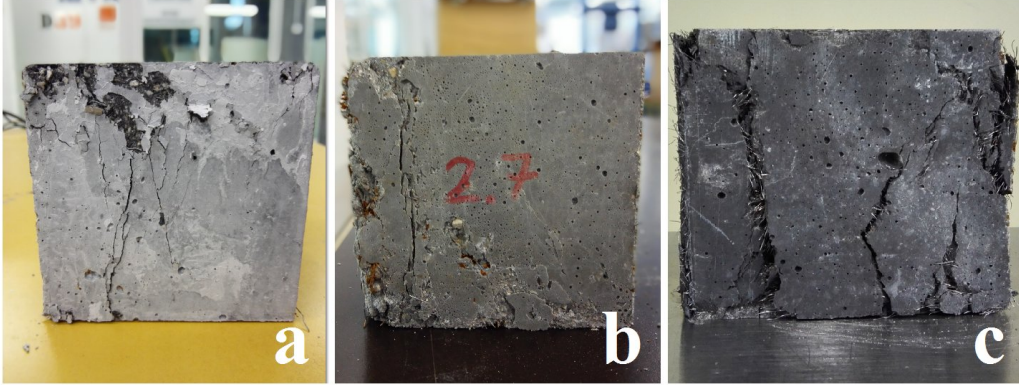


Figure 7: Cracking of samples subjected to the compression test: a) “A” mortar; b) “B” mortar; c) “C” mortar.

⁴Fracture can be modelled, in a nonlinear framework, following [34], whereas recent contributes about damage mechanics can be found in [18, 19, 21]. Bifurcation and stability in the context of homogeneous finite deformations can be found in [35].

138 *3.0.2. Tensile behavior in direct tensile test*

139 Table 3 reports the peak load, the average tension as well as the COV
140 of the cross cracking section of the dog bone specimens. The tensile stress
141 σ_N is obtained by dividing the measured tensile load by the area of the
142 nominal cross section at the crack location (30x40 mm², in this case). The
143 total elongation δ (deformation) is obtained by multiplying the axial strain
144 (specific deformation) measured by the characteristic length of the sensors
145 (80 mm). The tensile load-elongation curves $\sigma_N - \delta$, obtained by testing dog-
146 bones specimens, are shown in Fig. 8. It can be observed a series of sudden
147 drops of tensile stress during the load tests in a number of specimens of
148 mortars B and C. These crests and troughs in the stress-strain graphs often
149 occur in SFRC tests and they are caused by one or a combination of the
150 following mechanisms which can be recognized during the crack generation
151 and growth in FRC:

- 152 • *Fiber failure.* It is the less common phenomenon and it happens usually
153 in long fibers, where the bond is so high that the fiber can reach rupture.
- 154 • *Fiber pull-out.* This is the mechanism that dissipates less energy and
155 it's the most common in straight fibers.
- 156 • *Fiber bridging.* Fibers link the two edges of the crack and the stress can
157 be transferred through them. This is the most common phenomenon
158 in non-straight fibers. The energy is absorbed by the deformation of
159 the fiber.
- 160 • *Fiber/matrix debonding.* Like the fiber failure, this happens usually in
161 long and well bonded fibers.
- 162 • *Matrix crack.* The fiber can contrast the propagation of micro-cracking
163 through the matrix spreading the energy of the crack on a wider surface.

164 By observing the graphs in Fig. 8 it might be concluded that the crests
165 and troughs affecting the experimental curves about mortars “B” and “C”
166 are linked to the pull-out of the straight fibers used in these SFRCs. The
167 pull-out mechanism was prevented in SFRC “A” by the use of hooked fibers.
168 Dog-bone specimens of “A” SFRC specimens showed also a multi cracking
169 behavior (Fig. 9), probably ascribable to the use of hooked fibers [22]. The
170 hooked part of the fibers tend to prevent the total extraction of the fibers and
171 ensures a higher degree of load redistribution. A multi cracking behavior is

Specimen	f _i (MPa)	f _m (MPa)	COV (%)	Specimen	f _i (MPa)	f _m (MPa)	COV (%)	Specimen	f _i (MPa)	f _m (MPa)	COV (%)
A.1.1	26.51			A.1.4	6.52			A.1.7	88.47		
A.1.2	29.00			A.1.5	5.60			A.1.8	82.75		
A.1.3	30.45			A.1.6	5.79			A.1.9	86.29		
A.2.1	43.68			A.2.4	7.51			A.2.7	81.85		
A.2.2	32.87	34.52	16.25	A.2.5	6.77			A.2.8	92.38		
A.2.3	39.03			A.2.6	6.90			A.2.9	95.89		
A.3.1	30.50			A.3.4	5.42	6.30	11.52	A.3.7	90.21	86.42	5.06
A.3.2	40.54			A.3.5	5.94			A.3.8	83.19		
A.3.3	38.08			A.3.6	6.38			A.3.9	81.41		
A.4.1	26.61			A.4.4	6.15			A.4.7	83.27		
A.4.2	30.67	29.27	6.44	A.4.5	5.20			A.4.8	87.21		
A.4.3	30.54			A.4.6	7.46			A.4.9	84.12		
B.1.1	60.36			B.1.4	10.31			B.1.7	154.25		
B.1.2	58.18			B.1.5	10.44			B.1.8	156.52		
B.1.3	67.63			B.1.6	10.02			B.1.9	151.32		
B.2.1	75.92	66.69	9.31	B.2.4	14.80	11.84	15.40	B.2.7	151.95	151.08	2.56
B.2.2	65.72			B.2.5	11.76			B.2.8	147.24		
B.2.3	72.32			B.2.6	13.73			B.2.9	145.22		
C.1.1	62.08			C.1.4	14.45			C.1.7	148.65		
C.1.2	77.72			C.1.5	11.76			C.1.8	153.98		
C.1.3	65.75			C.1.6	11.28			C.1.9	149.11		
C.2.1	82.16			C.2.4	12.43			C.2.7	144.24		
C.2.2	75.63			C.2.5	11.55			C.2.8	146.58		
C.2.3	82.81			C.2.6	14.49			C.2.9	140.87		
C.3.1	77.72	71.52	10.20	C.3.4	13.85	13.06	8.49	C.3.7	148.51	148.61	2.54
C.3.2	62.53			C.3.5	13.80			C.3.8	153.53		
C.3.3	63.83			C.3.6	13.67			C.3.9	149.04		
C.4.1	71.50			C.4.4	13.80			C.4.7	147.08		
C.4.2	71.47			C.4.5	13.58			C.4.8	147.58		
C.4.3	65.05			C.4.6	12.11			C.4.9	154.16		

Table 3: Results.

172 always desirable in concrete since it indicates an augmented ductility of the
173 specimen under tension and bending. It is also well-known that an improved
174 ductility and a multi cracking behavior are necessary to have high rotational
175 capacity and good stress redistribution in certain structural elements. Direct
176 tensile tests carried out on dog-bones specimens are initially characterized
177 by an elastic phase. In this phase the contribution of the fibers could not
178 be decoupled, since the matrix characteristics are governing the behavior
179 of the SFRC. Instead, the post-peak phase was strongly influenced by the
180 contribution of the fibers. After the appearance of the first crack, located in
181 the central area of the specimen in B and C series and diffused along the mid-
182 length of the specimen in the series A (Fig. 9), the matrix does not contribute
183 any longer to the resistance. The stresses are transferred completely from the
184 matrix to the (activated) fibers and from the activated fibers to the matrix

185 thanks to the interfacial bond strength. The fibers, bridging the cracks,
186 transfer a part of the load in areas of the specimens that are not yet cracked.
187 Thanks to their slow pull-out resistance and their high ductility, during the
188 growth of the crack opening, a considerable amount of energy is dissipated.
189 This energy dissipation is highlighted by the length of the post-peak curve
190 as well as by the large areas under the graphs (see Fig. 8).

191 *3.1. Tensile behavior by four-point bending flexural test*

192 It is common practice to evaluate the tensile strength of concrete by
193 means of flexural tests. Although well established, this type of test has some
194 limitation when it comes to define the real tensile strength of materials such
195 as SFRC. In this study the flexural strength was evaluated by tensile and
196 flexural tests and a correlation between the two was established by means of
197 the “Composite Material Theory”. Table 3 shows the peak load, the average
198 and the COV of the flexural tests. These values and in particular the nominal
199 tension stress σ_N were determined assuming that all the materials remained
200 in the elastic field until failure [42]. The test campaign of SFRC “A” included
201 both notched and un-notched specimens: The tests series A.4 was carried
202 out on un-notched specimens. Most of the tests in all series were carried-
203 out on notched specimens (see Table 3). Results of flexural tests on notched
204 specimens are shown in Fig. 10. Fig. 10 presents the nominal tension-CTOD
205 ($\sigma_N - w$) curves of notched prismatic specimens.

206 A comparison between notched and un-notched prisms of the test se-
207 ries A.4 permitted to highlight that the un-notched specimens had a multi-
208 cracking behavior (although not pronounced) while notched specimens pre-
209 sented a single crack localized in the middle-span (Fig. 11).

210 Even though the notched specimens did not show a multi-cracking be-
211 havior, the great contribution of the fibers to the ductility was evident. The
212 contribution of fibers to the ductility is easier to be observed in bending rather
213 than in direct tensile test since the flexural test promote the formation of a
214 plastic region in the neighborhood of the middlespan, thus permitting to the
215 specimen important rotations. This plastic behavior is obtained only if the
216 fiber volume exceeds the critical value $V_{f,crit}$. The critical volume of the fibers
217 varies with the matrix and fibers characteristics.

218 *3.1.1. The composite material theory applied to SFRC*

219 According to the Composite Material Theory (CMT), the critical volume
220 of fibers that might promote a strain-hardening behavior can be obtained

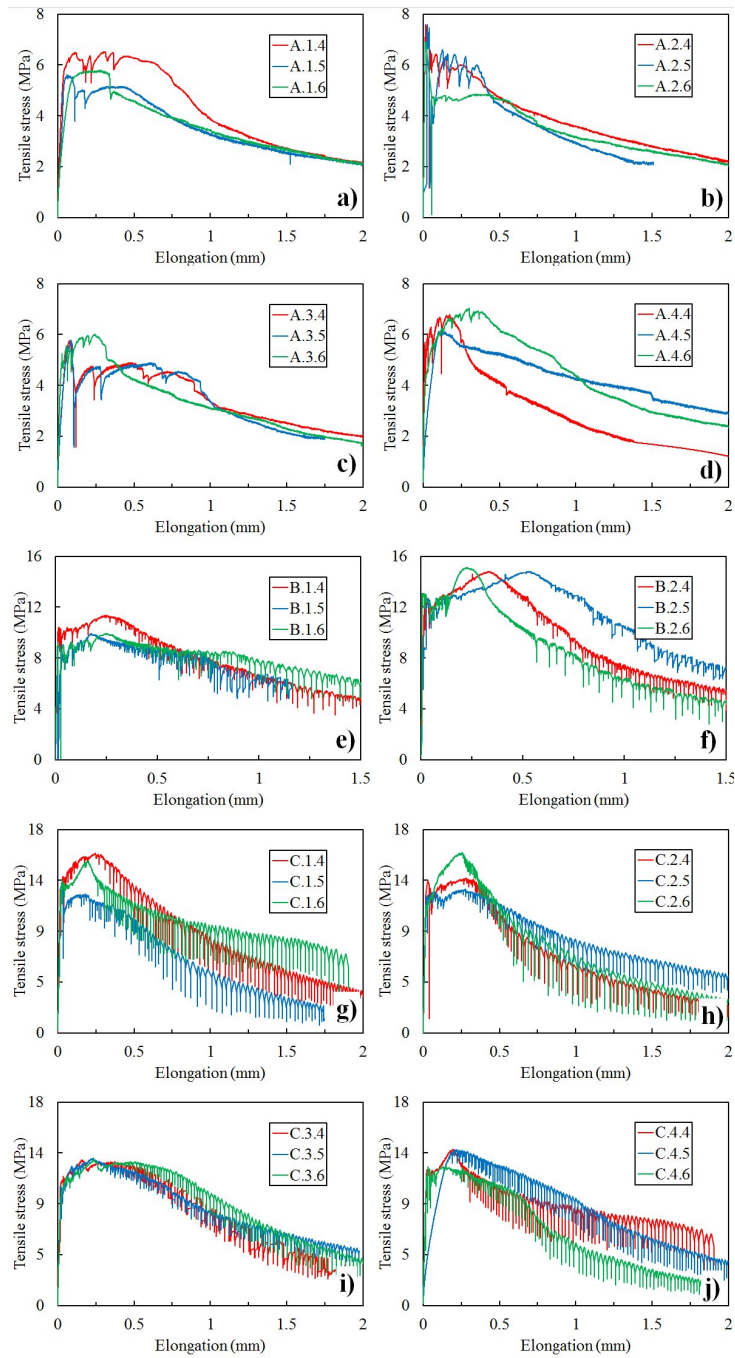


Figure 8: Tensile tension-elongation curves from direct tensile test on the dog-bone specimen series.

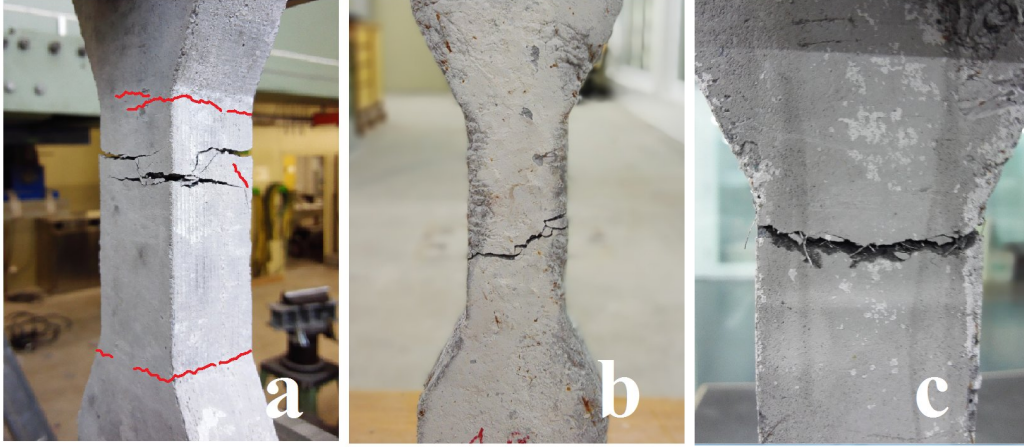


Figure 9: Tensile cracking: a) “A” mortar; b) “B” mortar; c) “C” mortar.

221 computationally by equating the normal stress acting on the composite σ_c
 222 before and after cracking. Before cracking the normal stress acting on the
 223 composite is

$$\sigma_c = V_{f,crit} E_f (1 - V_{f,crit}) \sigma_{mu} \quad (2)$$

224 whereas after the specimen cracks, the matrix does not contribute any longer
 225 to sustain the load and stresses are transferred to the active fibers crossing
 226 the cracked section. Then, in this case the tension of the composite becomes
 227

$$\sigma_c = V_{f,crit} \sigma_{fu}. \quad (3)$$

228 By equating (2) and (3) the critical fiber volume that promotes a hardening
 229 behavior under direct tensile stress is obtained

$$V_{f,Cr} = \frac{\sigma_{mu}}{\sigma_{fu} - E_f \epsilon_{mu}}, \quad (4)$$

230 where σ_{mu} is the maximum matrix tension just before the cracking; ϵ_{mu} is
 231 the corresponding deformation which, according to the assumption of perfect
 232 adhesion, is the same for steel fibers; σ_{fu} is the failure tension of the fibers
 233 (rupture or pull-out); E_f is the elastic modulus of the steel fibers.

234 If the volume of the fibers in the composite exceeds the critical threshold
 235 $V_{f,crit}$, a hardening post-peak behavior will be expected. If the volume of
 236 fibers is below the critical threshold, then a softening post-peak behavior
 237 will be observed. In order to calculate the critical volume of fibers $V_{f,crit}$,

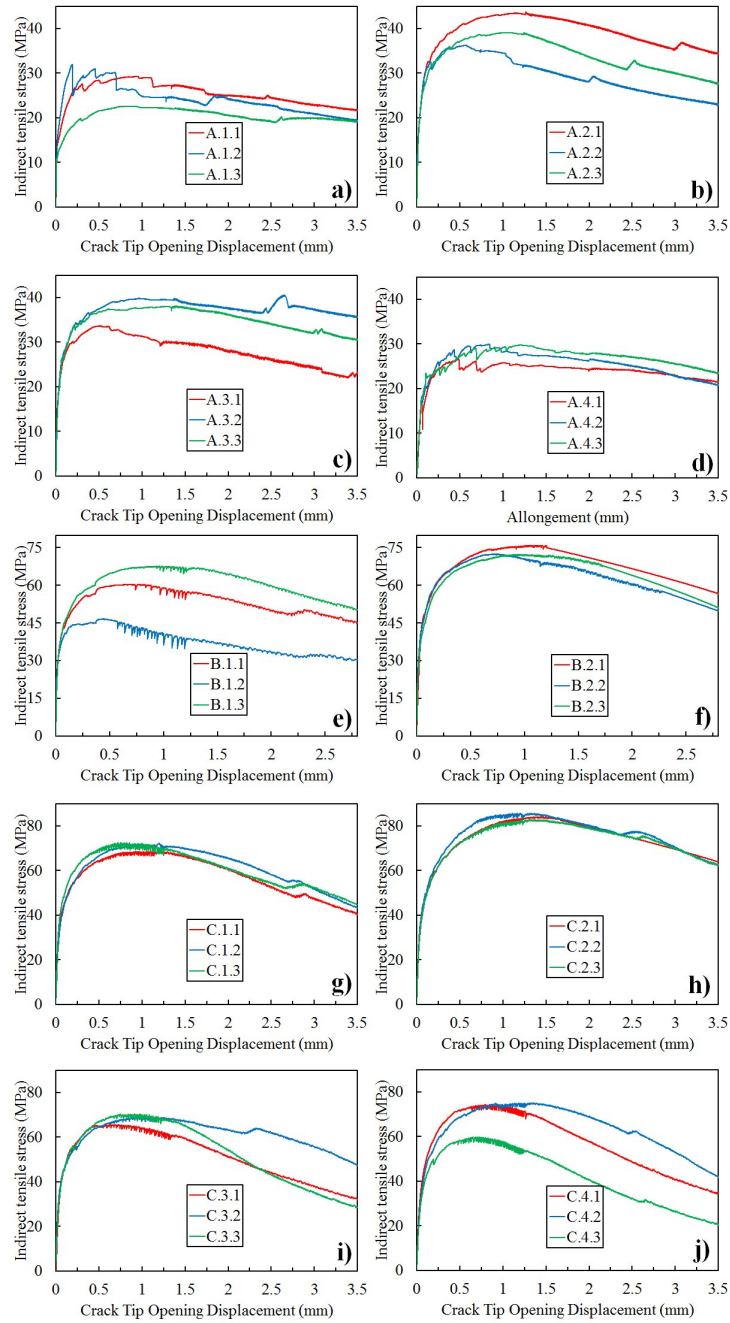


Figure 10: Tension-CTOD by flexion curves from four-point bending flexural test on prismatic specimens.

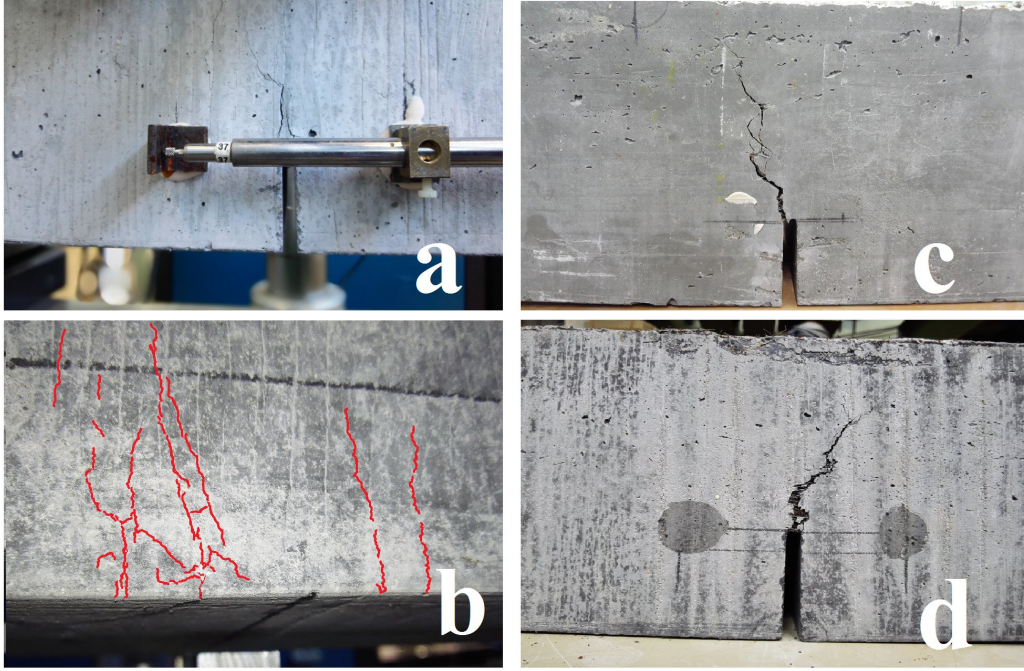


Figure 11: Failure modes observed during the loading bending tests: a) Mono-cracking behavior of notched beam A; b) multi-cracking behavior of un-notched beam A; c) mono-cracking behavior of notched beam B; d) mono-cracking behavior of notched beam C.

238 it is firstly necessary to model the stress distribution in the cross-section.
 239 The pre-peak stress distribution in the cross section can be modeled as in
 240 Fig. 12(a) with the tension stresses σ_{mu} and σ_{comp} having the same value.
 241 The post peak behavior can be modeled as in Fig. 12(b), where σ_{cu} is the
 242 ultimate strength of the composite reached in post-cracking phase. If the
 243 neutral axis depth is defined to be equal to $H/4$; the two ultimate bending
 244 moments (pre-peak $M_{R,a}$ and post-peak $M_{R,b}$) can be expressed as follows:

$$M_{R,a} = \frac{\sigma_{mu}BH^2}{6}, \quad M_{R,b} = \frac{\sigma_{cu}BH^2}{32}, \quad (5)$$

245 where H and B are the dimensions of the cross section.

246 By equating the moments it follows:

$$\sigma_{cu} = 0.41\sigma_{mu} \leftrightarrow \sigma_{mu} = 2.44\sigma_{cu}, \quad (6)$$

247 and

$$M_{R,b} \geq M_{R,a} \leftrightarrow \sigma_{cu} \geq 0.41\sigma_{mu}. \quad (7)$$

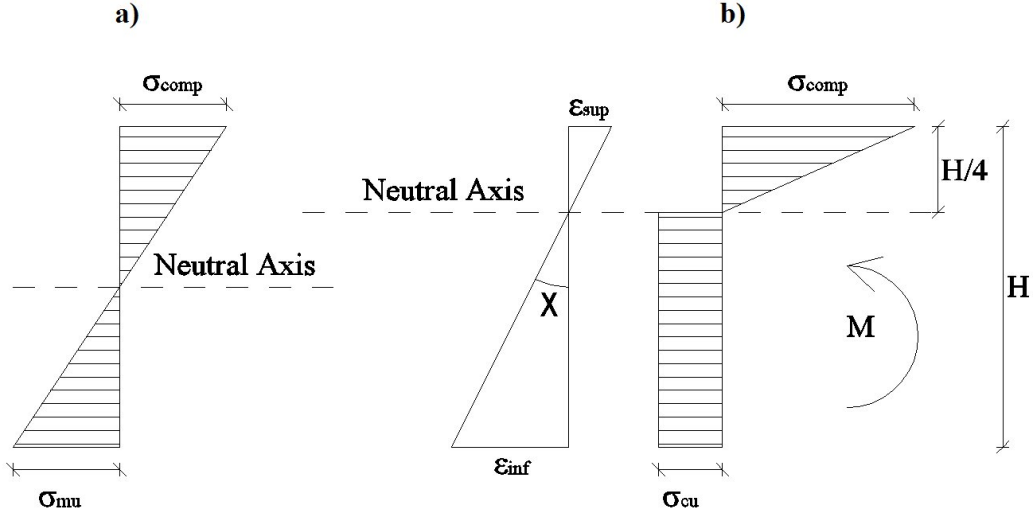


Figure 12: Stress and strain distributions on the cross section of a bent beam: a) Stress distribution before the matrix cracking; b) stress distribution in a post-cracking phase.

248 The fibers volume that is the boundary between hardening and softening
 249 behavior in flexion can be obtained by inserting (6) into (3)

$$V_{f,crit,flexion} = 0.41 \frac{\sigma_{mu}}{\sigma_{fu}} \cong 0.41 V_{f,crit,traction}. \quad (8)$$

250 Eq. (8) proves that the hardening behavior in bending stress is also ob-
 251 tained reducing the volume of fibers request to obtain the hardening behavior
 252 under tensile load. Fig. 13(a) shows the tensile stress-strain curve obtained
 253 by applying (2) and (3) under the hypothesis that the volume of the fibers
 254 is equal to $V_{f,crit,traction}$. Fig. 13(b) shows the tensile stress-strain curve ob-
 255 tained by applying (5)a and (5)b under the hypothesis that the volume of
 256 the fibers is equal to $V_{f,crit,traction}$. Fig. 13(a) shows that, under pure ten-
 257 sion, a post peak plastic plateau will appear, since the volume of fibers is the
 258 critical volume. Fig. 13(b) shows a hardening behavior post cracking and
 259 maximum tension strength equal to 2.44 times the peak obtained in direct
 260 traction. Fig. 14(a) shows the tensile stress-strain curve obtained by apply-
 261 ing (2) and (3) under the hypothesis that the volume of the fibers is equal
 262 to $V_{f,crit,flexion}$. Fig. 14(b) shows the tensile stress-strain curve obtained by
 263 applying (5)a and (5)b under the hypothesis that the volume of the fibers
 264 is equal to $V_{f,crit,flexion}$. In this case a softening behavior is seen under pure
 265 tensile stresses with the stress decreasing to 0.41 the max stress. A plastic

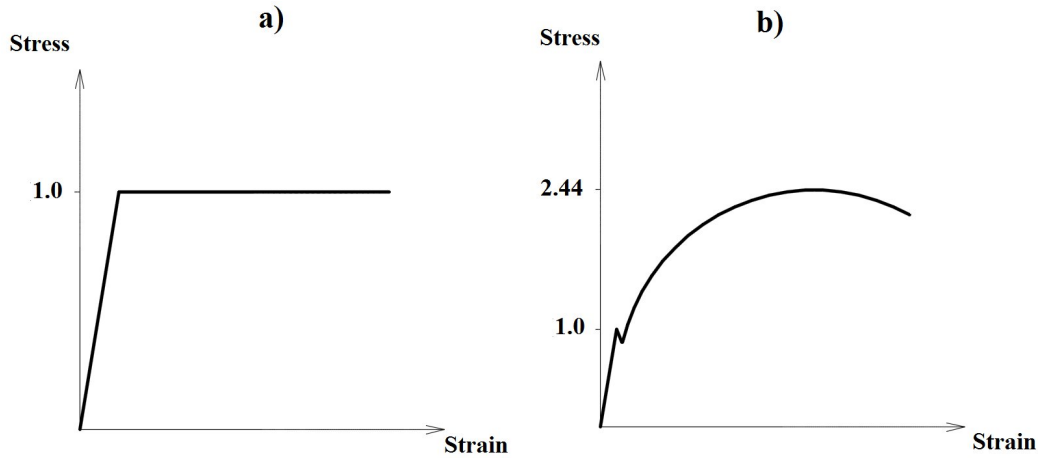


Figure 13: a) Direct tensile curve; b) indirect tensile curve by flexion test with a volume of fibers equal to $V_{f,crit,traction}$.

266 plateau is observed under bending (Fig. 14(b)). This simple application of
 267 the Composite Material Theory (CMT) is sufficient to explain how the tensile
 268 strength obtained by flexural tests is always higher than the value obtained
 269 in direct tensile tests. The CMT, due its simplicity might be misleading since
 270 many assumptions are made. Nevertheless the CMT builds a link between
 271 flexural and tensile strength of a SFRC that might prove useful is carefully
 272 verified for a specific commercial SFRC. Fig. 15 shows the direct tensile and
 273 flexural stress-strain curves obtained by testing specimens in tension and in
 274 bending. The similarity of diagram of Fig. 14 and Fig. 15 is evident.

275 3.1.2. Tensile stress-strain models under bending and direct tensile load

276 According to the standard used in this study [52], a bilinear tensile stress-
 277 strain model can be derived from test data based on three parameters: The
 278 tensile strength at the end of the elastic phase, the corresponding strain and
 279 the tensile strength at the end of the softening branch. Fig. 16 shows the
 280 test data (dog bones) and the curve obtained by the bilinear model derived
 281 according to the standard. On SFRC A model, due to the high COV, first
 282 and ultimate tensile strength values have been penalized more than 50%. In
 283 SFRC B model the reduction of 52% for the first and 37% for the last tensile
 284 strength values was caused by a COV of 16% and 8%, while in SFRC C a
 285 37% and 52% of reduction is due to COV of 9% and 18%. The different
 286 COVs and behavior of the three SFRCs can be explained by a number of

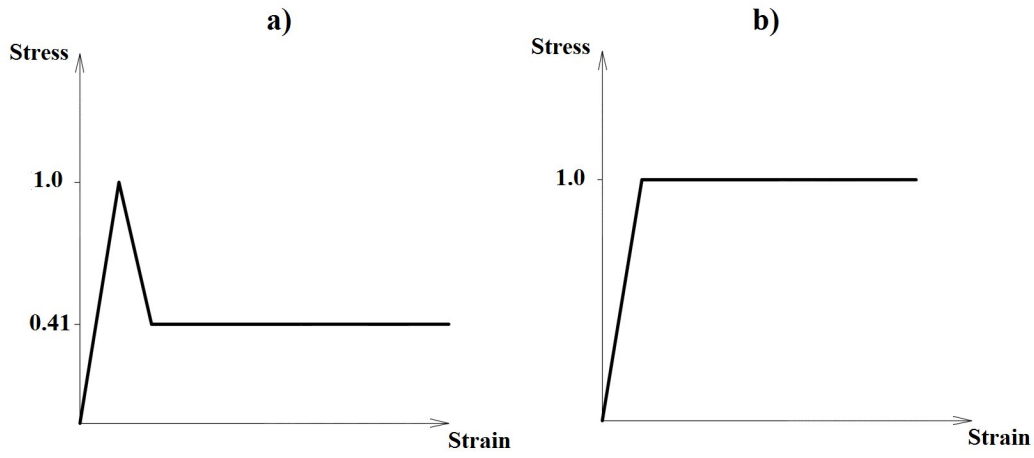


Figure 14: a) Direct tensile curve; b) indirect tensile curve by flexion test with a volume of fibers equal to $V_{f,crit,flexion}$.

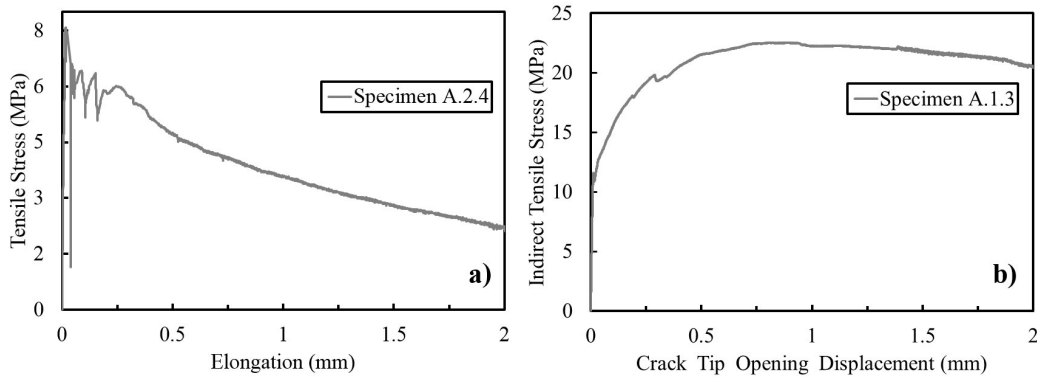


Figure 15: Experimental curves: a) direct tensile test on the specimen A.2.4; b) indirect tensile test provided by bending test on the specimen A.1.3.

287 factors. The most important ones, according to [55], are the fibers dosage,
 288 the geometry of the tested specimen (thickness, in particular), aggregate,
 289 fiber size and fiber orientation. Fiber dosage is one of the most important
 290 factors of COV variation since a higher dosage of fibers should promote a
 291 more even distribution of fiber [11]. As shown in Table 1 the fibres dosage in
 292 SFRCs is 1.7%, 2.5% and 3.8% for mortars A, B and C respectively. In fact
 293 the COV related to mortar A is slightly larger than that concerning mortar
 294 C. Fiber dosage seems to be less significant for indirect tensile strength for
 295 which the COV was about 20% for all notched specimens of A, B and C

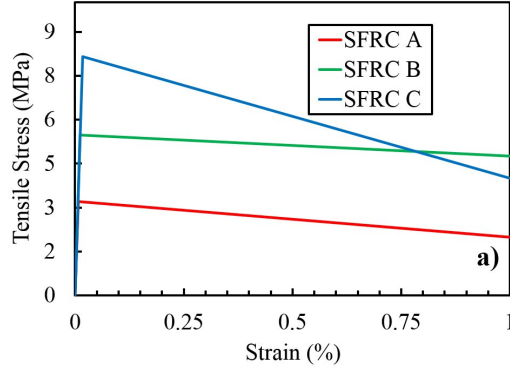


Figure 16: Standard bilinear tensile model.

296 mortars [25]. The COV in un-notched beams (SFRC A) is less than 6%.
 297 The ductility indexes and the tensile strength class, that serves to compare
 298 and choose between different commercial SFRCs, can be assessed according
 299 to [54]. These indexes are obtained from the models derived by the method
 300 proposed by the same standard. Table 4 shows the classification according to
 301 ductility and tensile strength standard indexes [54]. Data obtained by testing
 302 can be used to construct bilinear tensile constitutive law based on regression
 303 analysis. This model was developed for each SFRC and is shown in Fig. 17.
 304 Using this bilinear constitutive law, the CMT presented in section 3.3 and
 305 the parabola-rectangle compression law according to [56] an indirect tensile
 306 stress-strain model was derived for each SFRC. Fig. 18 shows a comparison
 307 of the experimental (bending) indirect tensile stress - CTOD results with the
 308 results of the analytic model for each concrete. Test results and predictions
 309 obtained with the CMT significantly agree.

Class	F2.0	F2.5	F3.0	F3.7	F4.5	F5.5	F6.5	F7.7	F9.0
$f_{11k,min}$ (Mpa)	2	2.5	3	3.7	4.5	5.5	6.5	7.7	9
Index of ductility	Softening			Plastic			Hardening		
$D_{0k,min}$	D_{S0}	D_{S1}	D_{S2}	D_P		D_{H0}	D_{H1}	D_{H2}	
	≤ 0.5	≥ 0.5	≥ 0.7	≥ 0.9		≥ 1.1	≥ 1.3	≥ 1.55	
Classification							A	B	C
SFRC							(HPC)	(UHPC)	(UHPC)
Class F							F6.5	>F9.0	F7.7
Class D_0							D_{S1}	D_{S1}	D_{S1}
Class D_1							D_{S0}	D_{S2}	D_{S2}

Table 4: Classification of the SFRCs according to UNI 11039-2:2003.

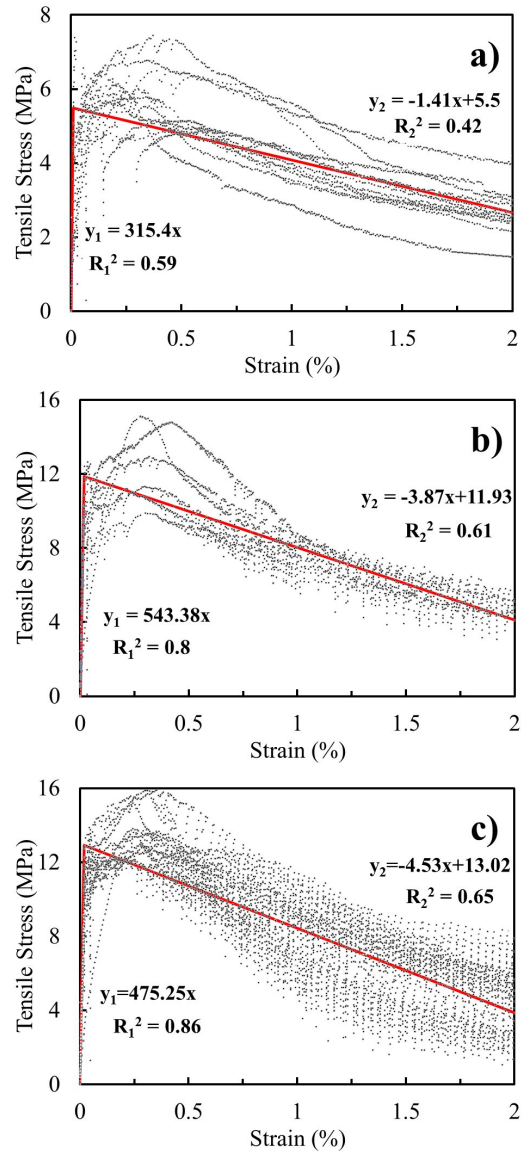


Figure 17: Standard Experimental bilinear tensile model for a) SFRC A; b) SFRC B; c) SFRC C.

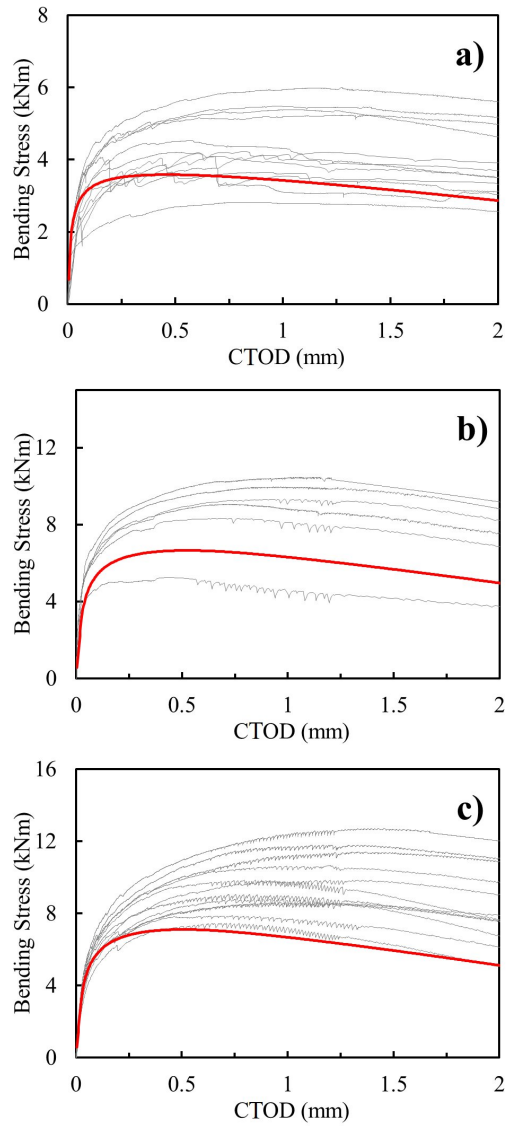


Figure 18: Predictive model Bending Stress-CMOD for a) SFRC A, b) SFRC B, c) SFRC C

310 4. Conclusion

311 This paper presents the mechanical characterization of three different
312 SFRCs, two of which are UHPFRCs. The tests have been made according
313 to recent standard protocols for compressive strength, direct tensile strength
314 and flexural strength. The behavior in terms of ductility was assessed accord-
315 ing to standards and rated. A tensile constitutive law have been constructed
316 for each concrete and used to predict the indirect tensile stress-strain be-
317 havior. Based on the experimental evidence and on the data analyses, the
318 following conclusions can be drawn.

319 Stress-strain models proposed by codes are sensible to the COV of the tests
320 results. Therefore, a concrete with a greater dispersion of the test results
321 might be rated lower, in term of ductility and strength, that a less perfor-
322 mant concrete.

323 Hooked fibers and higher aspect ratios promote a more ductile behavior and
324 they are proved to be more efficient in providing ductility than a stronger
325 matrix bonding straight fibers w/o higher aspects ratios. This conclusion is
326 drawn on a limited number of tests and therefore must be further confirmed.
327 All test results obtained with four points bending tests were compared with
328 a model based on the CMT, showing good agreement. The CMT clearly
329 explains the differences of the post-peak behavior of the tests carried out in
330 a four-point bending and under direct tensile stress.

331 The purpose of the standards used in this study is to supply a fast and in-
332 expensive method for conformity control of a SRFC to be used in field. All
333 tested commercial SFRCs have been classified as low ductility. This might be
334 the effect of the test protocols that might not to be able to fully characterize
335 the stress-strain and ductility characteristics of all SFRC. Nevertheless the
336 principle that it exist a mixture-intensive correlation between the direct and
337 indirect tensile strengths of a SFRC has been found to be true.

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Supplementary data

The raw/processed data required to reproduce these findings cannot be shared at this time due to time limitations. However the Authors will provide them soon.

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